



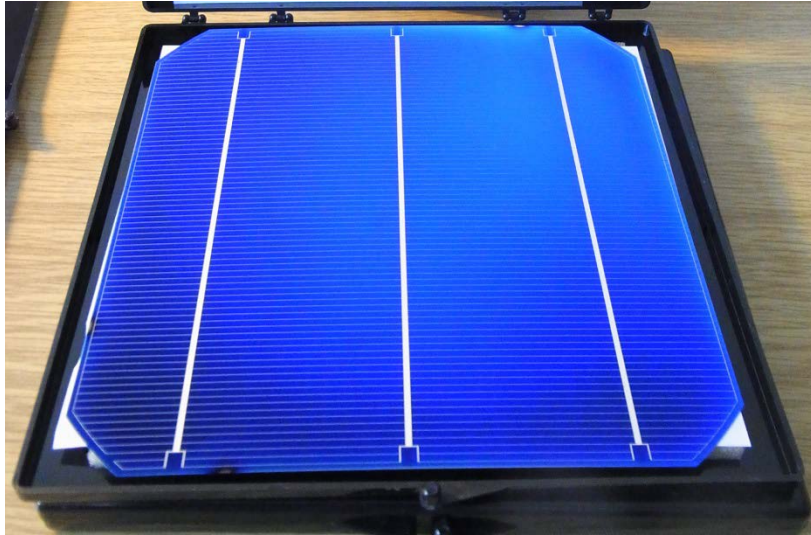
# **Konfektionierung einer 50mm x 50mm Solarzelle aus einer größeren Zelle**

PV-Praktikum

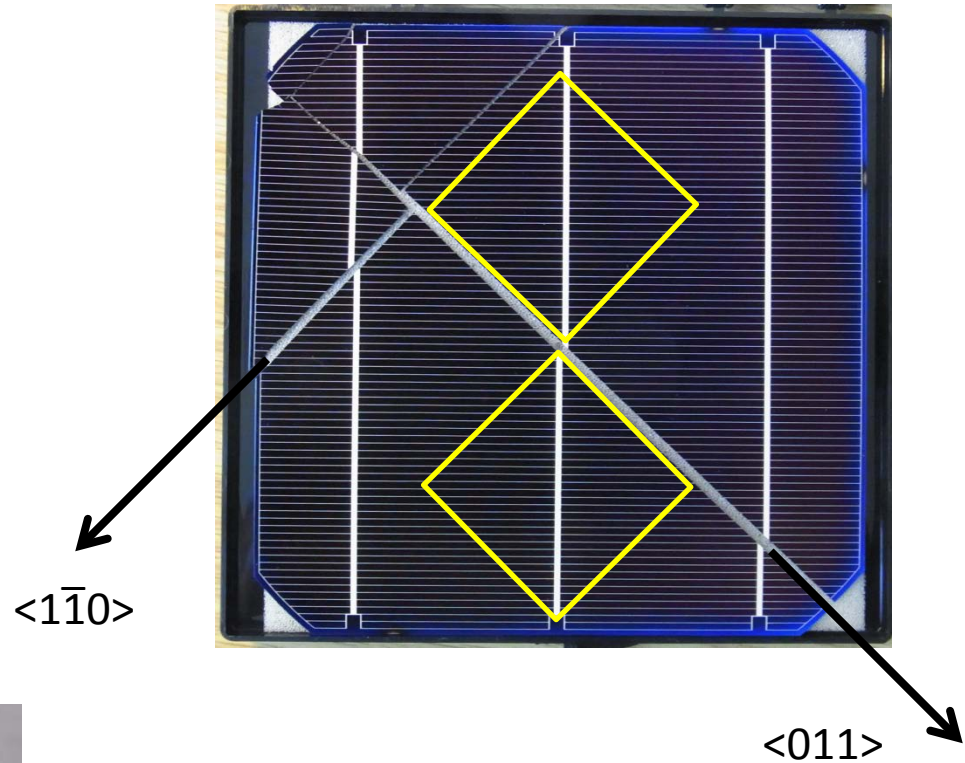
**Ritzen/Brechen - Kleben - Löten -  
Kontaktmontage**

Technische Universität Dresden  
Institut für Angewandte Physik  
Lehrstuhl für Halbleiterphysik

# Cut-out of 50 mm x 50 mm test structures

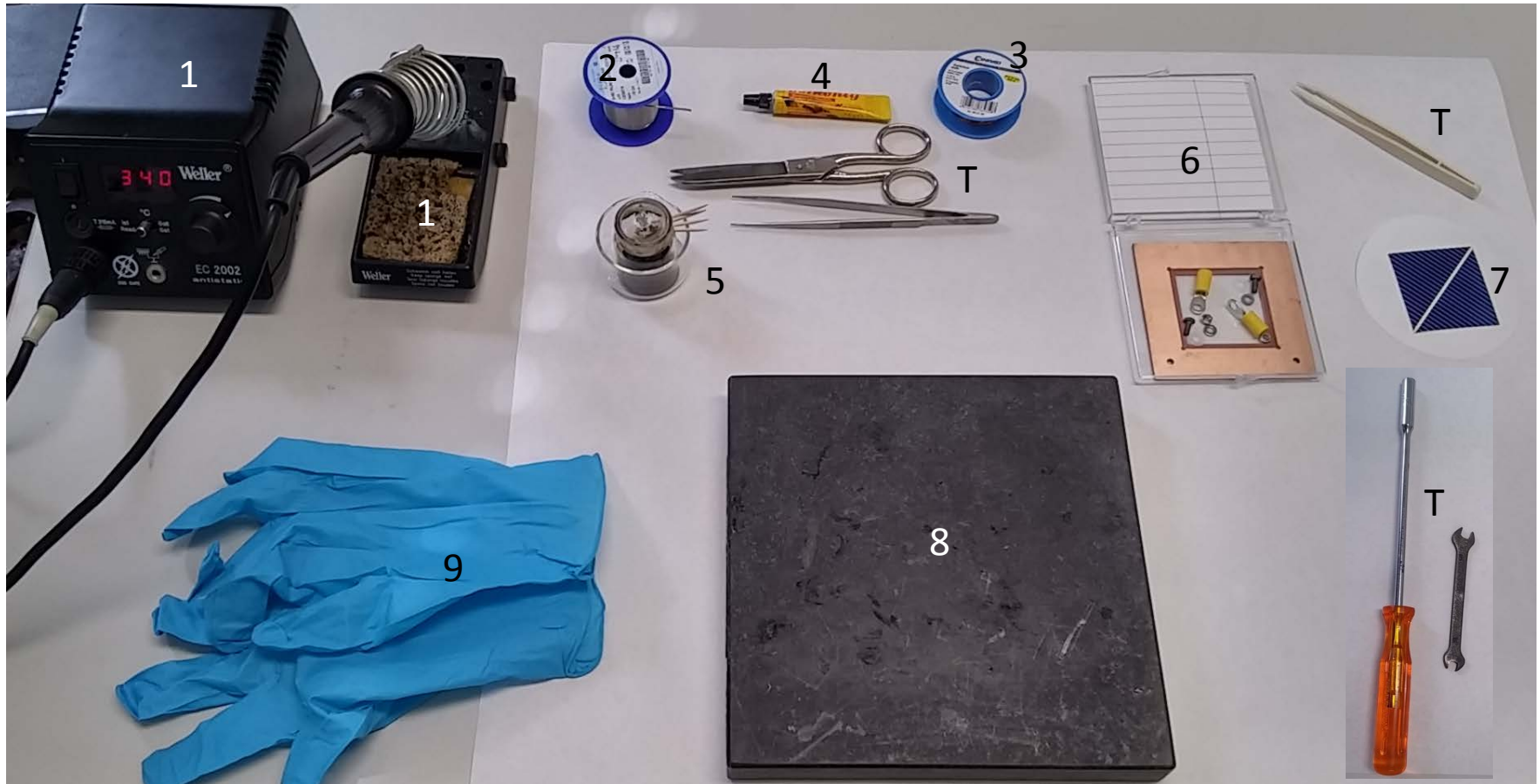


Complete Cz-Si solar cell



50 mm x 50 mm test structure

# A set of necessary materials and instruments



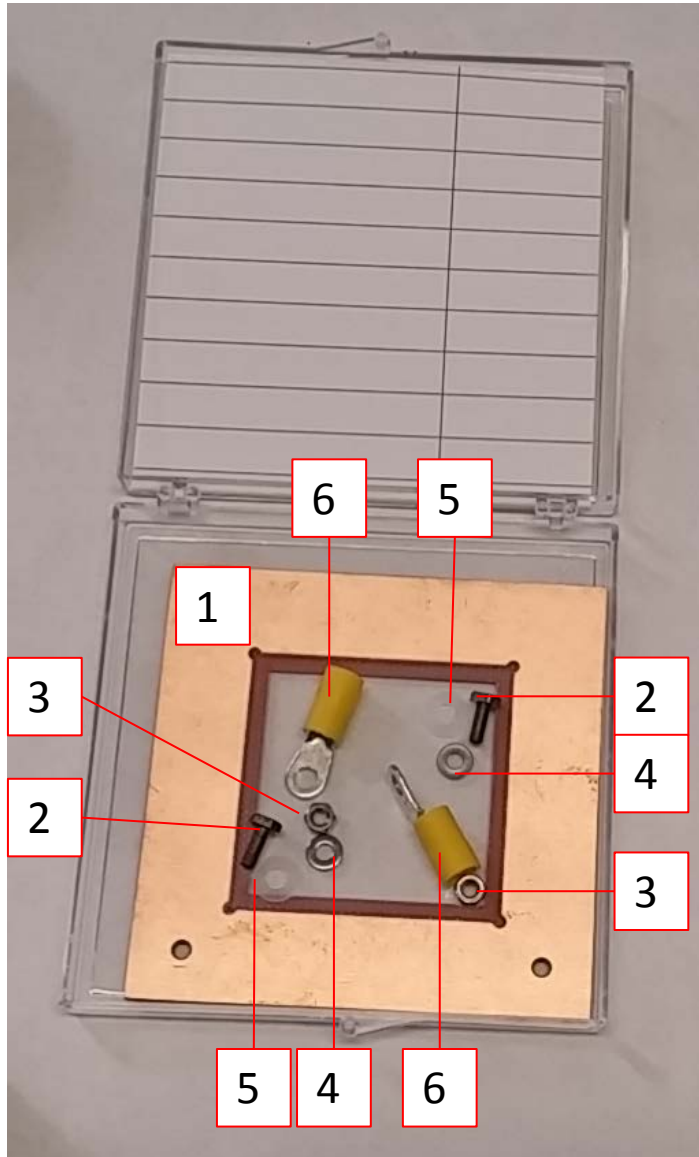
1. Soldering Iron (30 Watt);
2. Solder wire  $\text{Sn}_{60}/\text{Pb}_{38}/\text{Cu}_2$  (Flutin 1532);
3. Cu wire ( $\varnothing$  0.15 mm);

4. Lothonig Super Flux (775-95);
5. Varnish (Asphaltlack);
6. Assembly kit (see next page);
7. Test Structure;

7. Stone plate;
8. Gloves;
- T. Tools.



# Assembly kit



1. Frame (Pertinax plate with Cu cladding on both sides);
2. Stainless steel screws M3 ( $\times 2$ );
3. Stainless steel nuts M3 ( $\times 2$ );
4. Stainless steel spacers ( $\times 2$ );
5. Plastic spacers ( $\times 2$ );
6. Contacting connectors ( $\times 2$ ).



# Preparation of wires

**! Use the gloves during the whole process of assembling !**

Set temperature of the soldering iron to 340°C



Cut 2x ~30 mm wires

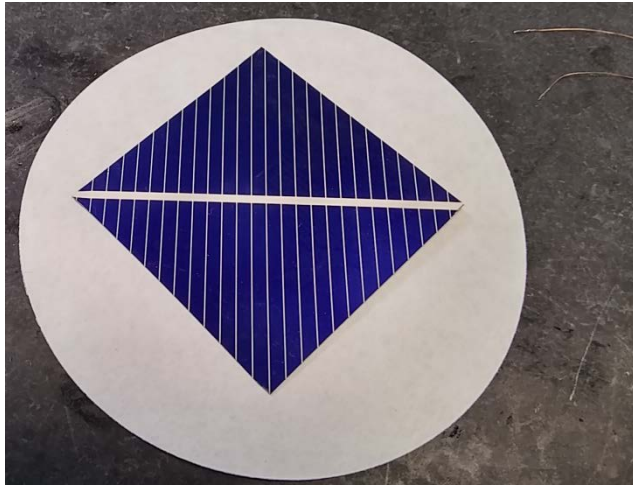


Solder both ends for each wire (2-3 mm long).

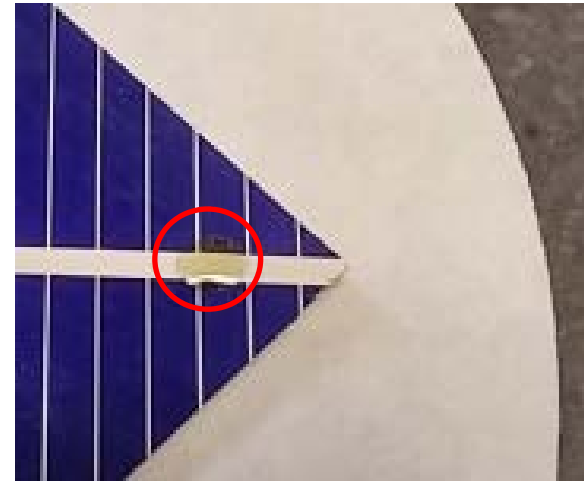


2-3 mm long

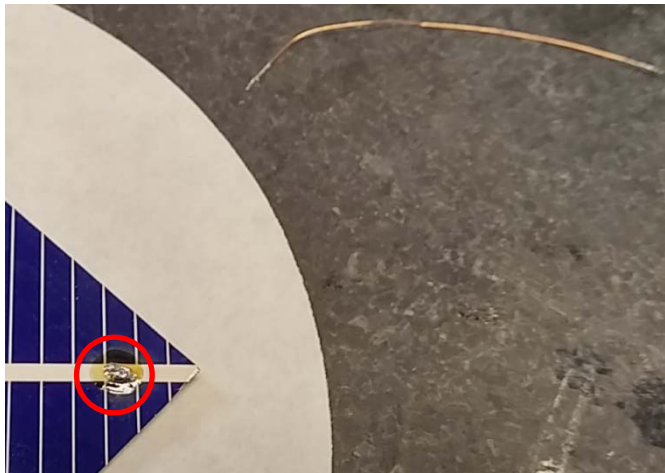
# Attach front contact to the test structure



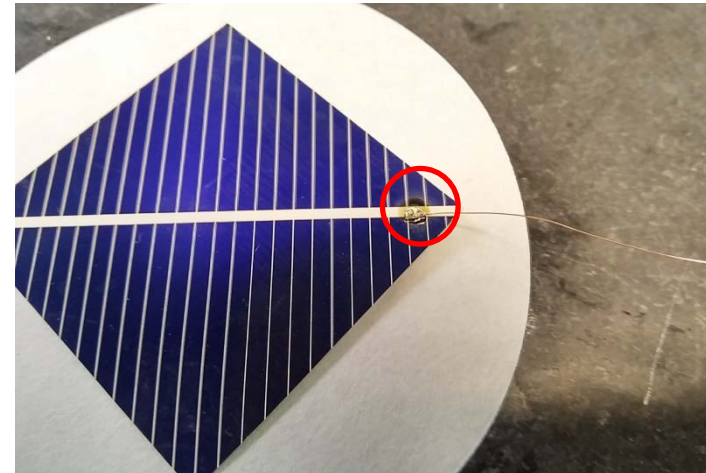
Place test structure on the stone plate.



Put a tiny drop of flux on the busbar.

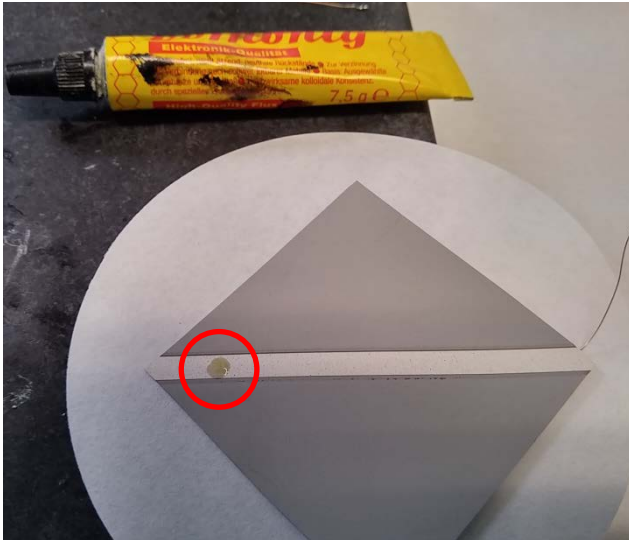


Attach soldering solution using the iron.

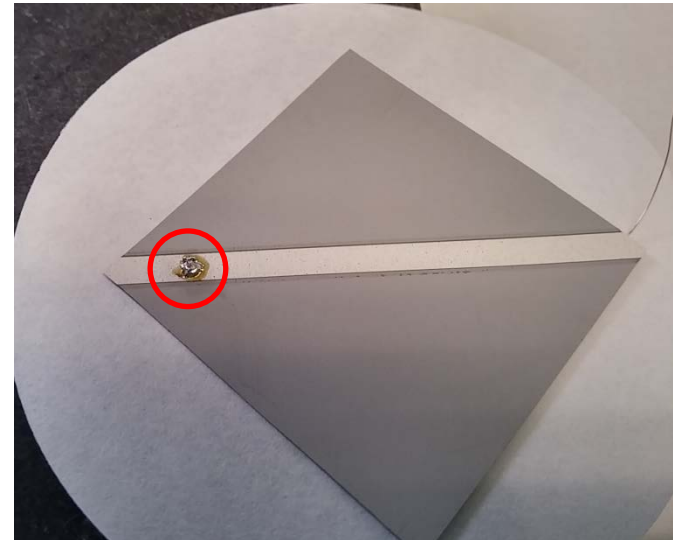


Attach wire using the soldering iron.

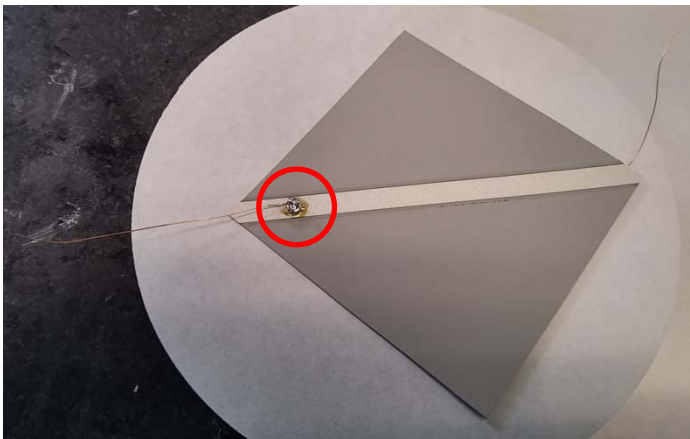
# Attach back contact to the test structure



Put a tiny drop of flux on the busbar.  
**! Keep the soldered front contact  
outside the stone plate !**



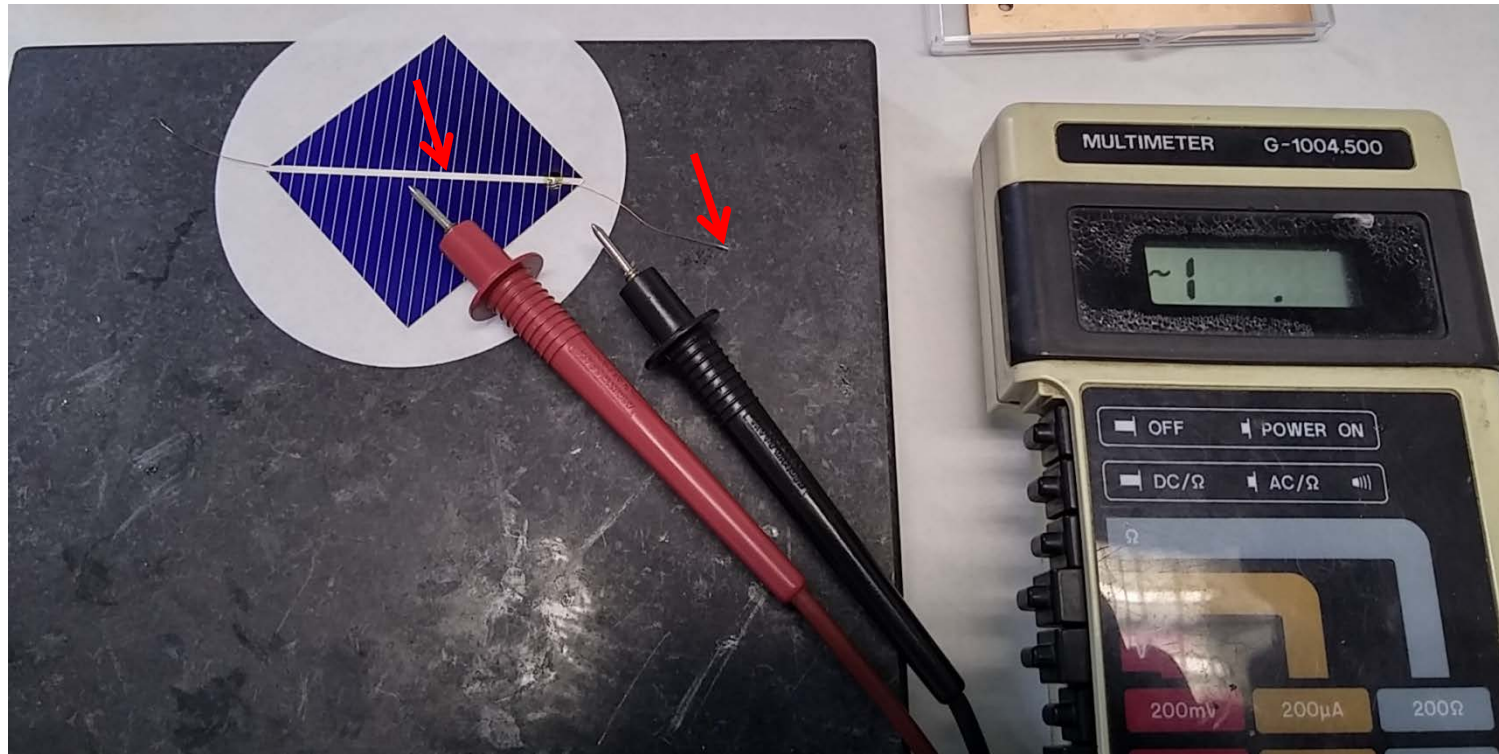
Attach soldering solution using the iron.



Attach the wire using the soldering iron.



# Check of the contacts using multimeter

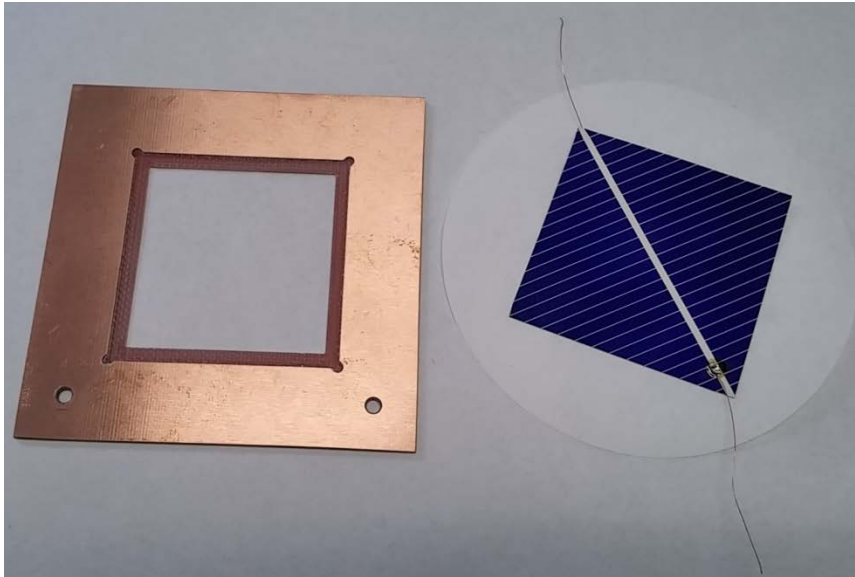


- Set multimeter to the “Short” checking mode;
- Check the contact quality for the front and for the back contacts by touching the busline and the end of the contacted wire.

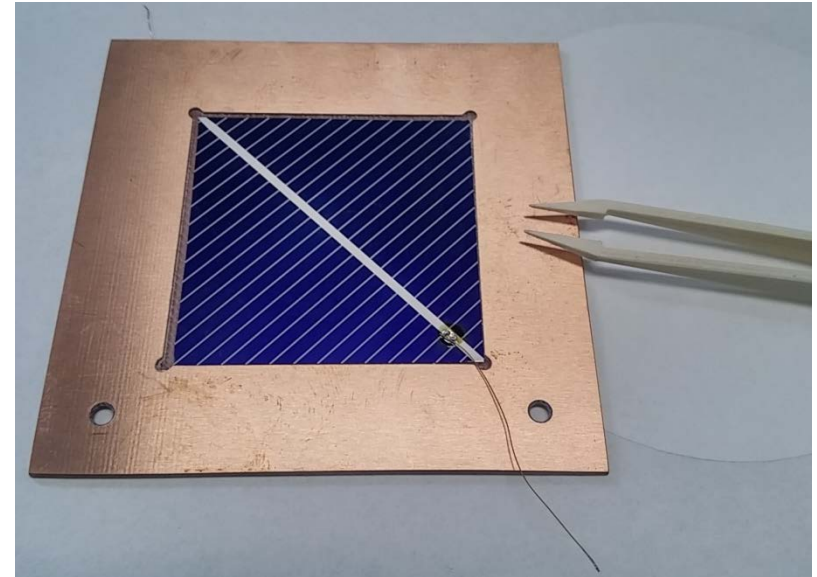




# Framing the test structure



Take the frame from the assembly kit.

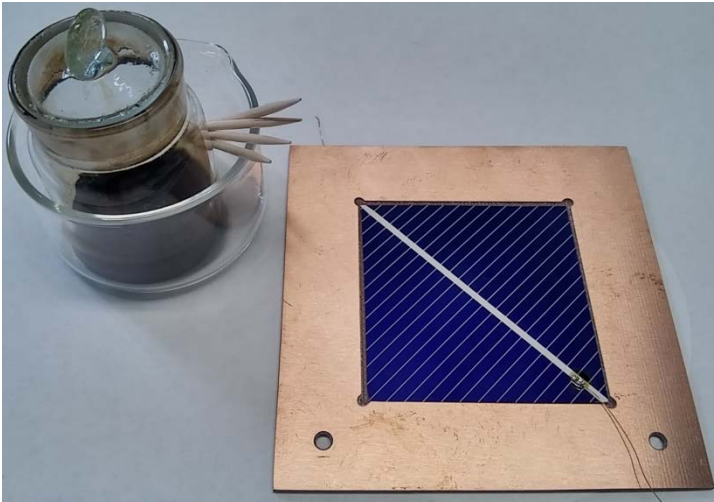


Carefully place the test structure inside the frame using the plastic tweezers.

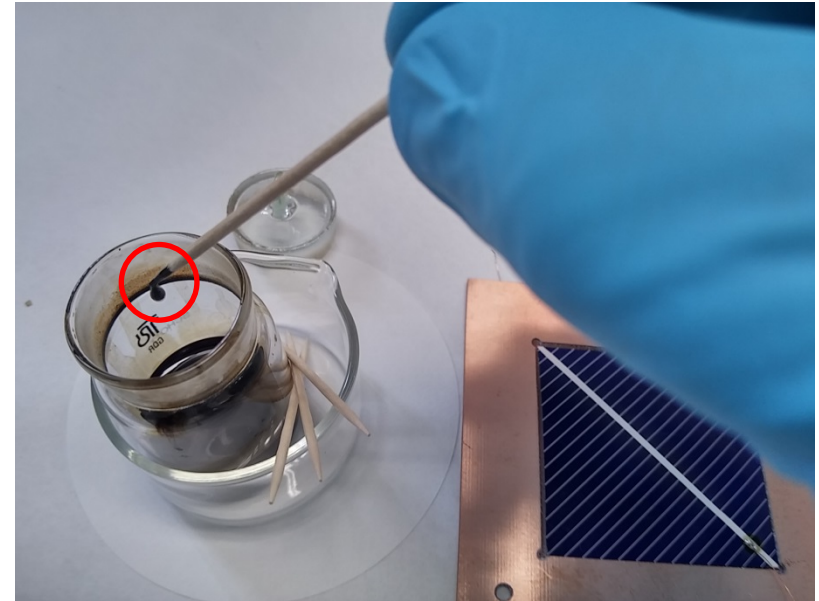
**! Keep the soldered wires out of the frame!**



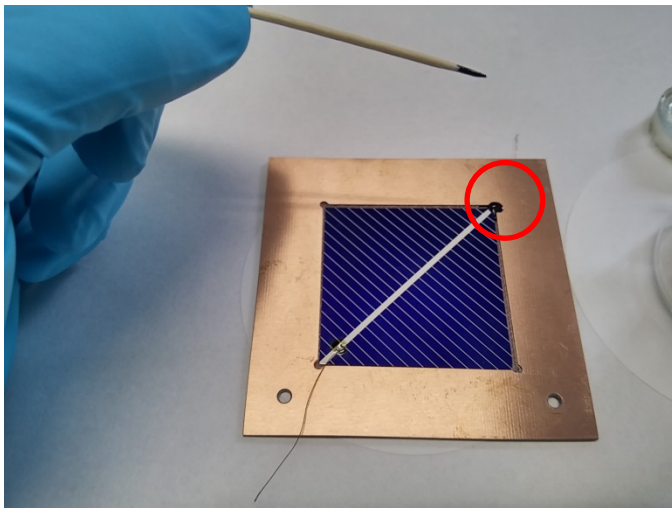
# Framing the test structure



Bring the varnish close to the sample.



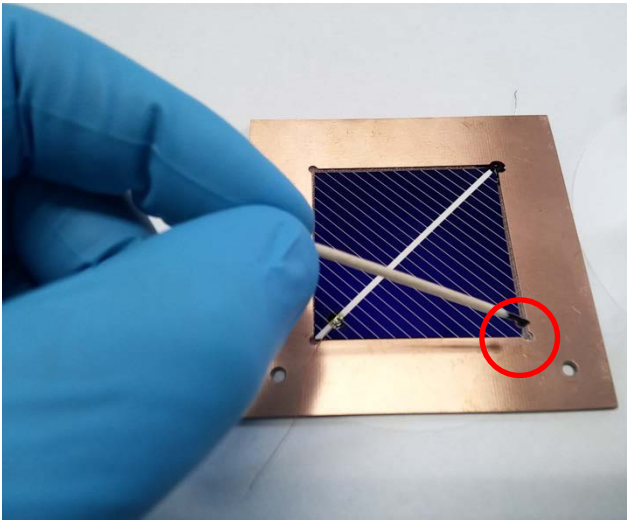
Take a small drop of the varnish using a toothpick.



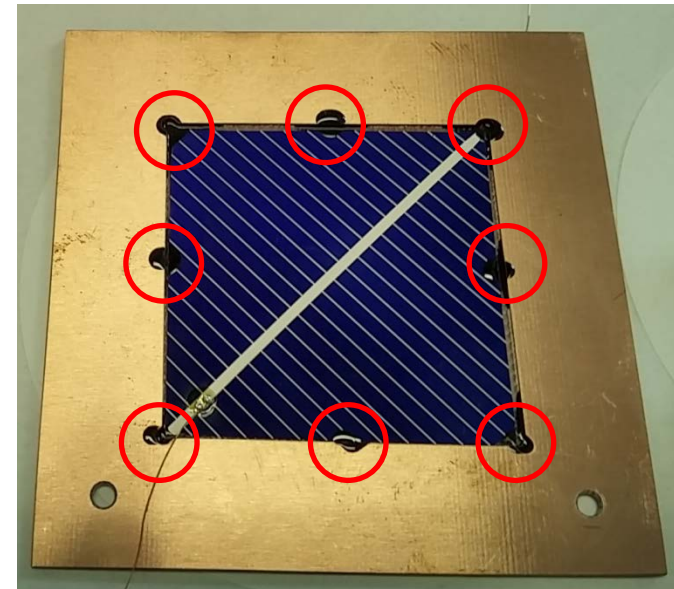
Place the drop in the corner of the frame on the top of the test structure and the frame.



# Framing the test structure



Repeat same with the second corner.



Repeat the same for the rest of the corners and for mid positions.

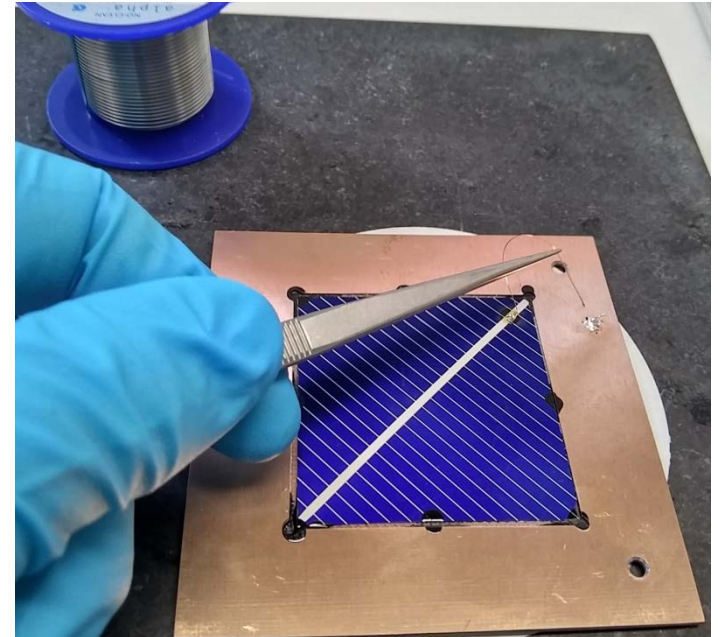
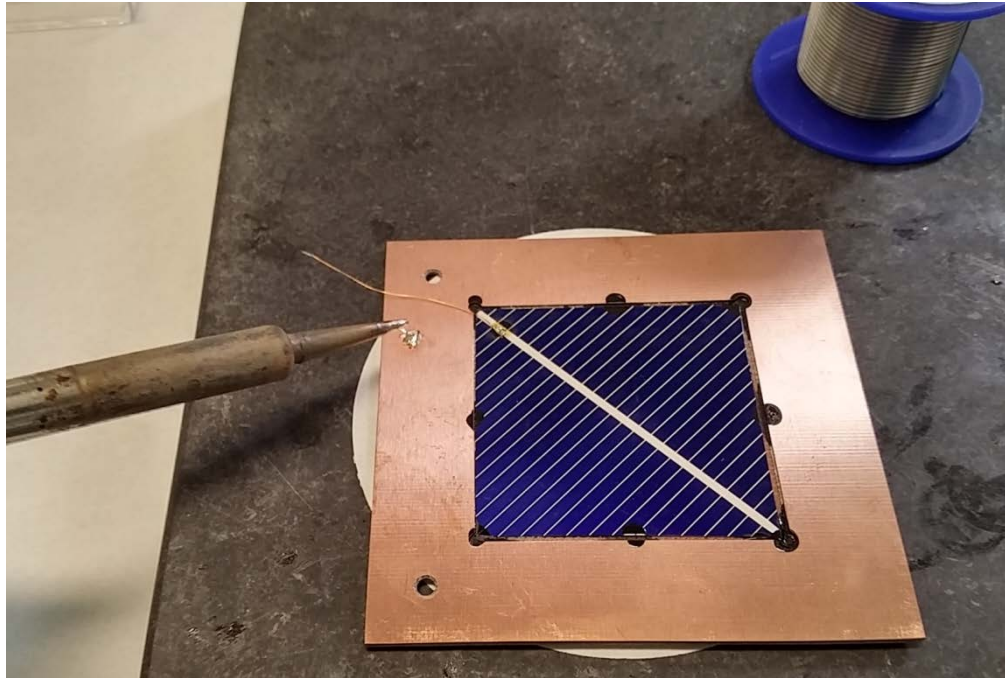
Wait 15-20 min for the varnish to dry.

**! Check if the test structure is well attached to the frame by flipping the frame !**

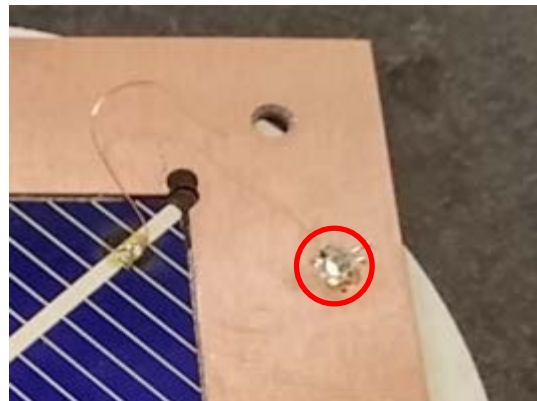


# Connecting the wires to the frame

Make a pad on the frame using the soldering iron.

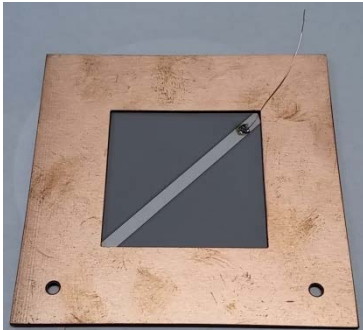


While holding the wire with the tweezers, attach it to the pad using the soldering iron.

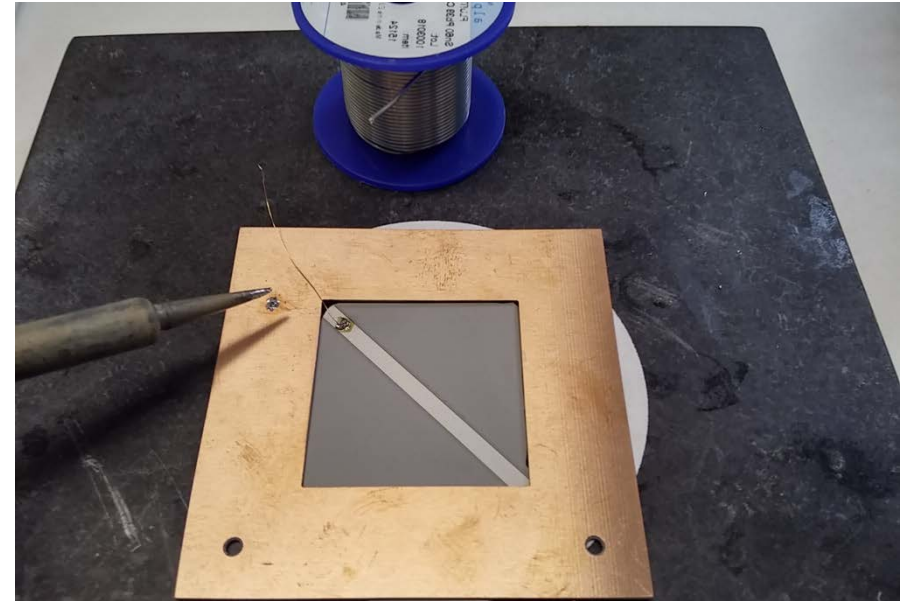




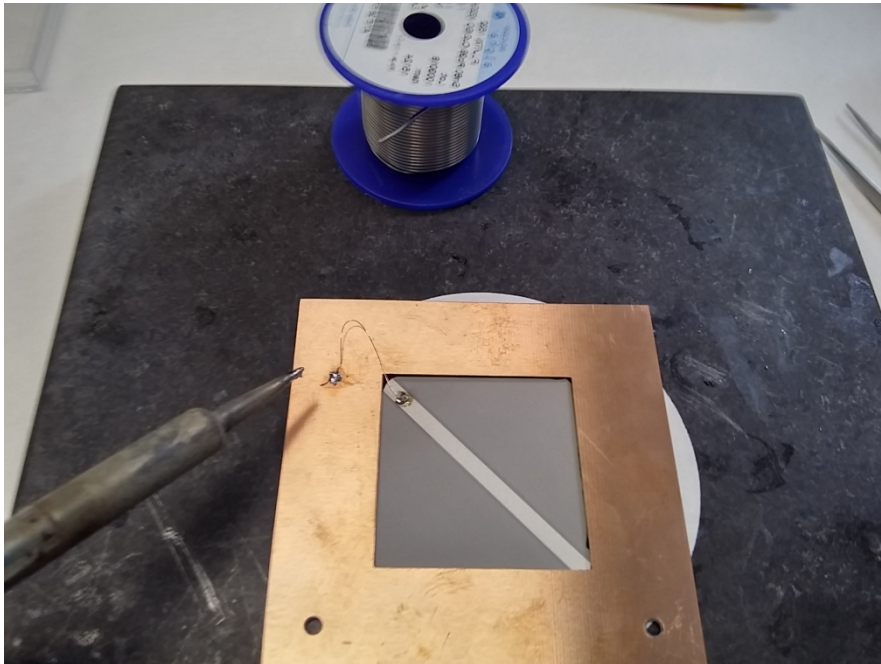
# Connecting the wires to the frame



Flip the frame.



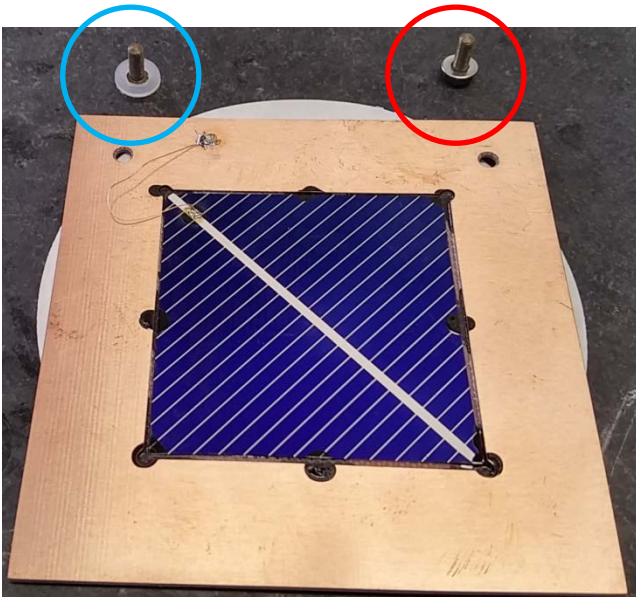
Make a pad on the frame using the soldering iron.



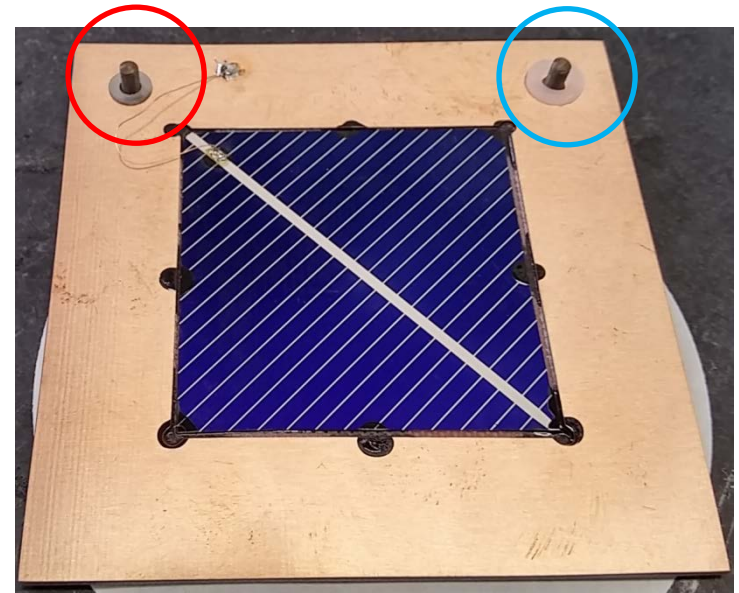
Attach the wire to the pad.



## Assembling the contacts



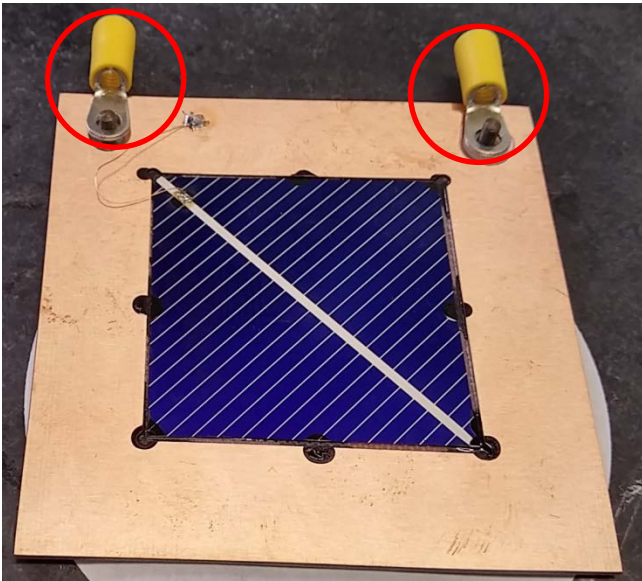
Face the structure up and prepare the screws with one **plastic** and another **metallic** spacers.



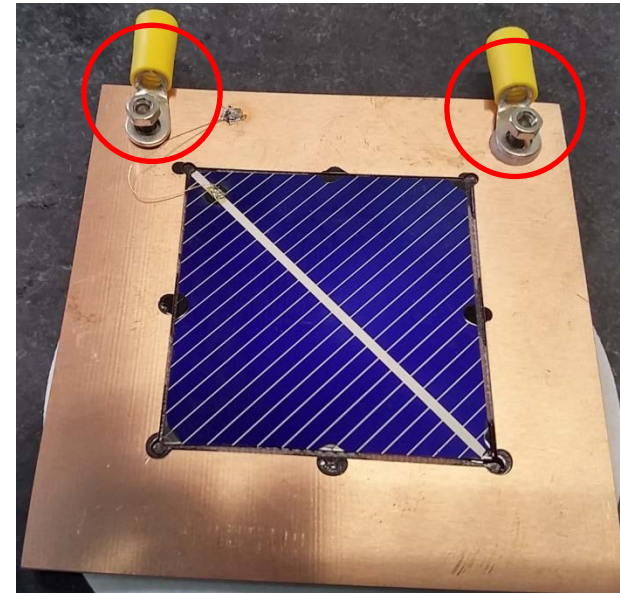
Pass the screws through the holes in the frame and put the rest spacers in opposite order: the **metallic** one for the screw with the first plastic spacer and the **plastic** for the first metallic spacer.



# Assembling the contacts



Pass the screws through the contacting connectors.



Attach the screw-nuts.

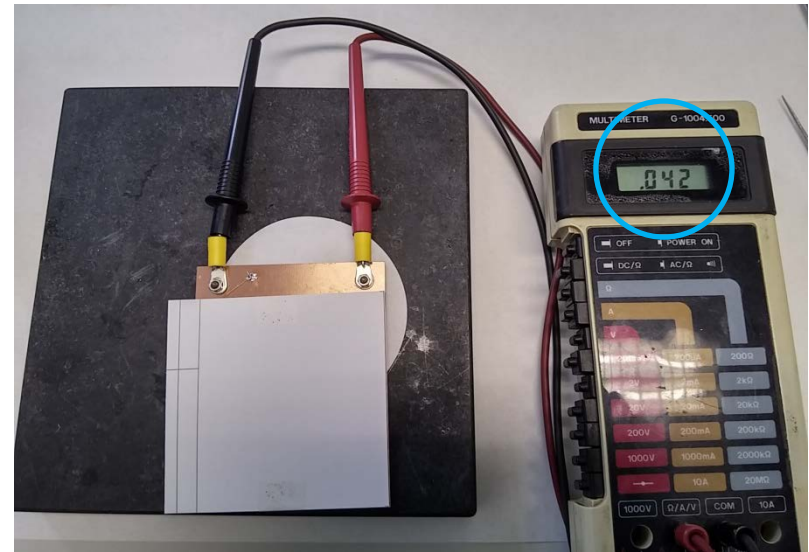
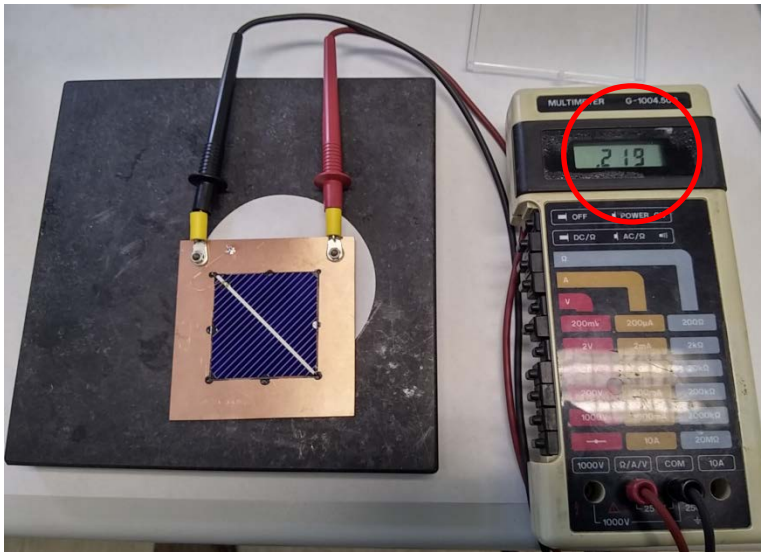


Tighten the connections using the tools.





# Check your test structure



Check your test structure by measuring the open circuit voltage ( $V_{OC}$ ) between the contacts. If the assembly was correct, the  $V_{OC}$  will be larger **under illumination** and it will be smaller if the cell is **covered with sheet**.



Place the structure inside the pocket from the kit and save it for the further test measurements.



# ფოტოვოლტაიკა

თეიმურაზ მჭედლიძე  
დრეზდენის ტექნიკური უნივერსიტეტი  
თებერვალი 2016

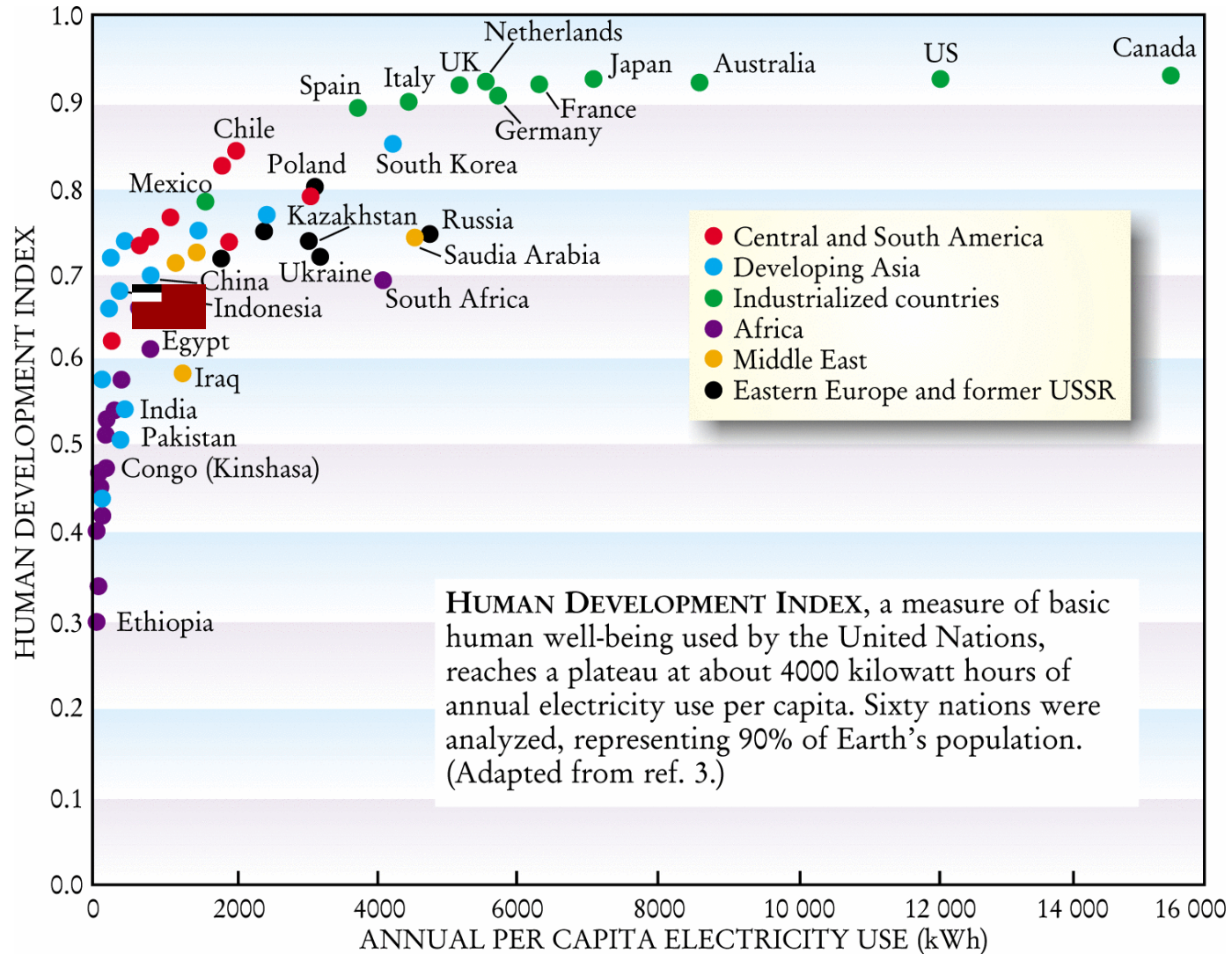
# ლექციების გეგმა

1. შესავალი;  
მზე როგორც ენერჯის წყარო.
2. მზის ენერჯის გარდაქმნა ელექტრობად  
ნახევარგამტარების საშუალებით.
3. ფოტოვოლტაიკური ელემენტები, მოდულები,  
ქსელები;
4. დასკვნები და მომავლის პერსპექტივა.

## ლექცია I: მზე როგორც ენერჯის წყარო

- შესავალი
- მზის გამოსხივების სიმძლავრე და სპექტრი;
- დედამიწამდე მოღწეული მზის გამოსხივების სიმძლავრე;
- სეზონური და დღე-ღამური ცვლილებები;
- პირდაპირი და დიფუზიური გამოსხივება;
- ინსოლიაცია და ინსოლიაციის რუქები;
- მარტივი შეფასებები.

# Human development index (HDI)



# Photovoltaic

- Economy, ecology, philosophy, design, architecture.

- Sun studies, meteorology, landscape studies.

- Research & development:

- Materials studies
- Solar cell structure
- Module, network, grid
- Energy storage
- Space solar

Characterization and monitoring.

- Production:

- Materials
- Solar cell
- Modules
- Components

- Solar system utilization:

- Installation
- Maintenance
- Disposal

Planck's radiation law:

$$F(\lambda) = \frac{2\pi hc^2}{\lambda^5 \left( \exp\left(\frac{hc}{k\lambda T}\right) - 1 \right)}$$

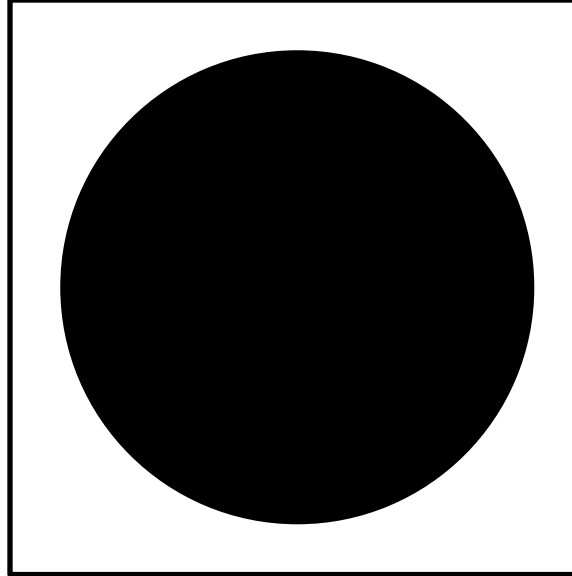
where:

$\lambda$  is the wavelength of light;

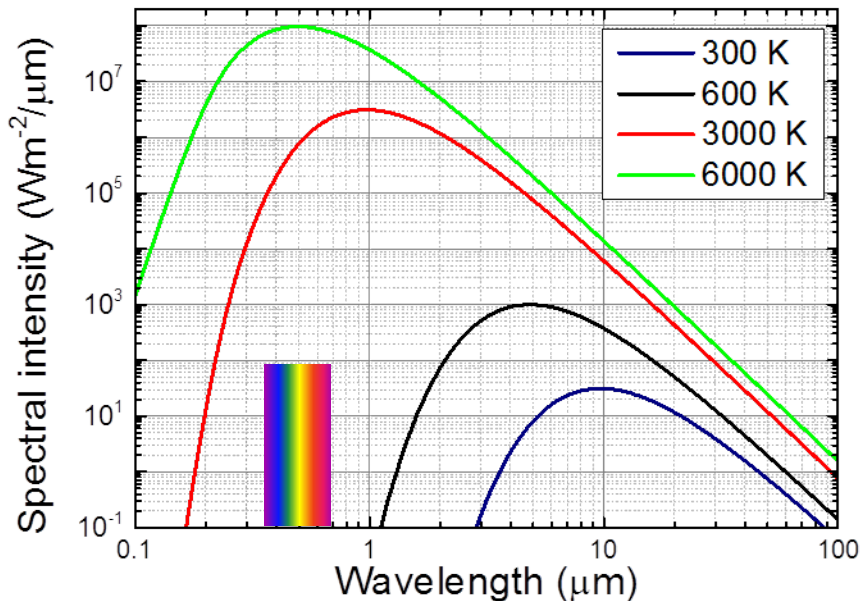
$T$  is the temperature of the blackbody (K);

$F$  is the spectral irradiance in  $\text{Wm}^{-2}\mu\text{m}^{-1}$ ;

And  $h$ ,  $c$  and  $k$  are constants



A blackbody absorbs all radiation incident on its surface and emits radiation based on its temperature.



The total power density from a blackbody is determined by integrating the spectral irradiance over all wavelengths which gives:

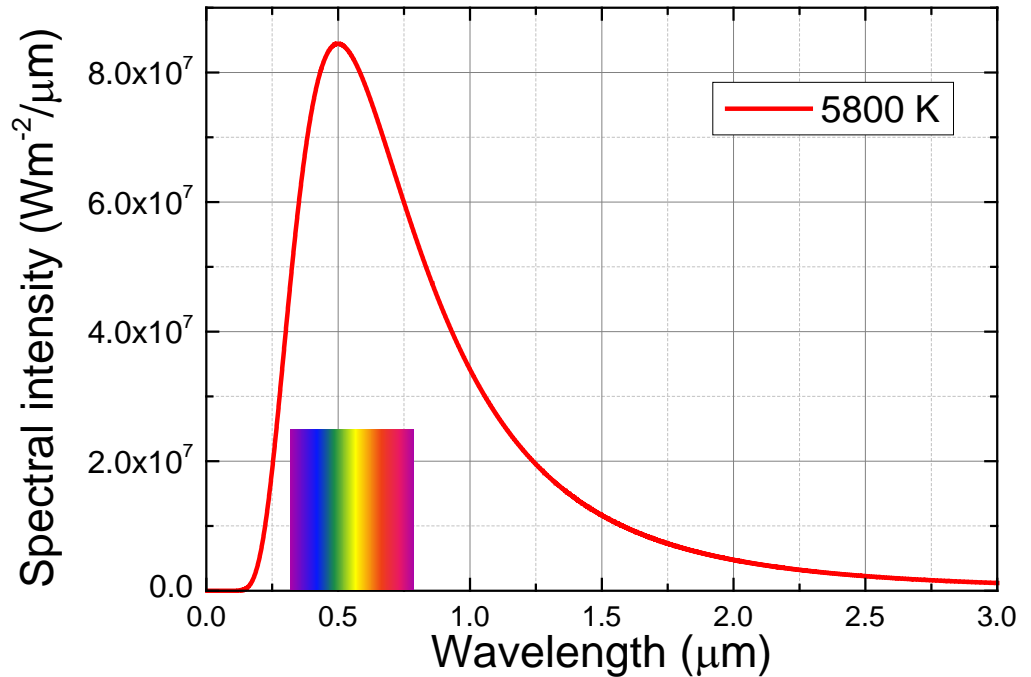
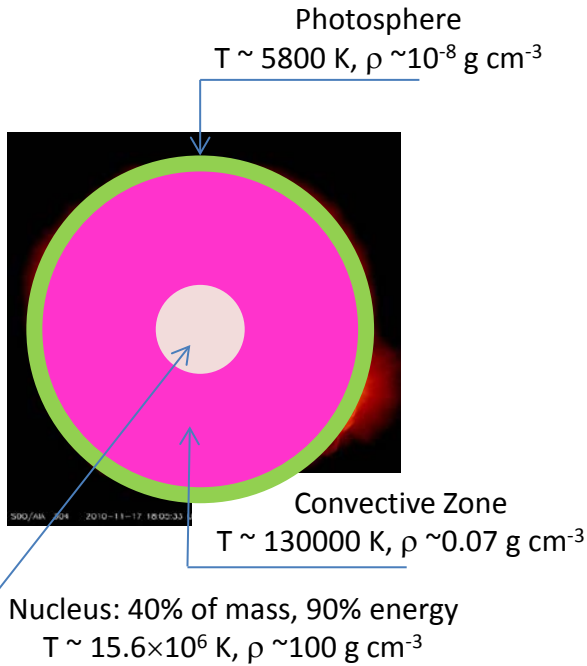
$$H = \sigma T^4$$

where  $\sigma = 5.67 \times 10^{-8} \text{ J/m}^2\text{s K}^4$  is the Stefan-Boltzmann constant and  $T$  is the temperature of the blackbody in Kelvin.

The wavelength where most of the power is emitted, the peak wavelength of the spectral irradiance can be obtained from Wien's Law:

$$\lambda_p(\mu\text{m}) = 2900/T$$

# Energy coming from the sun



For  $T=5800 \text{ K}$  we will get

$$\lambda_p = 0.5 \mu\text{m}$$

$$H_{SUN} \approx 6.42 \times 10^7 \text{ W/m}^2$$

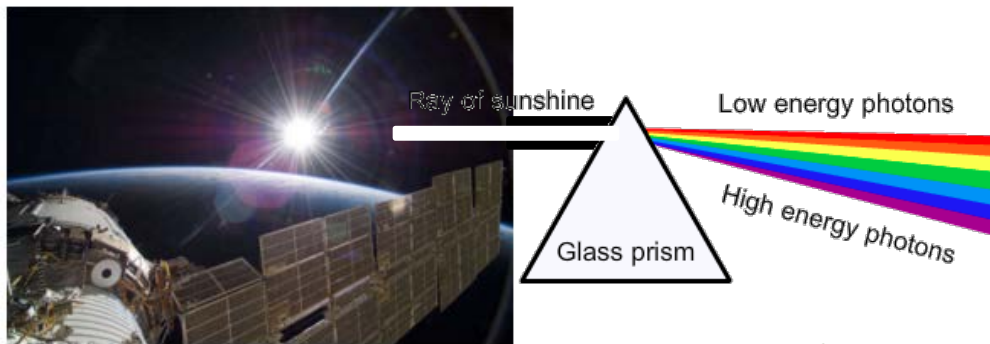
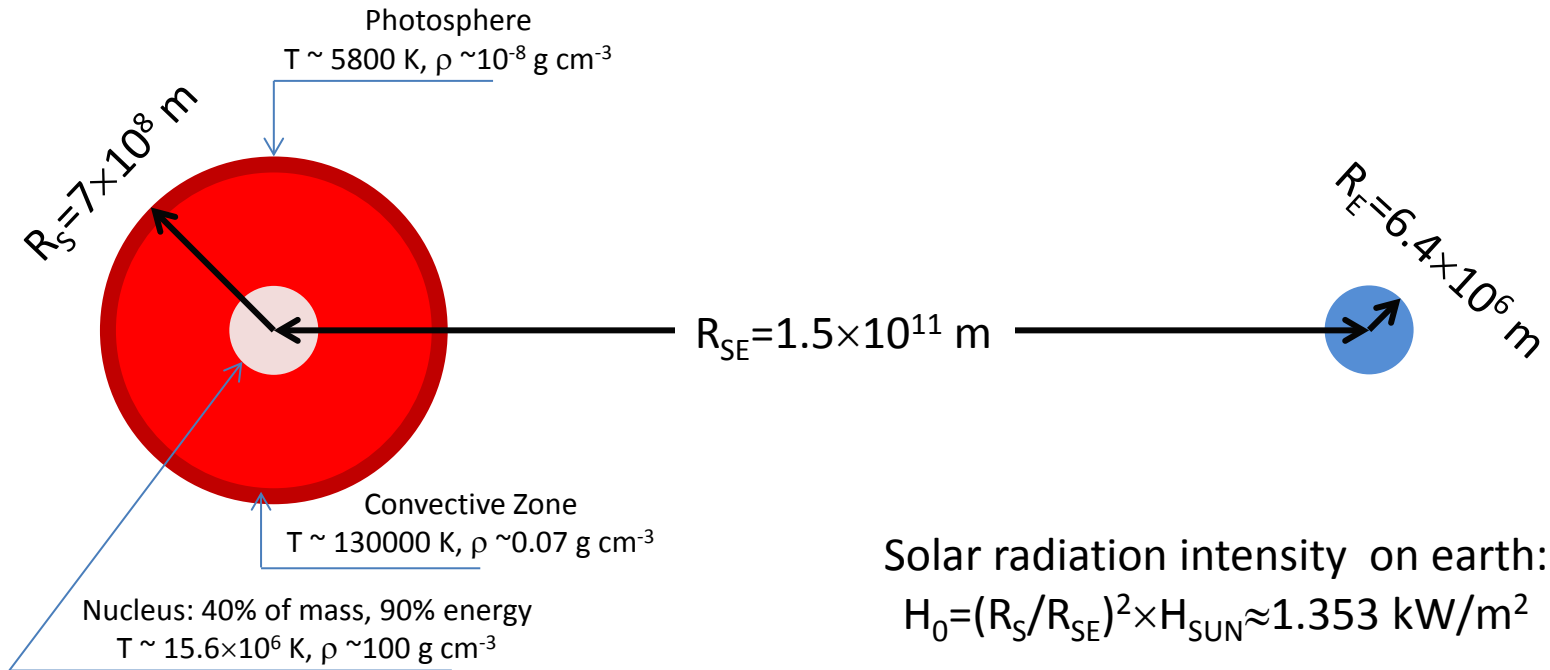


Image courtesy NASA

# Energy coming from the sun



Solar radiation intensity on earth:

$$H_0 = (R_S/R_{SE})^2 \times H_{SUN} \approx 1.353 \text{ kW/m}^2$$

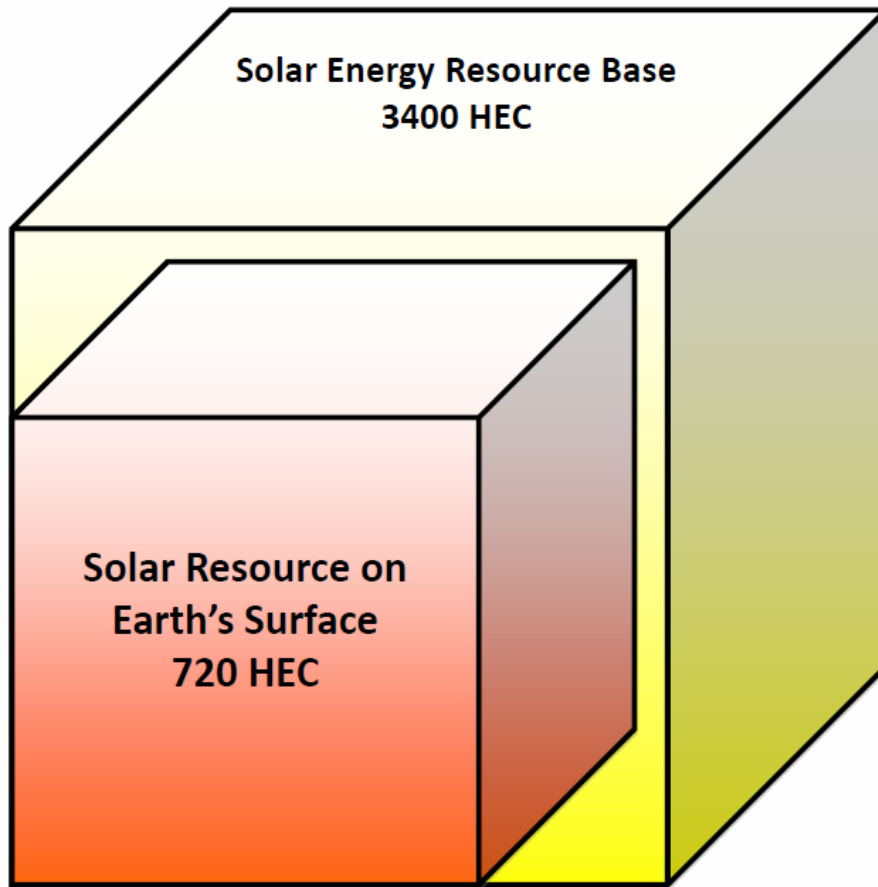
The value of the solar constant and its spectrum are fixed by ASTM as a standard value called "air mass zero" or **AM0**

Total Power emitted by the sun

$$P_{SUN} = H_{SUN} \times A_{SUN} = 9.5 \times 10^{25} \text{ W}$$



# Solar resource



In units of HEC  
(human energy  
consumption)



Wind Energy  
Resource Base  
1.4 HEC



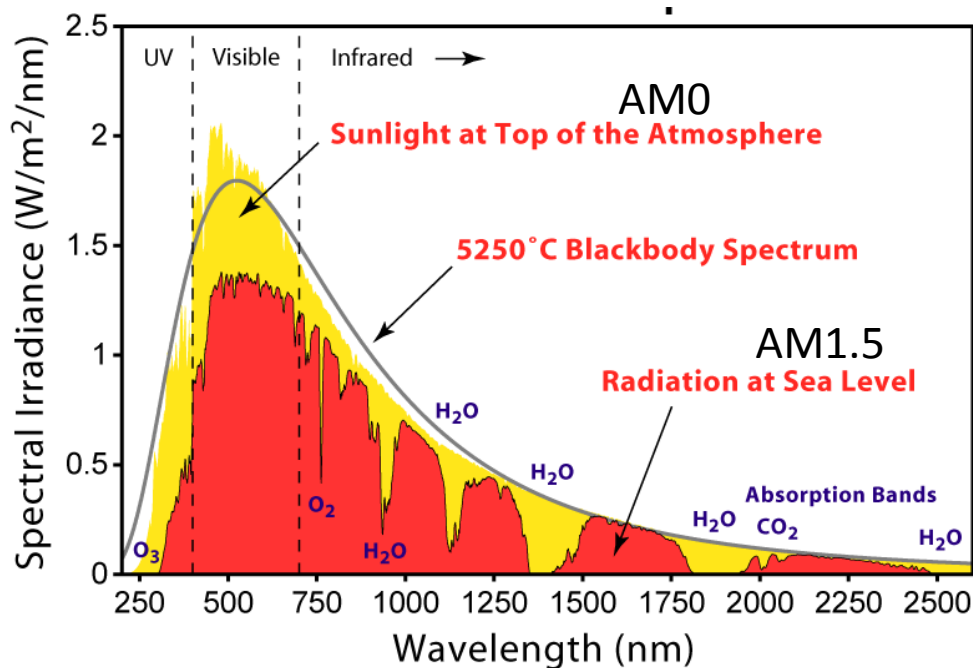
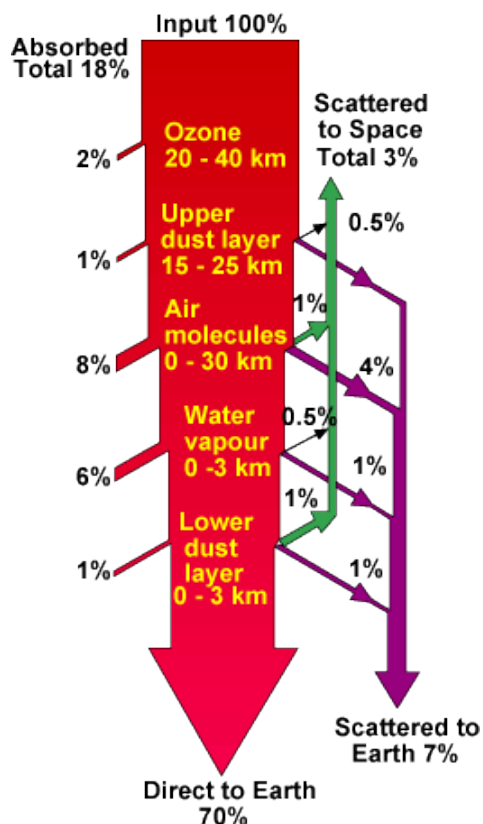
Human Energy Use  
(mid- to late-century)  
1 HEC

## References:

Wind Energy: C.L. Archer and M.Z. Jacobson, *J. Geophys. Res.* **110**, D12110 (2005).

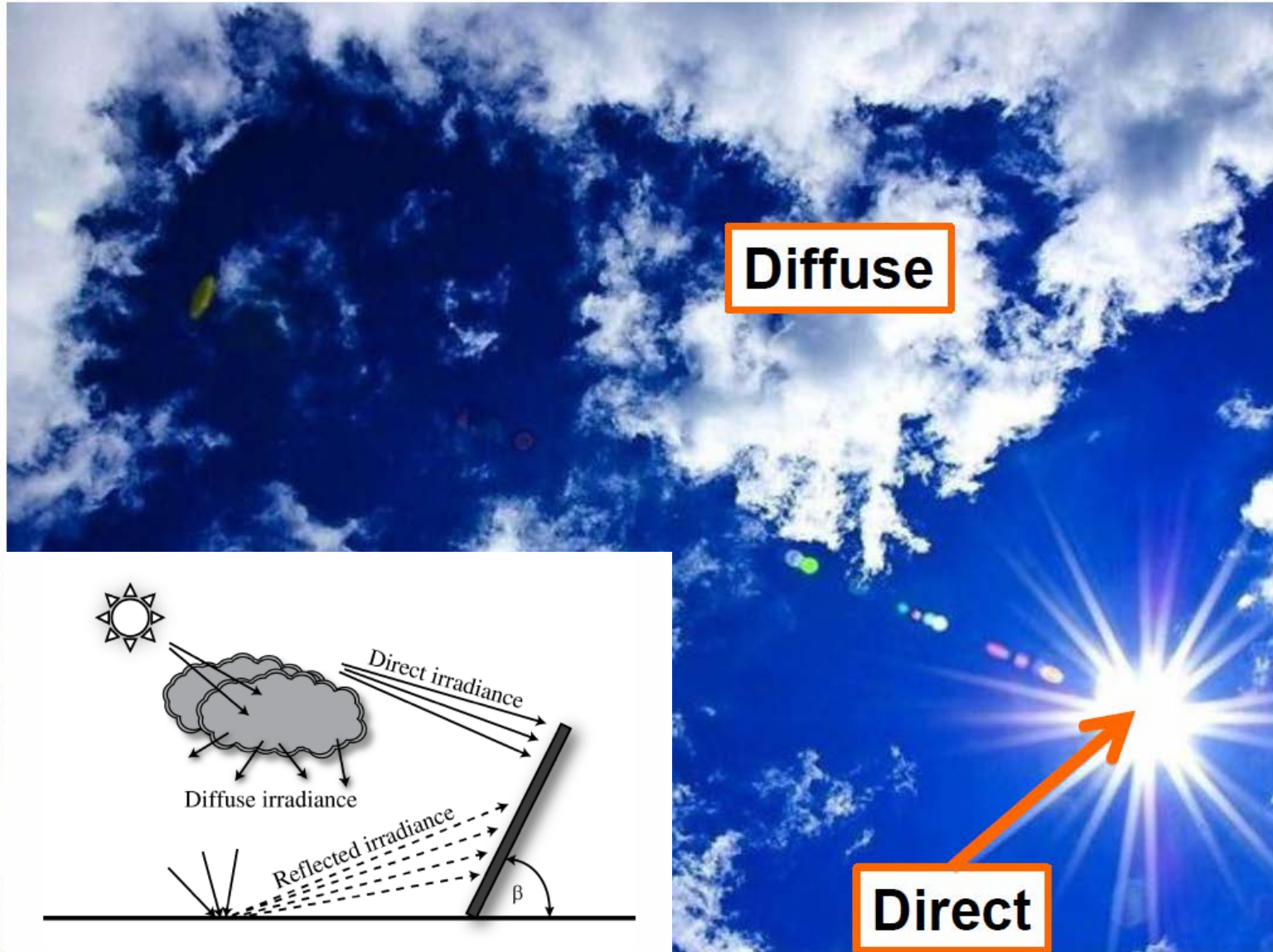
# Sun energy on the earth

- Seasonal variations due to elliptic orbit:  $H=H_0(1+0.033\cos(360(n-2)/365))$
- Time of the day + Latitude of the location.



- Atmospheric effects, including absorption and scattering;
- Local variations in the atmosphere, such as water vapor, clouds, and pollution.

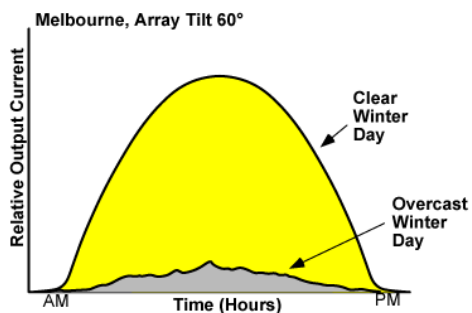
# Direct, reflected and diffuse solar radiation



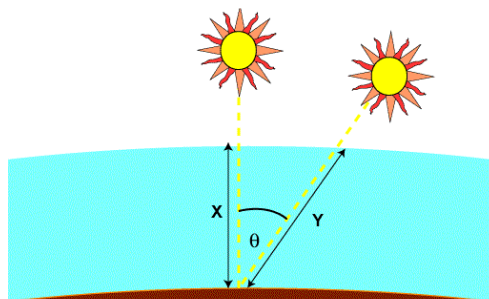
# Solar spectra calculators

- Direct irradiation: from sun
- Diffuse Irradiation: sun irradiation scattered from particles in atmosphere (up to 10%, blue)
  - Rayleigh scattering ( $\lambda^{-4}$ )
  - Mie scattering

- Effect of clouds:



- Air mass:  $AM = \cos^{-1}(\Theta)$



**SOLAR SPECTRUM CALCULATOR**
RESTORE
EXPORT

Calculator

Options

Upload spectrum

About

RELATED LINKS

ASTM standard spectra

Fraunhofer ISE CalLab spectrum

IEC standard spectra

NREL: reference spectra

PV Education: Sunlight

SMARTS

Spectral mismatch calculator

Spectrum Library

**INPUTS**

**Date and sidereal time:**

Year  Hour

Month  Minute

Day  Second

**Module location:**

Latitude  °

Longitude  °

**Module orientation:**

Tilt angle  °

Azimuth angle  °

**Extraterrestrial spectrum:**

Incident spectrum

Earth-Sun factor

**Atmospheric inputs:**

Transmission model

Atmospheric pressure  mb

Turbidity at 500 nm

Precipitable water vapour  cm

Ozone  atm-cm

Albedo

**OUTPUTS**

**Insolation**

**Solar position**

Air mass

Zenith angle  °

Azimuth angle  °

Incident angle  °

	Power density (W/m <sup>2</sup> )		Photon current (mA/cm <sup>2</sup> )	
	perpendicular	module	perpendicular	module
Direct	853.4	422.5	61.04	30.22
Diffuse	82.3	78.0	4.15	3.63
Global	935.7	500.5	65.19	33.85

Integrated over the wavelength range 280–4000 nm

**Graph**

Plot

incident to

against

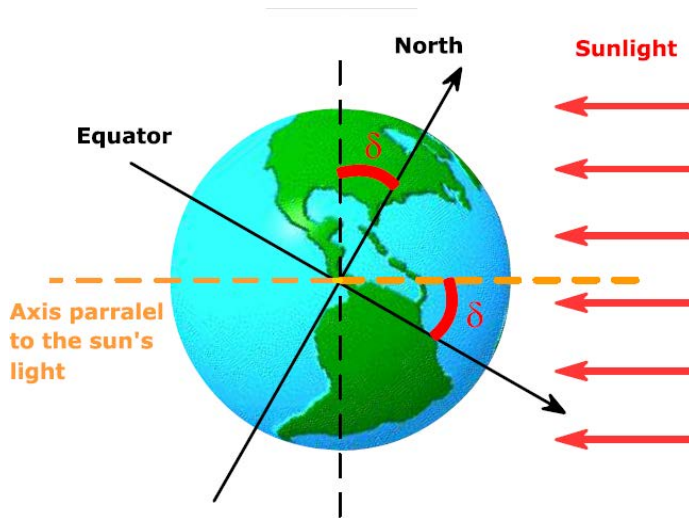
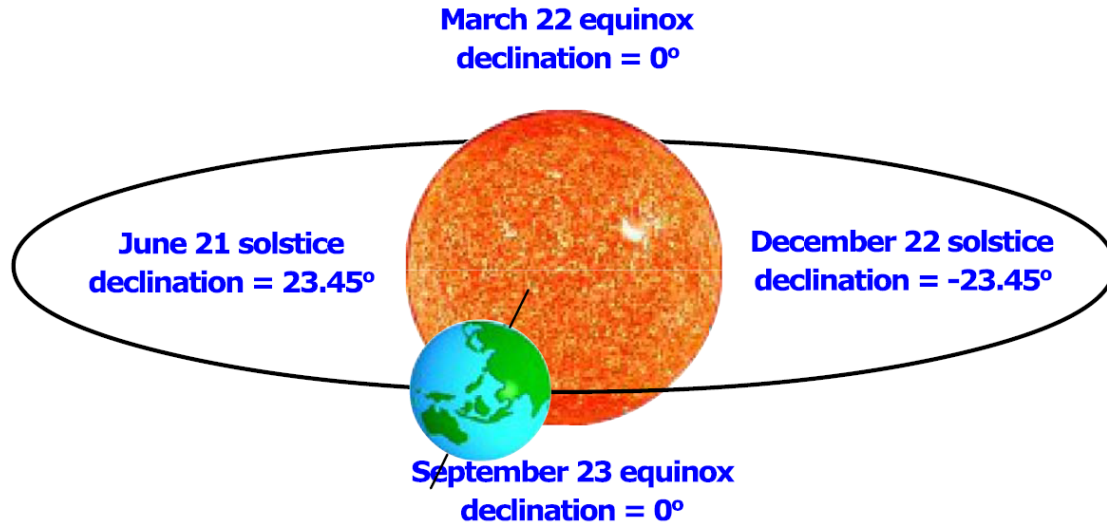
Extraterrestrial  
 Direct  
 Diffuse  
 Global

Spectral irradiance vs wavelength incident to module

Computation time: 0.000 s.

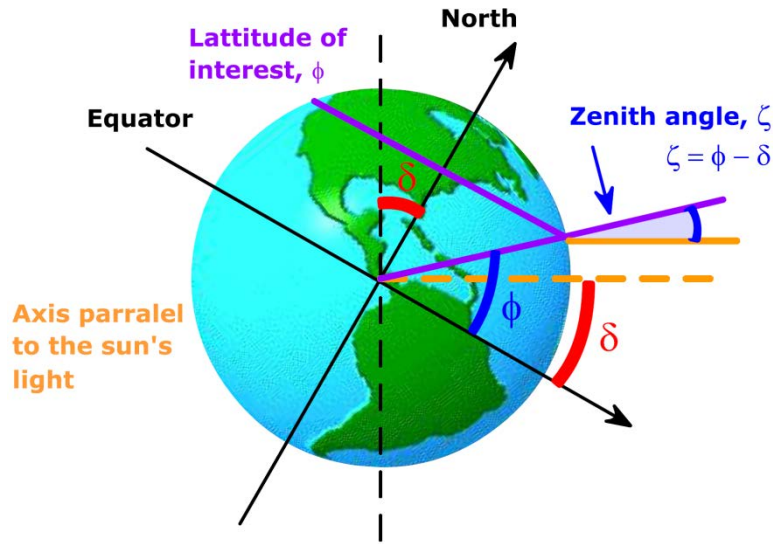
<https://www.pvlighthouse.com.au/calculators/>  
<http://www.pveducation.org/>

# Motion of the earth



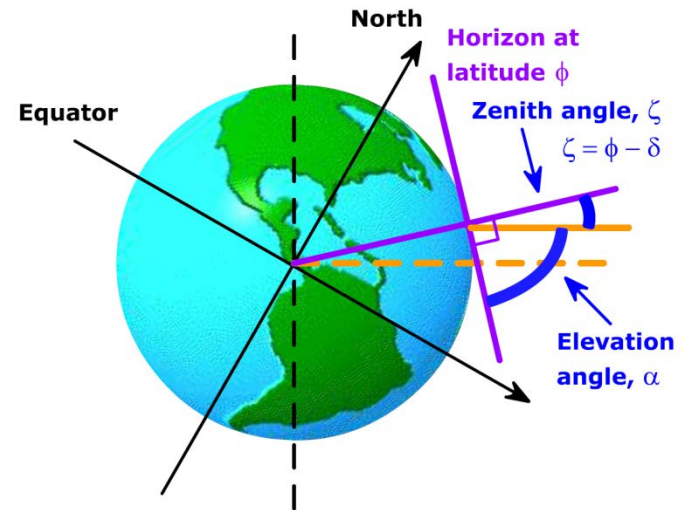
The tilt of the earth compared to the sun, the declination angle  $\delta$ , depends on the season. The maximum angle occurs at summer solstice in northern hemisphere and at winter solstice in southern hemisphere

# More angles



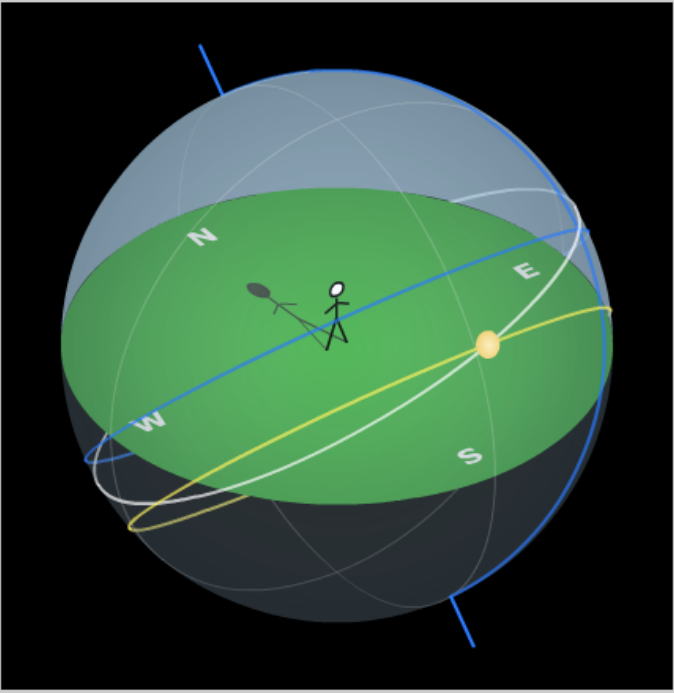
The zenith angle,  $\zeta$ , at solar noon is defined as the angle between the incident sunlight and the particular location and is given by  $(\phi - \delta)$ .

The elevation or altitude angle,  $\alpha$ , is defined from the horizontal plane and is given by  $90^\circ$ -zenith angle, or  $90^\circ - (\phi - \delta)$ .



# Motions by the sun simulator

Motions of the Sun Simulator reset help about




### Time and Location Controls

the day of year:

| Jan | Feb | Mar | Apr | May | Jun | Jul | Aug | Sep | Oct | Nov | Dec |

the time of day:

the observer's latitude:



### Information

The horizon diagram is shown for an observer at latitude 44.0° N on 1 February at 12:00 (12:00 PM).

<p><i>advanced</i></p> <p>sun's hour angle: -0h 13m</p> <p>sidereal time: 20h 48m</p> <p>equation of time: -13:38</p> <p><input type="checkbox"/> show analemma</p>	<p>sun's altitude: 29.0°</p> <p>sun's azimuth: 176.3°</p> <p>sun's right ascension: 21h 1m</p> <p>sun's declination: -16.9°</p>
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### Animation Controls

animation mode:

continuous  loop day

step by day

animation speed: 3.0 hrs/sec

slower faster

use lower quality graphics when animating to improve performance

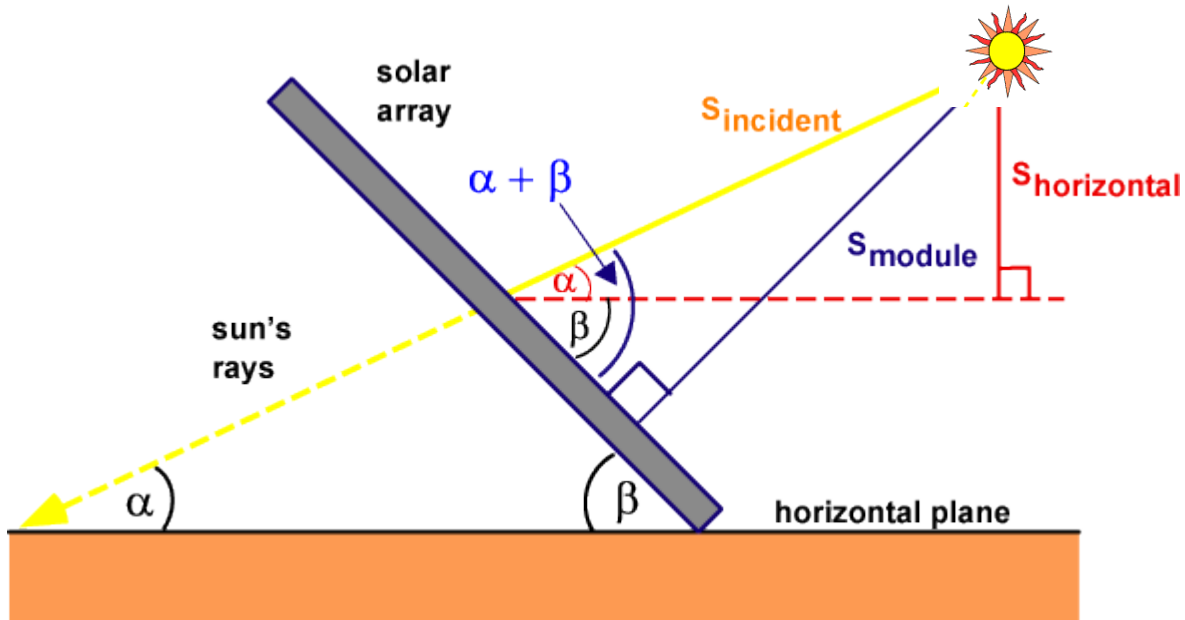
### General Settings

- show the sun's declination circle
- show the ecliptic
- show month labels
- show underside of celestial sphere
- show stickfigure and its shadow

dragging the sun's disk changes the ...

- time of day
- day of year

## Solar radiation on a tilted surface



Power density,  $S_{\text{incident}}$  on a PV module with tilt angle  $\beta$ :

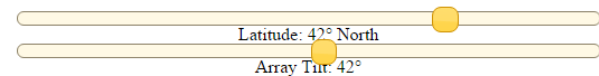
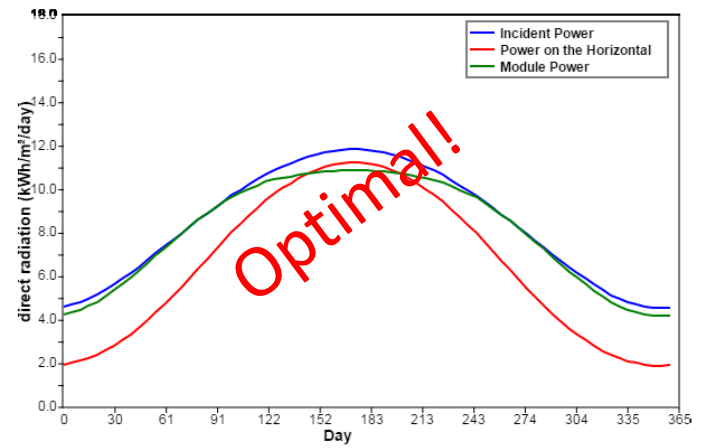
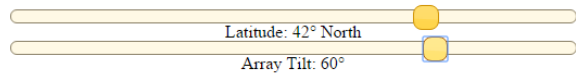
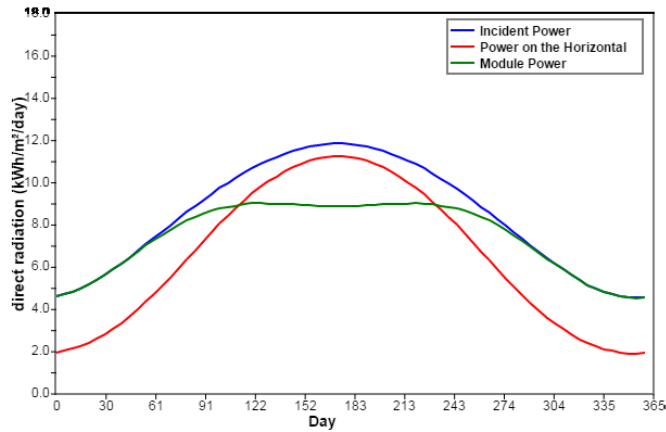
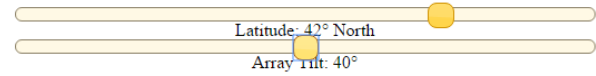
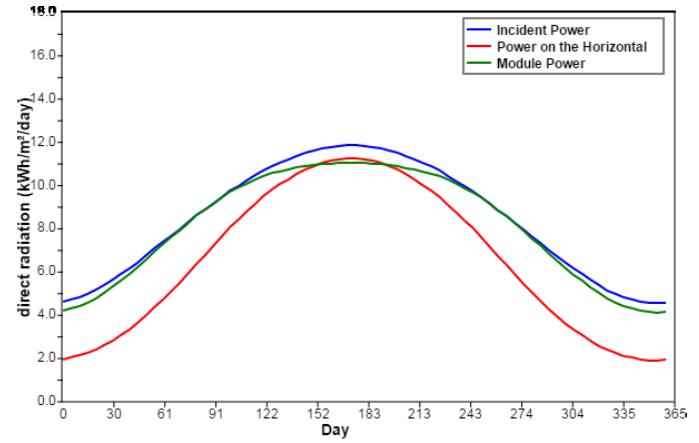
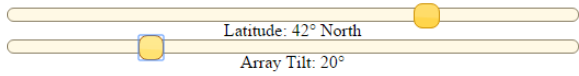
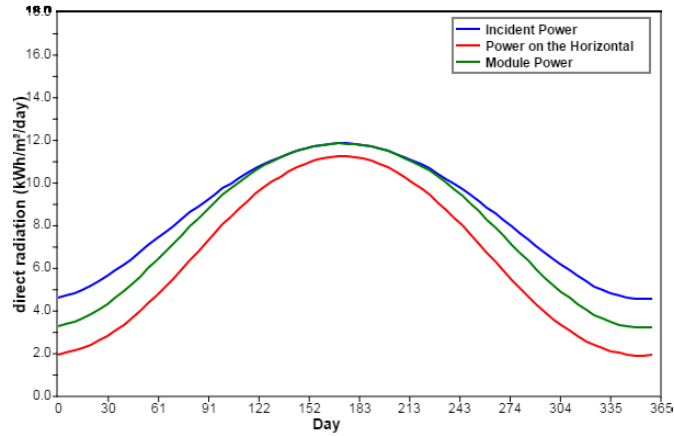
$$S_{\text{module}} = S_{\text{horizontal}} \sin(\alpha + \beta) / \sin \alpha$$

The elevation angle:  $\alpha = 90^\circ - \Phi \pm \delta$  with  $\Phi$  : latitude;  $\delta$ : declination

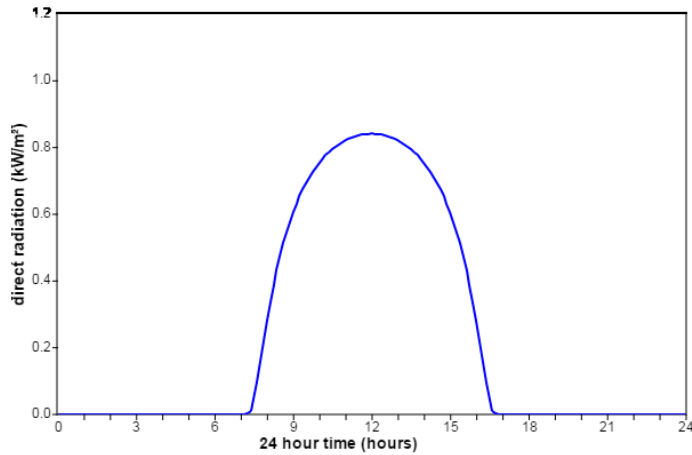
$\delta$  depends on the day of year, best tilt angle  $\beta = \Phi$



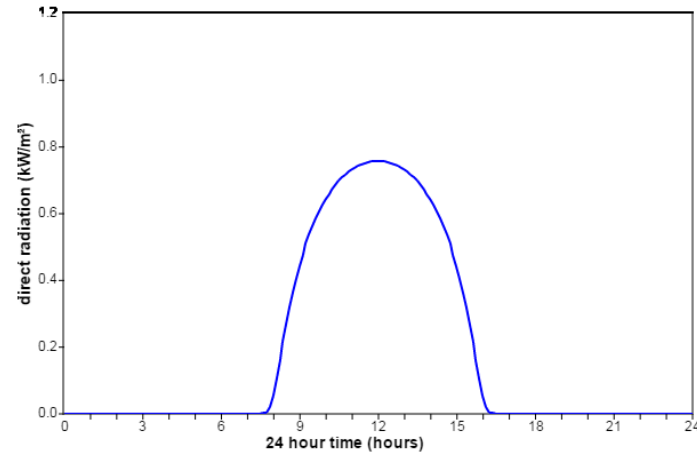
# Module power over the year



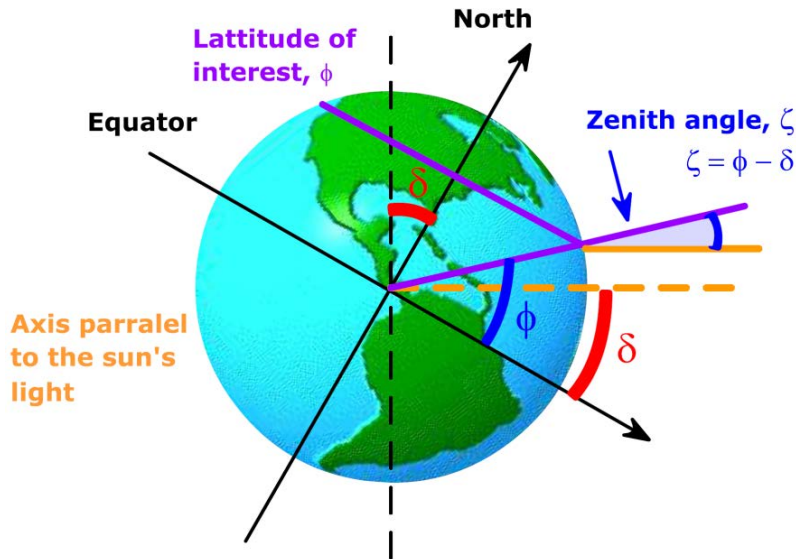
# Calculation of Solar Insolation



Sunrise: 7:6 Sunset: 16:53  
 Latitude: 42° North  
 Day: 32 (Feb 1)



Sunrise: 7:31 Sunset: 16:28  
 Latitude: 42° North  
 Day: 357 (Dec 23)



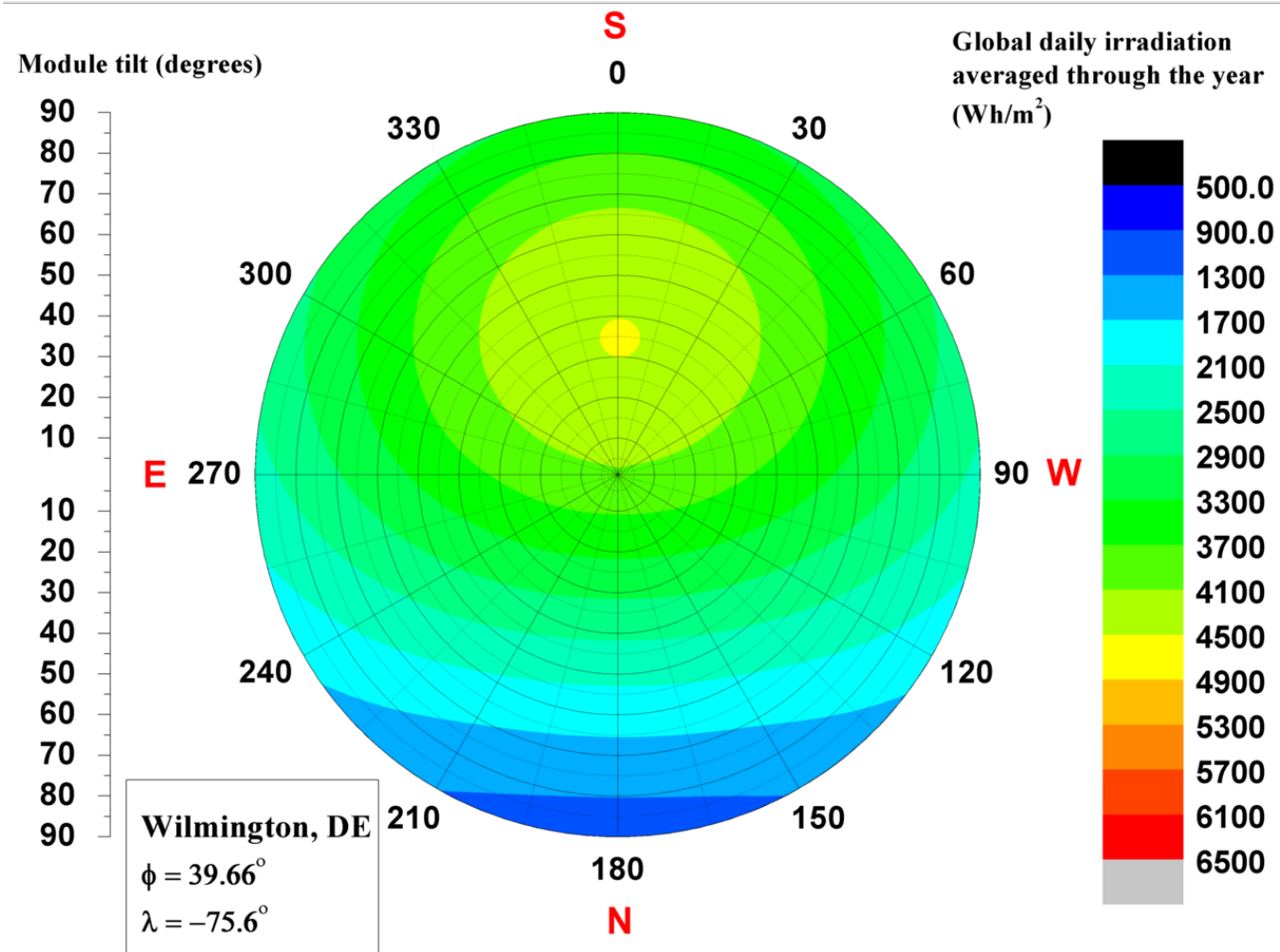
$$\text{Sunrise} = 12 - \frac{1}{15^0} \cos^{-1} \left( \frac{-\sin \phi \sin \delta}{\cos \phi \cos \delta} \right)$$

$$\text{Sunset} = 12 + \frac{1}{15^0} \cos^{-1} \left( \frac{-\sin \phi \sin \delta}{\cos \phi \cos \delta} \right)$$

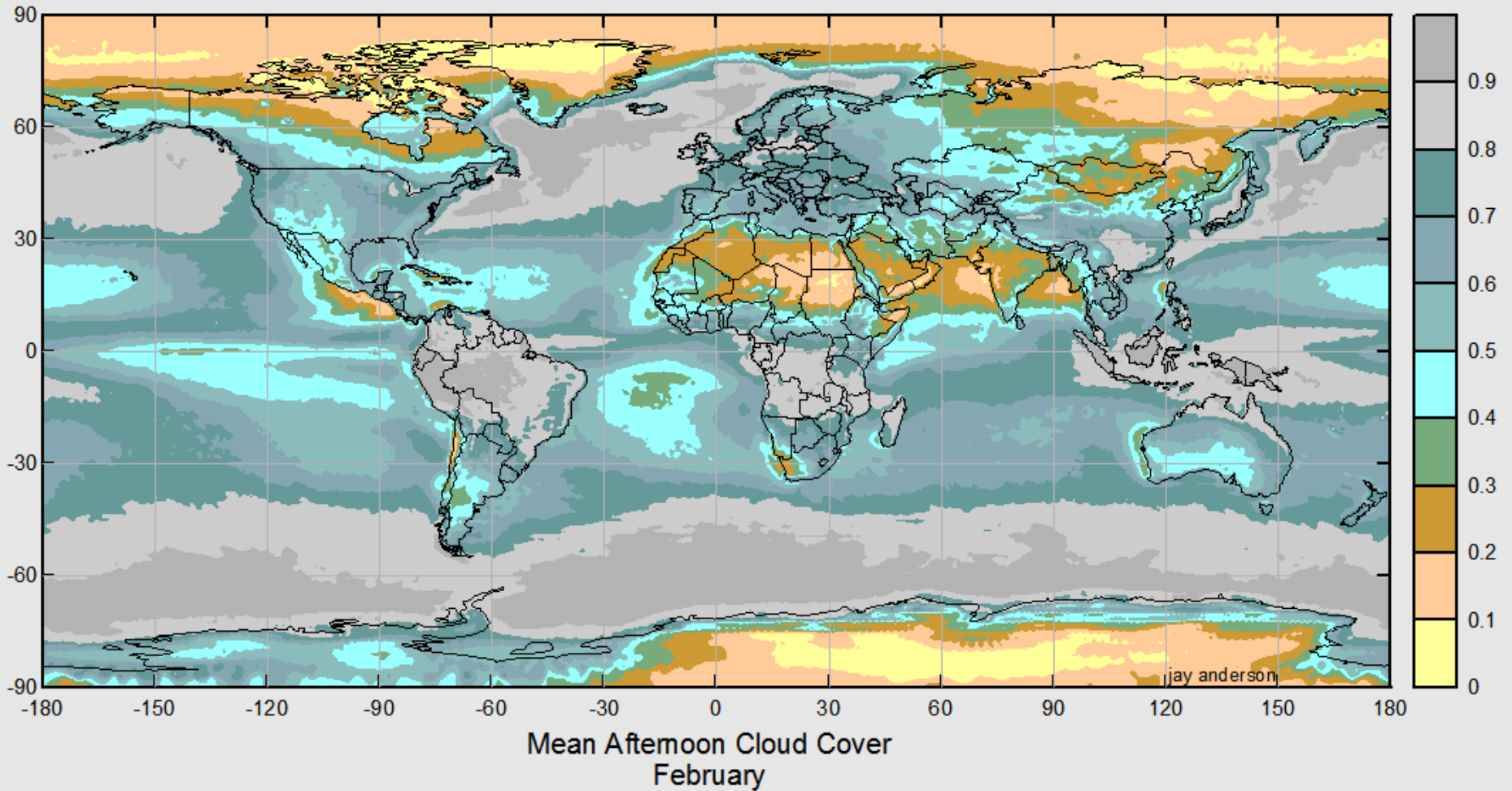
$$I_D = 1.353 \times 0.7^{(AM^{0.678})}$$

$$AM = \frac{1}{\cos \theta}$$

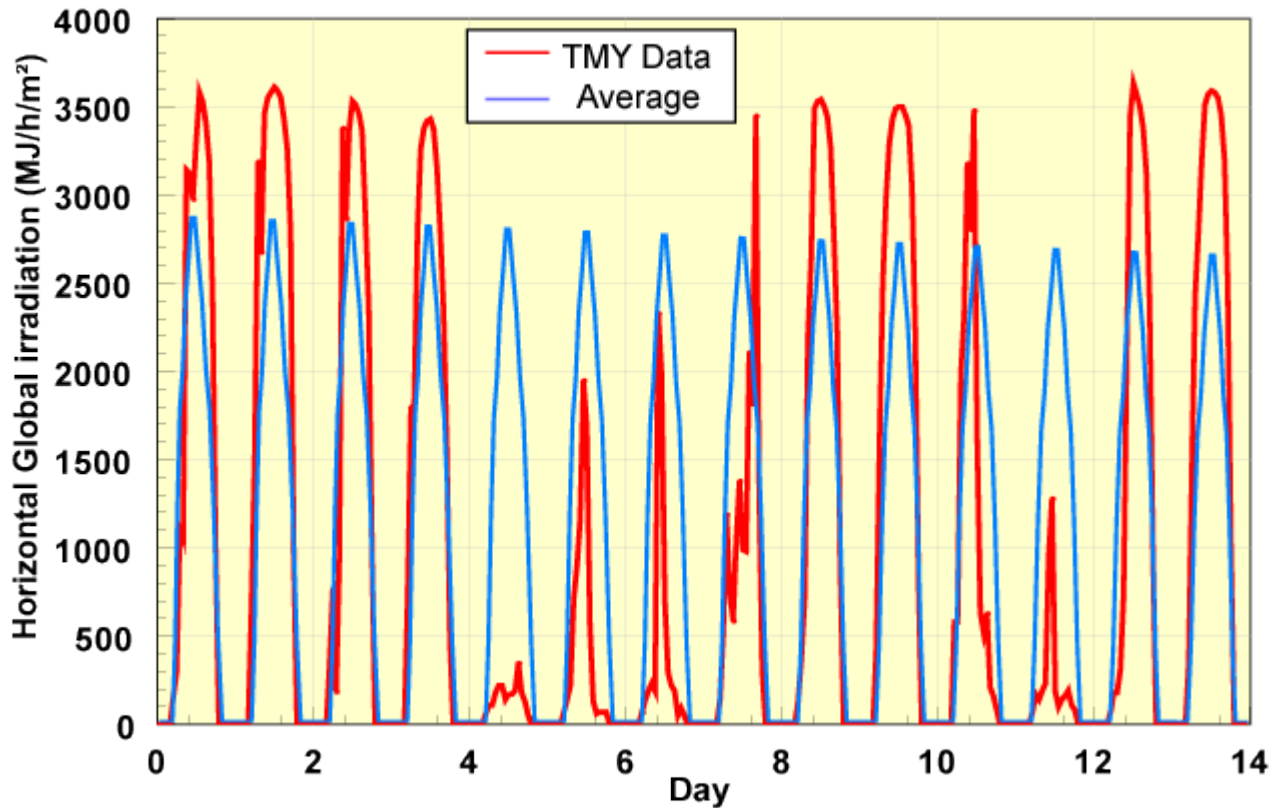
# The contour diagram of the global daily irradiation averaged through the year



# Cloud Cover Data



## Typical Meteorological Year Data (TMY)



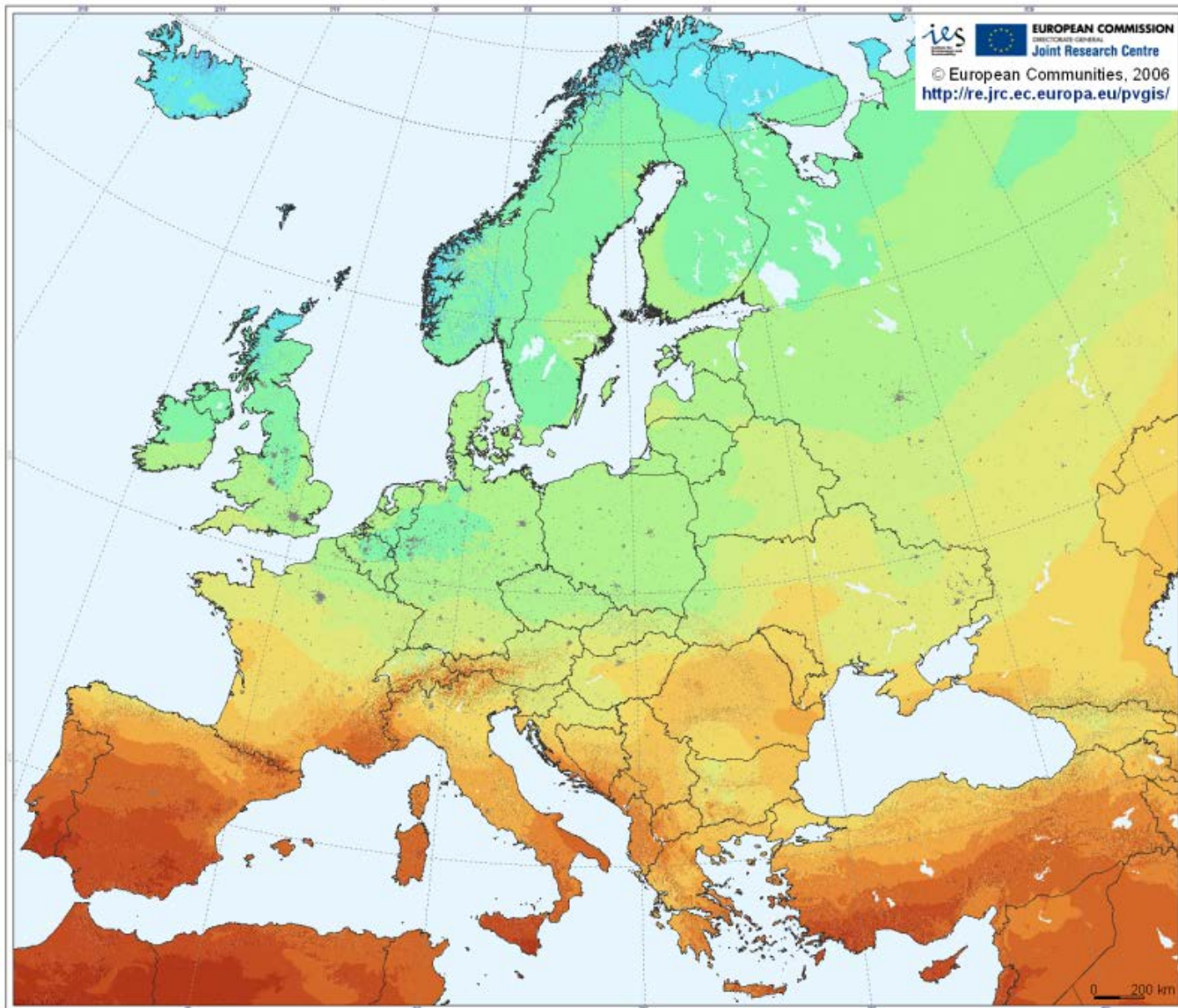
**Solar radiance:** [kWh/m<sup>2</sup>]

**Solar insolation:** total amount of solar energy received during a specific time period [kWh/m<sup>2</sup>day]

**Peak sun hours:** average daily solar insolation in units of kWh/m<sup>2</sup>

**Watt peak (W<sub>p</sub>):** under test conditions of AM1.5 (1000W/m<sup>2</sup>) and 25°C a module produces an electrical output of e.g. 10kW, this is given as 10kW<sub>p</sub>.

# Photovoltaic Solar Electricity Potential in European Countries

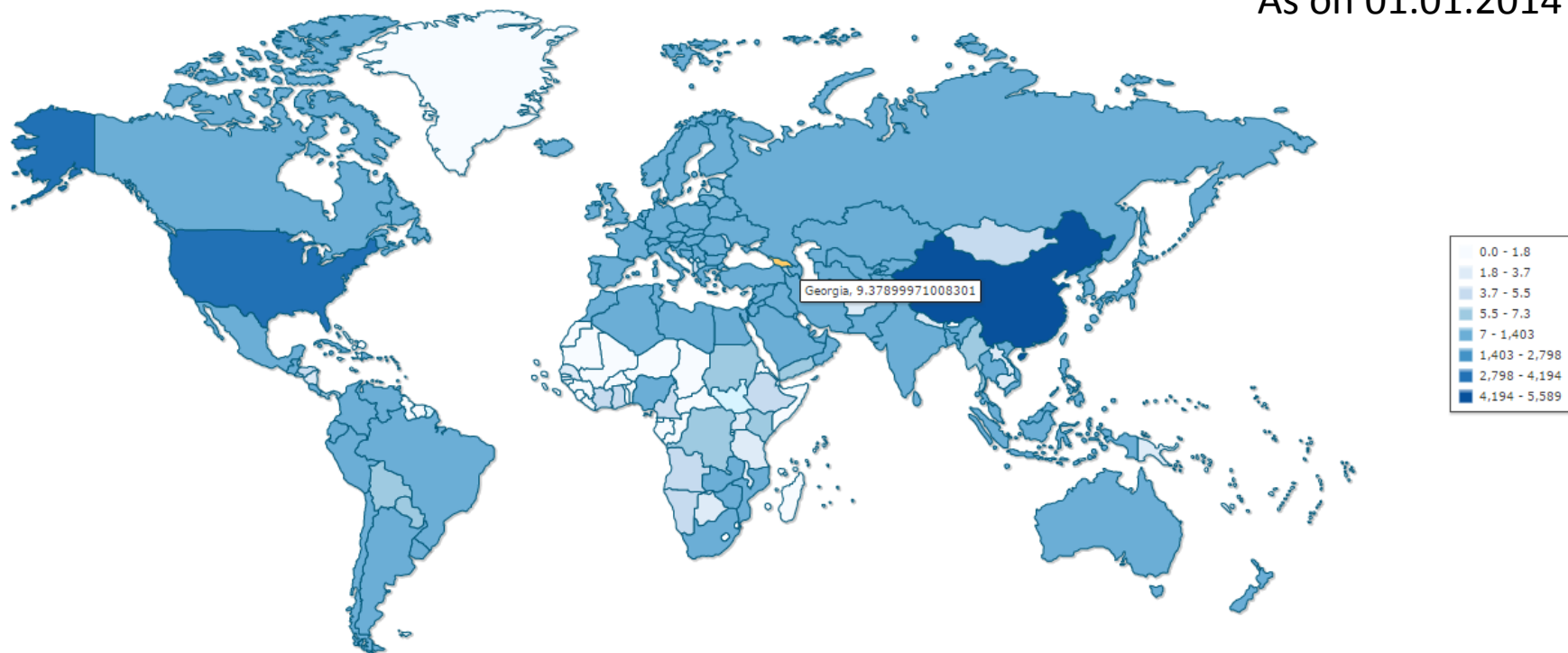


**Yearly sum of global irradiation incident on optimally-inclined south-oriented photovoltaic modules**  
Global irradiation [kWh/m<sup>2</sup>] <600 800 1000 1200 1400 1600 1800 2000 2200>

**Yearly sum of solar electricity generated by 1 kWp system with optimally-inclined modules and performance ratio 0.75**  
Solar electricity [kWh/kWp] <450 600 750 900 1050 1200 1350 1500 1650>

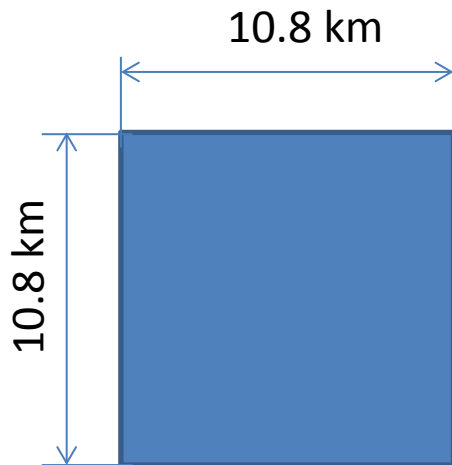
# Electricity consumption in the world

As on 01.01.2014



# For the whole Georgia

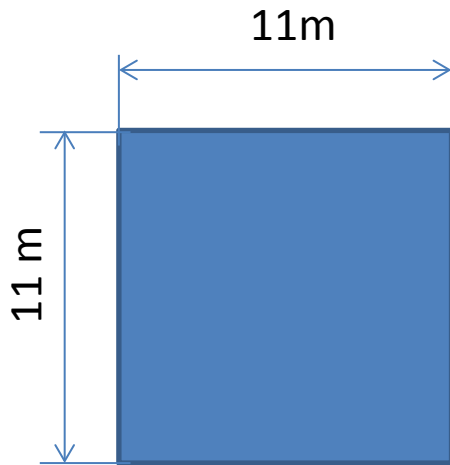
$$\begin{aligned} \text{Area required} &= \frac{\text{Energy consumption } \left(\frac{kWh}{\text{year}}\right)}{\text{Energy resource } \left(\frac{kWh}{m^2 \text{ day}}\right) \times 365 \text{ (day)} \times \text{Efficiency}} = \\ &= \frac{9.38 \cdot 10^9 \text{ kWh/year}}{3.68 \frac{kWh}{m^2 \text{ day}} \times 365 \text{ day} \times 0.06} = 1.16 \cdot 10^8 \text{ m}^2 \end{aligned}$$



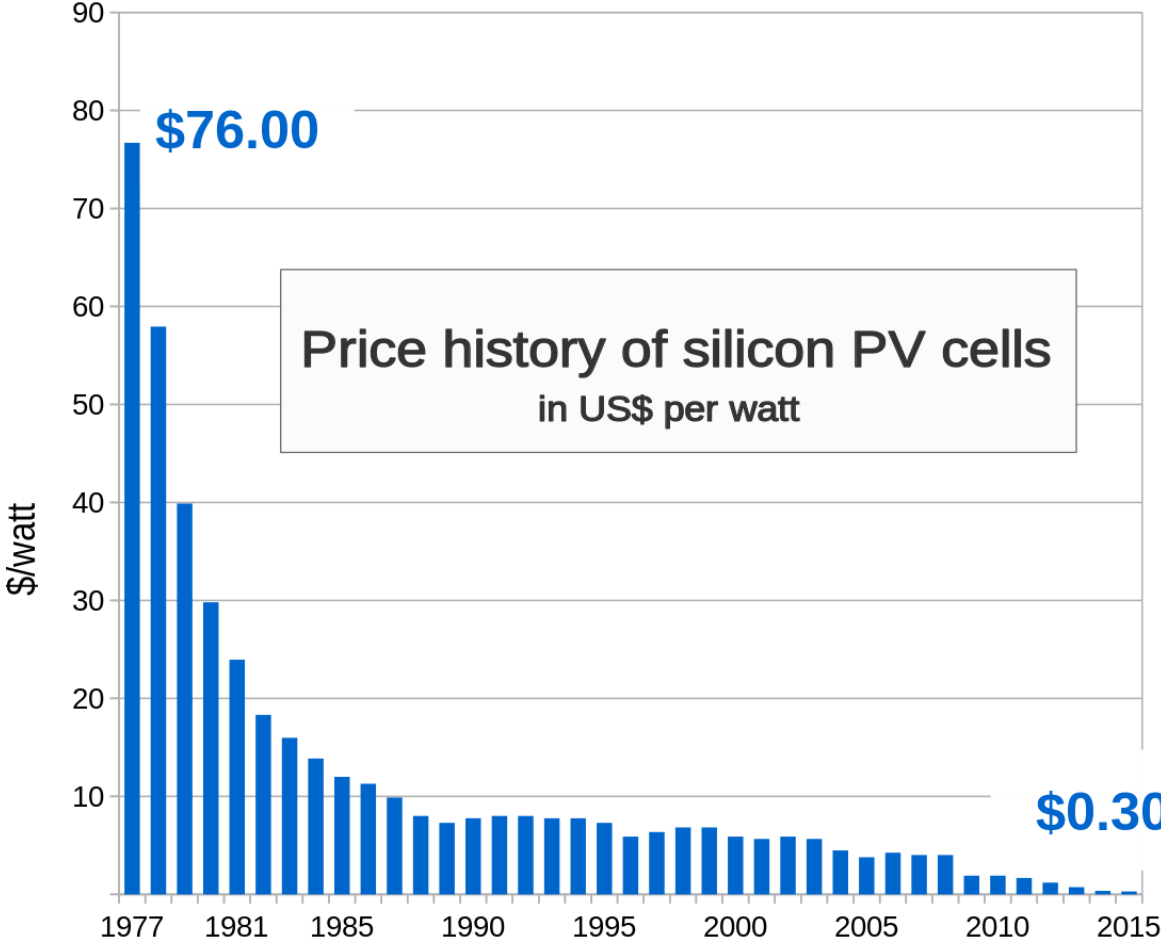


## For a single house

$$\begin{aligned} \text{Area required} &= \frac{\text{Energy consumption } \left(\frac{\text{kWh}}{\text{year}}\right)}{\text{Energy resource } \left(\frac{\text{kWh}}{\text{m}^2\text{day}}\right) \times 365 \text{ (day)} \times \text{Efficiency}} = \\ &= \frac{10^5 \text{ kWh/year}}{3.68 \frac{\text{kWh}}{\text{m}^2\text{day}} \times 365 \text{ day} \times 0.06} = 124 \text{ m}^2 \end{aligned}$$



# Price of Si solar cells



Source: Bloomberg New Energy Finance & pv.energytrend.com

## Price of necessary Si solar cells

$$\begin{aligned} \text{Price}(\$) &= \frac{\text{Required Power (W)} \times \text{price (\$ per WP)}}{W/W_P} = \\ &= \frac{9.38 \cdot 10^{12} \left( \frac{Wh}{\text{year}} \right) \times 0.3 \left( \frac{\$}{W_P} \right)}{365 \text{ day} \times 24 \text{ hour} \times 0.6 \left( \frac{W}{W_P} \right)} \approx 0.535 \cdot 10^9 \$ \end{aligned}$$

Georgia Budget (2013): Budget: revenues:  $4.834 \times 10^9$  \$

Price for a single house  $\approx 6000$  \$

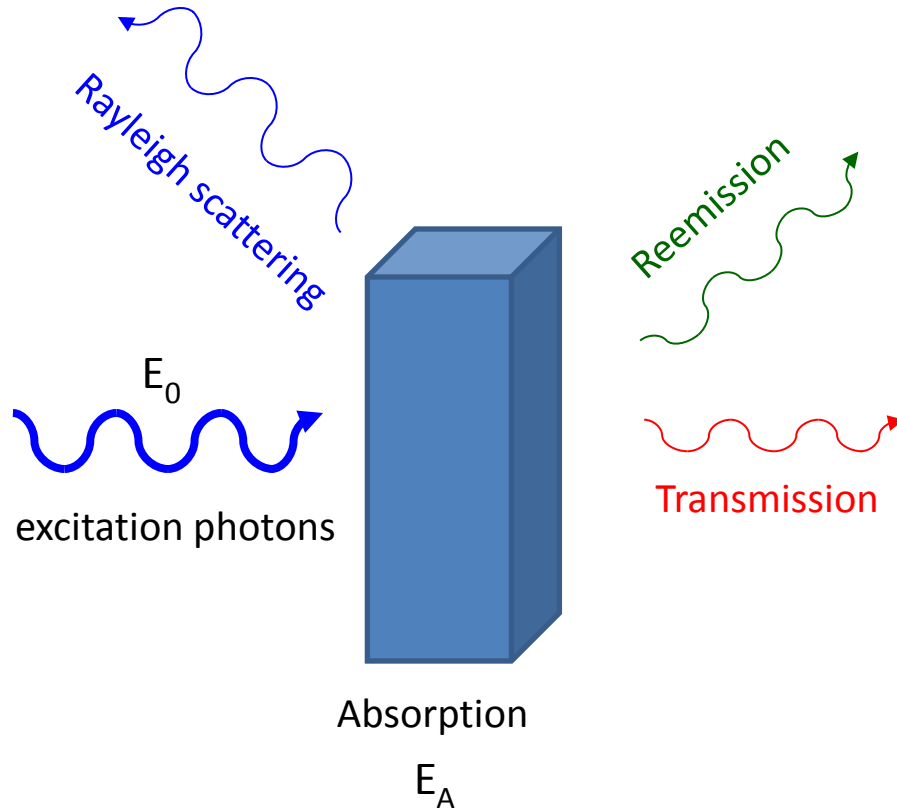
# დასკვნები

- მზის ენერჯის რესურსი 700-ჯერ აღემატება მთელი დედამიწის მოსახლეობის თანამედროვე მოთხოვნილობას ელექტროენერჯიაში.
- მზის პირდაპირი (უშუალო) გამოსხივების გარდა, არსებობს დიფუზიური და არეკლილი გამოსხივება, რომელიც აგრეთვე შეიძლება გამოყენებულ იქნას ენერჯის მოსაპოვებლად.
- შესაძლებელია განვახორციელოთ საკმაოდ კარგი სიზუსტის გამოთვლები იმ ენერჯისა რომლის "მოპოვება" შესაძლებელია მზის გამოსხივებიდან. ასეთ გამოთვლებზე დაყრნობით შედგენილია მზის დასხივების დღიური და წლიური რეჟები.
- აგრეთვე შეიძლება დავითვალოთ მზის პანელების ოპტიმალური ორიენტაცია და საჭირო რაოდენობა.
- საქართველოსთვის მზის ენერჯის გამოყენებას საკმაოდ კარგი პერსპექტივები გააჩნია.

# ლექცია II: მზის ენერჯის გარდაქმნა ელექტრობად ნახევარგამტარების საშუალებით.

- გამოსხივების შთანთქმის ნახევარგამტარებში;
- ეფექტურობის ლიმიტი;
- დენის მატარებლების გენერაცია ფოტონების შთანთქმის შედეგად;
- ენერჯის დანაკარგები; ბრძოლა მაღალი ეფექტურობისათვის;
- ფოტოვოლტაიკური ელემენტების ისტორია.

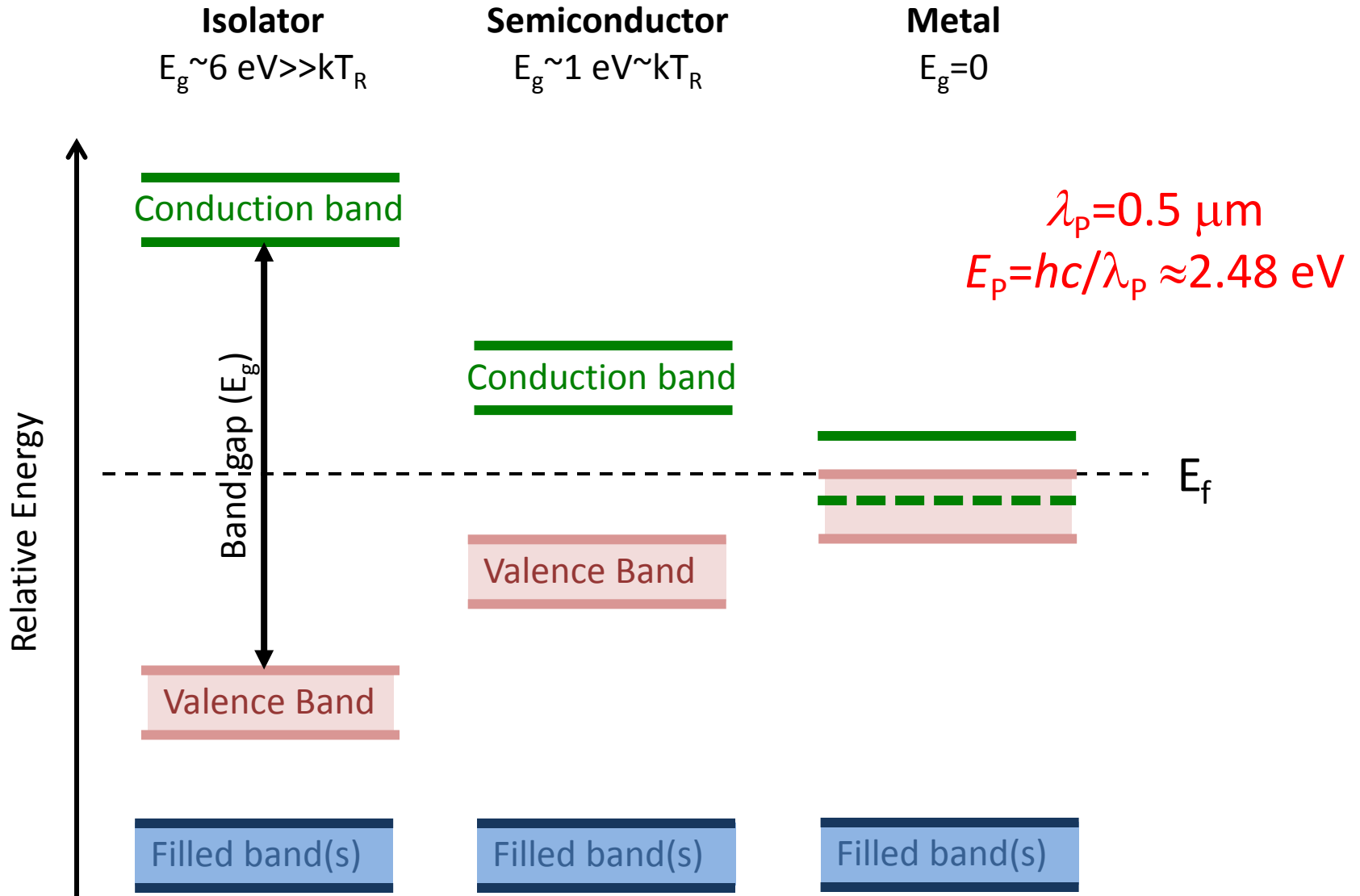
# Interaction of photons with matter



- **Transmission:** “untouched” photons,  $\lambda_{in} = \lambda_{out}$
- **Rayleigh scattering:** elastic scattering, no change in wavelength,  $\lambda_{in} = \lambda_{out}$
- **Reemission:** inelastic (Raman) scattering, Photoluminescence,  $\lambda_{in} < \lambda_{out}$
- **Absorption ( $E_A$ ).**

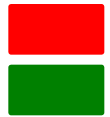
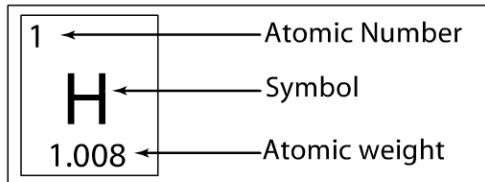
$$E_0 > E_A > E_{el}$$
$$\eta = E_{el}/E_0$$

# Energy band gaps in materials



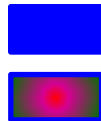
# Periodic table of elements

IA												VIII		IIIA		IVA	VA	VIA	VIIA	VIII		IIA	VIII A																												
1	H													5	B	6	C	7	N	8	O	9	F	10	Ne																										
1.008														10.811	12.011	14.007	15.999	18.998	20.183																																
3	Li	4	Be													13	Al	14	Si	15	P	16	S	17	Cl	18	Ar																								
6.939		9.012														26.981	28.086	30.974	32.064	35.453	39.948																														
11	Na	12	Mg													19	K	20	Ca	21	Sc	22	Ti	23	V	24	Cr	25	Mn	26	Fe	27	Co	28	Ni	29	Cu	30	Zn	31	Ga	32	Ge	33	As	34	Se	35	Br	36	Kr
22.990		24.312														39.102	40.08	44.956	47.90	50.942	51.996	54.938	55.847	58.933	58.71	63.54	65.37	69.72	72.59	74.922	78.96	79.904	83.80																		
37	Rb	38	Sr	39	Y	40	Zr	41	Nb	42	Mo	43	Tc	44	Ru	45	Rh	46	Pd	47	Ag	48	Cd	49	In	50	Sn	51	Sb	52	Te	53	I	54	Xe																
85.47		87.62		88.905		91.22	92.906	95.94	(99)	101.07	102.905	106.4	107.868	112.40	114.82	118.69	121.75	127.60	126.904	131.30																															
55	Cs	56	Ba	57	La	72	Hf	73	Ta	74	W	75	Re	76	Os	77	Ir	78	Pt	79	Au	80	Hg	81	Tl	82	Pb	83	Bi	84	Po	85	At	86	Rn																
132.905		137.34		138.91		178.49	180.948	183.85	186.2	190.2	192.2	195.09	196.967	200.59	204.37	207.19	208.980	(210)	(210)	(222)																															
87	Fr	88	Ra	89	Ac													58	Ce	59	Pr	60	Nd	61	Pm	62	Sm	63	Eu	64	Gd	65	Tb	66	Dy	67	Ho	68	Er	69	Tm	70	Yb	71	Lu						
(223)		(226)		(227)													140.12	140.907	144.24	(147)	150.35	151.96	157.25	158.924	162.50	164.930	167.26	168.934	173.04	174.97																					
																						90	Th	91	Pa	92	U	93	Np	94	Pu	95	Am	96	Cm	97	Bk	98	Cf	99	Es	100	Fm	101	Md	102	No	103	Lr		
																						232.038	(231)	238.03	(237)	(244)	(243)	(247)	(247)	(251)	(254)	(257)	(256)	(254)	(260)																



Group IV (Si, Ge)

Group III-V (GaAs, InP,...)

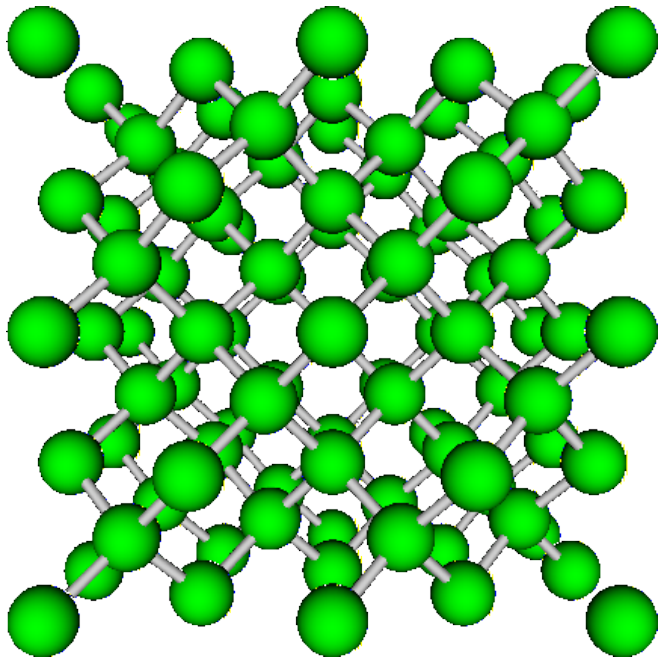


Group II-VI (ZnTe, CdS, ...)

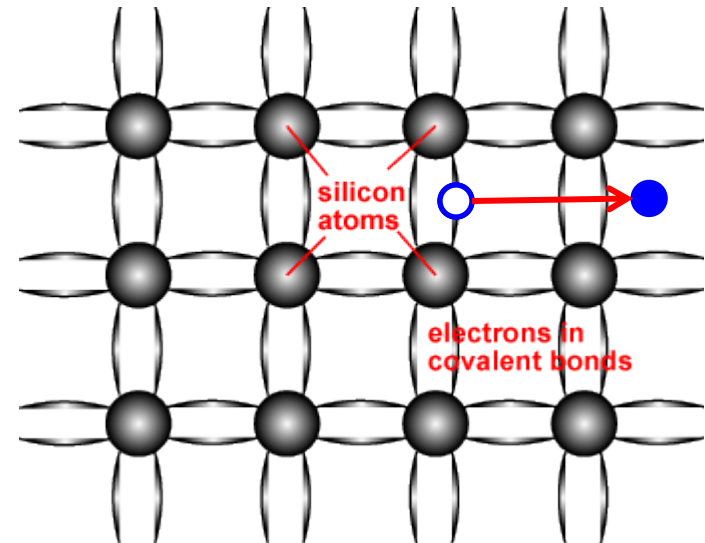
Compound, Alloy ( $Al_xGa_{(1-x)}As$ ,  $CuO$ ,  $Si_xGe_{1-x}$ ...)



# Silicon: atomic structure

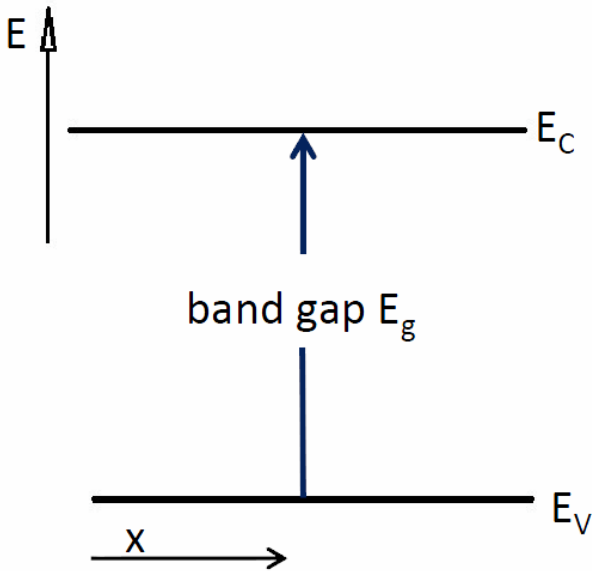


Diamond structure  
Si, Ge

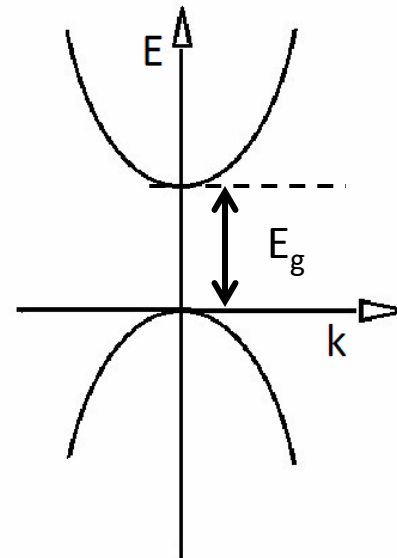


2D - representation

# Energy band diagram, band structure

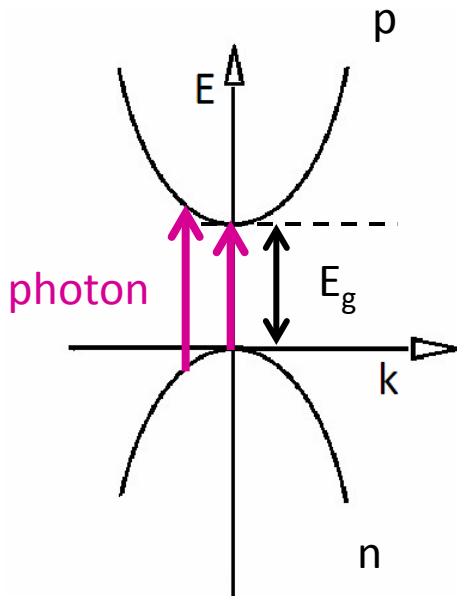


energy band diagram  $E(x)$



band structure  $E(k)$   
dispersion relation

# Photon absorption: conservation rules



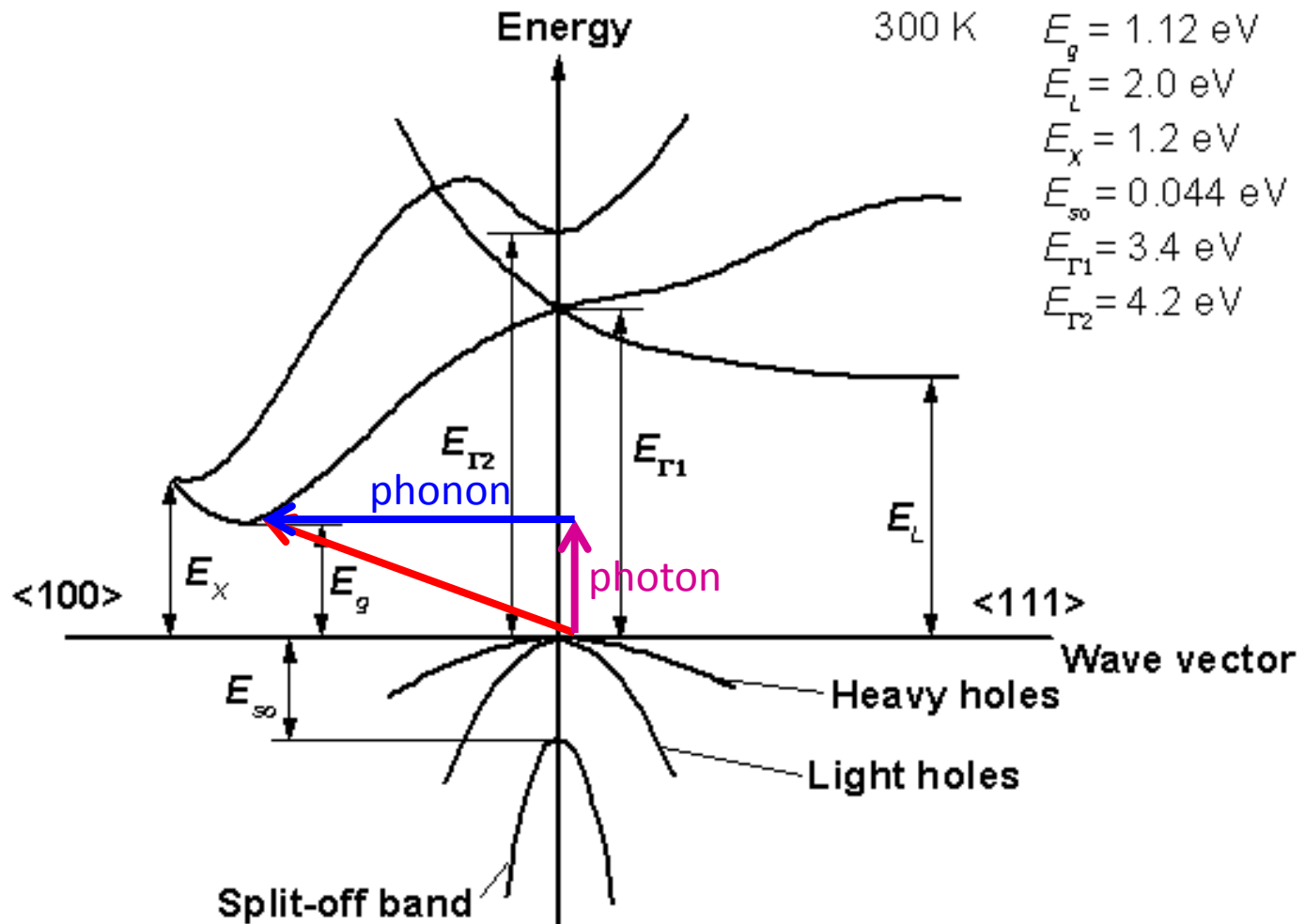
Energy:

$$\hbar\omega_{phot} = E_g + \frac{\hbar^2 k_n^2}{2m_n} + \frac{\hbar^2 k_p^2}{2m_p} \pm \hbar\omega_{phon}$$

Momentum:

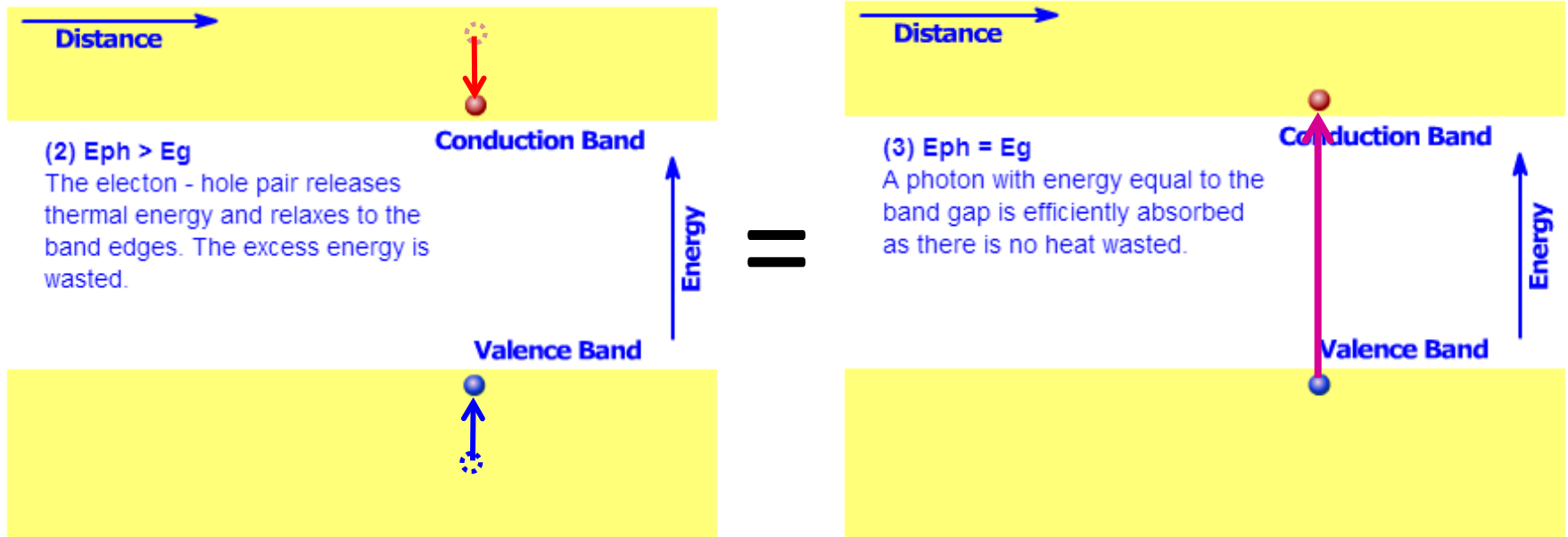
$$\hbar\vec{k}_{phot} = \hbar(\vec{k}_n + \vec{k}_p) + \hbar\vec{k}_{phon}$$

# Formation of electron-hole pair by photon



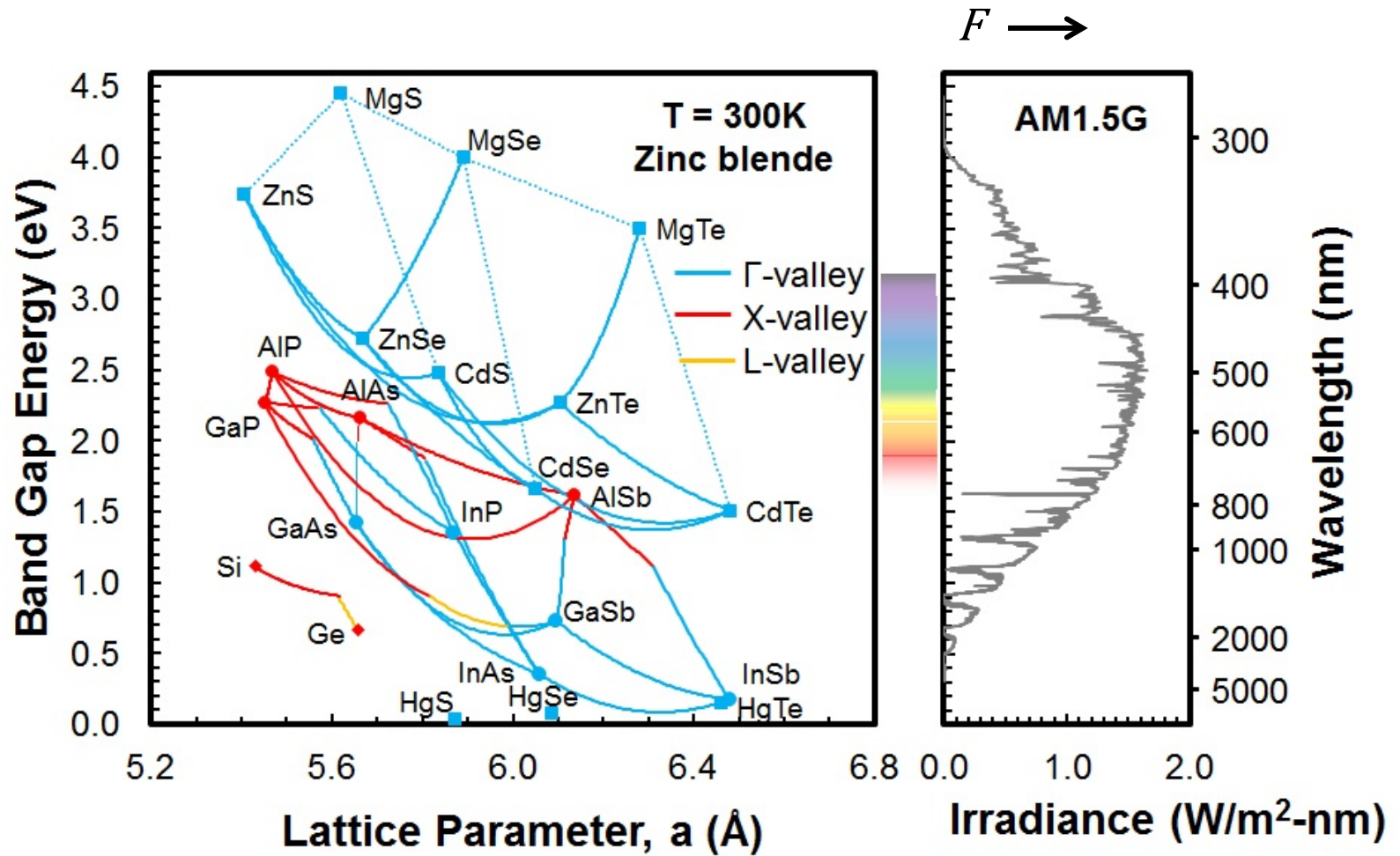
# Formation of electron-hole pair by photon

So called „Internal photo effect“



Photons with  $\hbar\omega > E_g$  create electron-hole pairs with energy  $E_g$

# Band gaps and solar spectra



# Looking for optimal bandgap

All photons are absorbed, no reflection, out of atmosphere...

Efficiency:  $\eta_0 = \frac{H_{el}}{H_0}$

$H_{el}$ : electrical power density (W/m<sup>2</sup>)

$H_0$ : solar constant

$$H_0 = \frac{R_{sun}^2}{D^2} H_{sun} = \rho^2 \sigma \cdot T_S^4$$

Stefan-Boltzman,  $\rho = R_{sun}/D$

$$H_{el} = \rho^2 \cdot \int_{\nu=0}^{\infty} F(\nu) d\nu$$

$$F(\nu, T_S) d\nu = \Phi(\nu, T_S) \cdot h\nu d\nu$$

$F$ : spectral irradiance

$\Phi$ : photonflux

$$H_{el} = \rho^2 \cdot \int_{\nu=0}^{\infty} \Phi \cdot h\nu d\nu$$

For each absorbed photon with  $h\nu \geq E_g$  an electron-hole pair with energy  $h\nu_g$  is created

$$H_{el} = \rho^2 \cdot h\nu_g \int_{\nu_g}^{\infty} \Phi(\nu, T_S) d\nu$$

# Looking for optimal bandgap

Spectral irradiance of a blackbody  $F(\lambda, T) = \frac{2\pi h c^2}{\lambda^5 \left( \exp\left(\frac{E}{kT}\right) - 1 \right)}$

[Planck, Annalen der Physik 4, 553-563 (1901)]

$$\lambda = \frac{c}{\nu}; \quad d\lambda = -\frac{cd\nu}{\nu^2} = -\frac{\lambda^2 d\nu}{c}; \quad F(\lambda, T)d\lambda = \frac{2\pi h \nu^2}{\left(\frac{c}{\nu}\right)^3 \left(\exp\left(\frac{E}{kT}\right) - 1\right)} \frac{cd\nu}{\nu^2} = \frac{2\pi h \nu^3}{c^2 \left(\exp\left(\frac{E}{kT}\right) - 1\right)} d\nu;$$

$$\Phi(\nu, T_S)d\nu = \frac{2\pi h \nu^3}{h\nu c^2 \left(\exp\left(\frac{E}{kT}\right) - 1\right)} d\nu = \frac{2\pi \nu^2}{c^2 \left(\exp\left(\frac{h\nu}{kT_S}\right) - 1\right)} d\nu$$

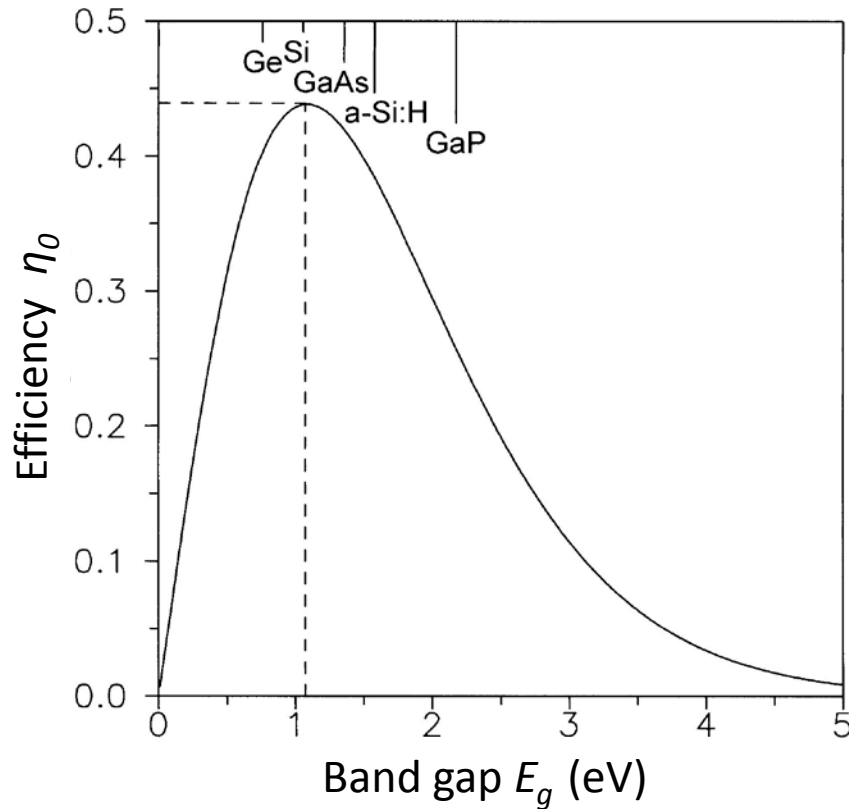
$$\eta_0 = \frac{H_{el}}{H_0} = \frac{h\nu_g}{\sigma \cdot T_S^4} \int_{\nu_g}^{\infty} \Phi(\nu, T_S)d\nu = \frac{h\nu_g}{\sigma \cdot T_S^4} \int_{\nu_g}^{\infty} \frac{2\pi \nu^2}{c^2 \left(\exp\left(\frac{h\nu}{kT_S}\right) - 1\right)} d\nu = \frac{h\nu_g}{\sigma \cdot T_S^4} \frac{2\pi}{c^2} \int_{\nu_g}^{\infty} \frac{\nu^2}{\left(\exp\left(\frac{h\nu}{kT_S}\right) - 1\right)} d\nu$$

$$\eta_0 = \frac{h\nu_g}{\sigma \cdot T_S^4} \frac{2\pi}{c^2} \cdot I \quad \text{Integral } I \text{ can be calculated analytically (see [1])}$$

$$I = \nu_g^3 \cdot \frac{1}{x^4} G(x) \quad x = \frac{h\nu_g}{kT_S} \quad G(x) = \frac{x^3}{e^x - \frac{1}{2}} + \frac{2x^2}{e^x - \frac{1}{4}} + \frac{2x}{e^x - \frac{1}{8}}$$



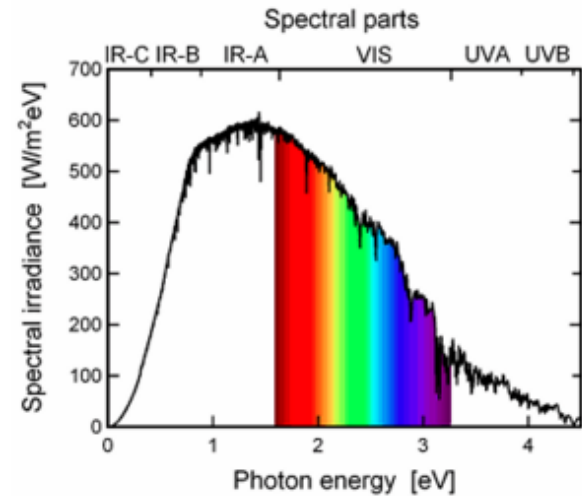
# Looking for optimal bandgap



$$\eta_0 = \frac{15}{\pi^4} \cdot G(x)$$

**! Ultimate efficiency  $\eta_0$  !**

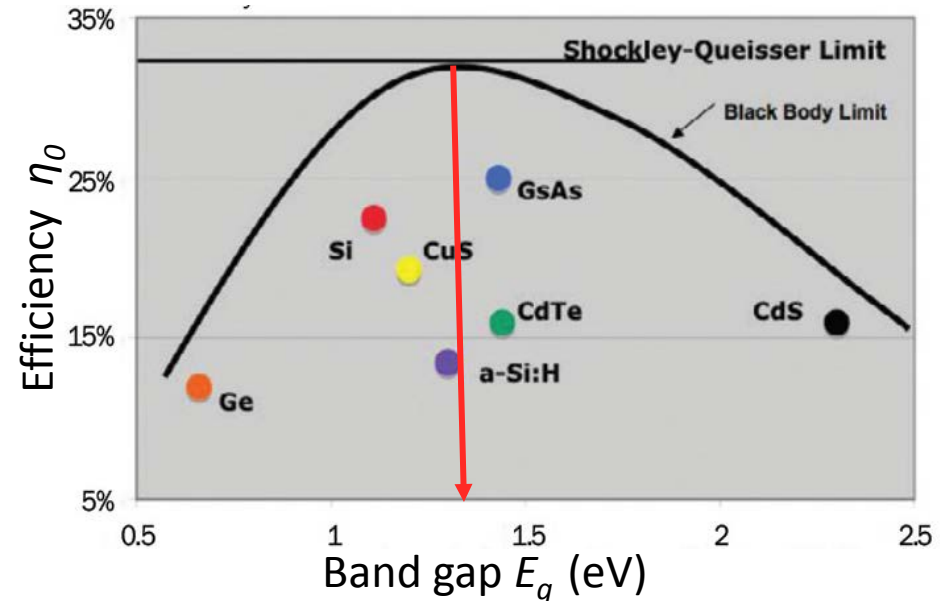
The only criteria is the band gap of the semiconductor.



# The Shockley-Queisser efficiency limit

## The Critical SQ Limit Assumptions:

- One semiconductor material (excluding dopants) per solar cell;
- One p/n junction per solar cell;
- The sunlight is not concentrated - a "one sun" source;
- All energy is converted to heat from photons greater than the band gap.

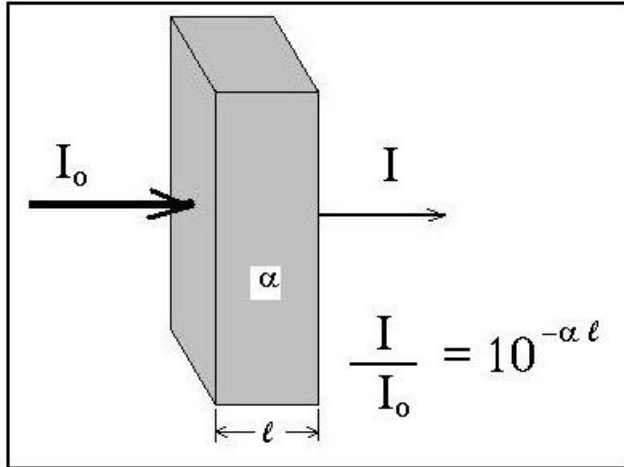


## Where Does The 67% Of Energy Loss Go?

- 47% of the solar energy gets converted to heat.
- 18% of the photons pass through the solar cell.
- 0.2% of energy is lost from local recombination of newly created holes and electrons.

According to the SQ model the optimal band-gap for the solar spectra is 1.4 eV

# Light absorption, Lambert-Beer's law



Spectral photon flux:  $\Phi(\lambda) = \frac{F(\lambda)}{hc} \lambda$

In homogeneous semiconductor  $\Phi(\lambda)$  will be reduced proportional to its value and thickness:

$$-\frac{\partial \Phi(\lambda, x)}{\partial x} = \alpha(x) \Phi(\lambda, x)$$

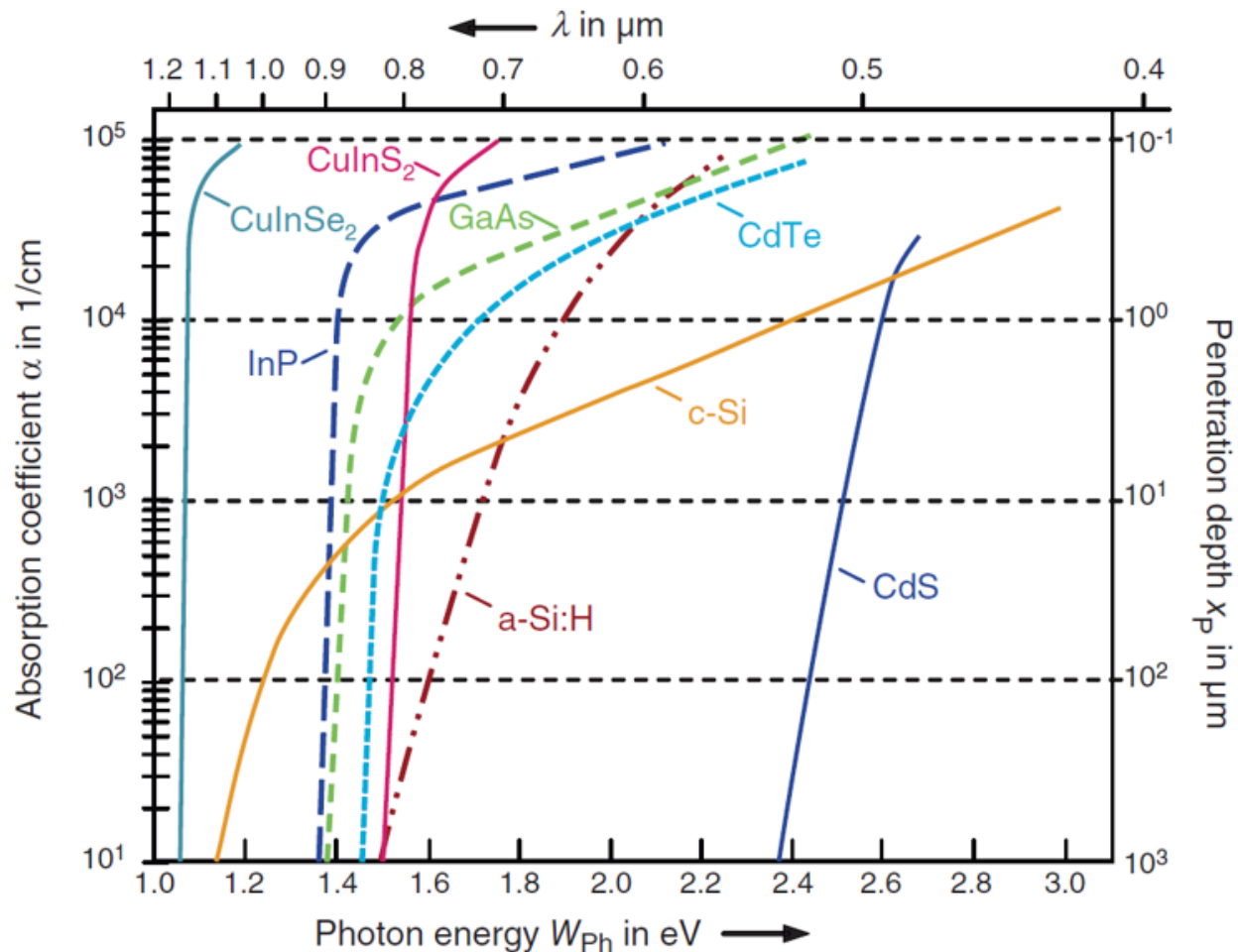
$$\Phi(\lambda, x) = \Phi(\lambda, x = 0) e^{-\alpha(\lambda)x}$$

By absorption of photons, electron-hole pairs are generated.

Generation rate:  $G(\lambda, x) = -\frac{\partial \Phi(\lambda, x)}{\partial x}$  where  $G$  (N/s m<sup>3</sup>), N number of electrons.

$$G(\lambda, x) = \alpha(x) \Phi(\lambda, x = 0) e^{-\alpha(\lambda)x}$$

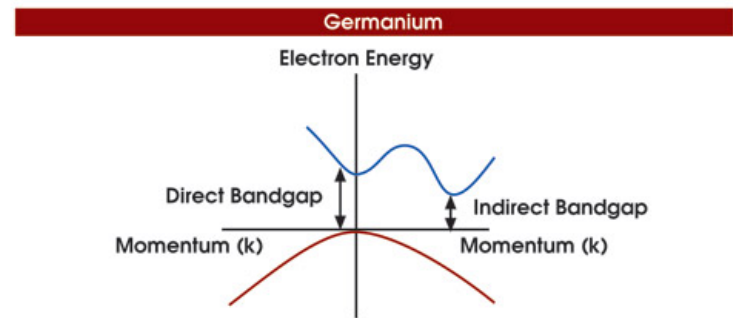
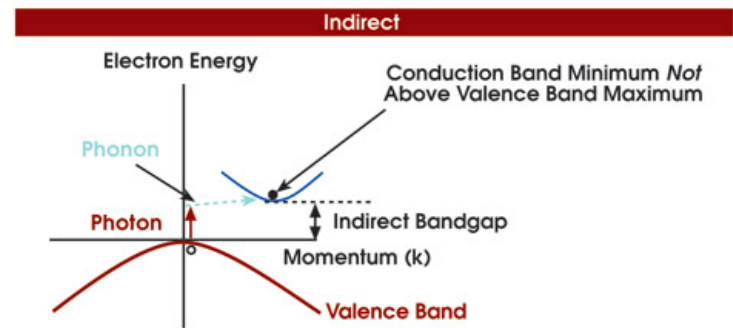
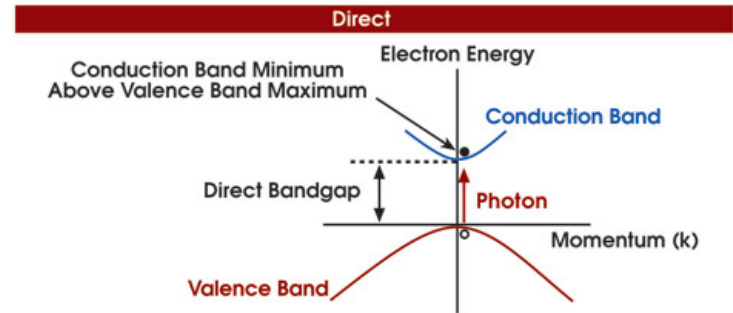
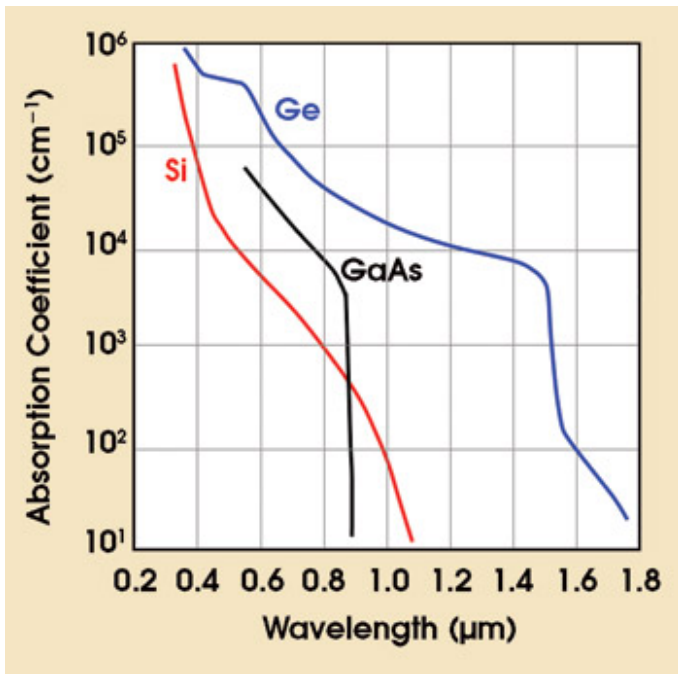
# Absorption coefficients in semiconductors



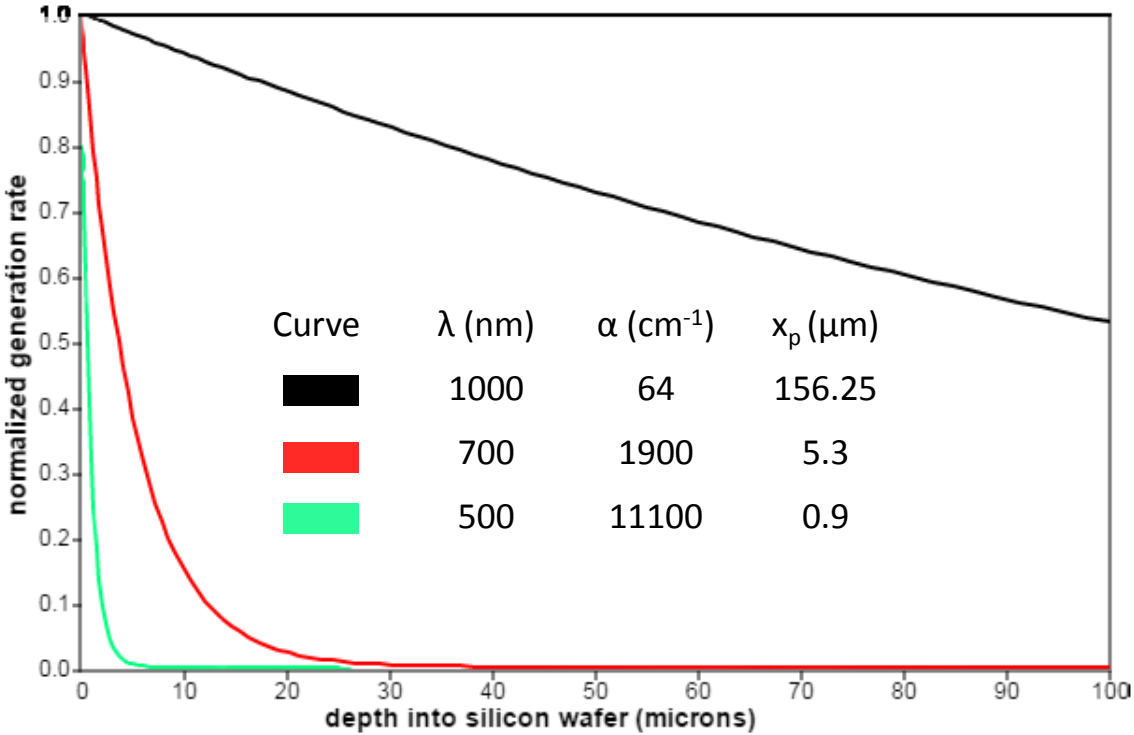
Source: K. Mertens: textbook-pv.org

The absorption (penetration) depth is the inverse of the absorption coefficient. An absorption depth of, for example,  $1 \mu\text{m}$  means that the light intensity has fallen to 36% ( $1/e$ ) of its original value.

# Absorption coefficients in semiconductors



# Generation rate for various wavelengths

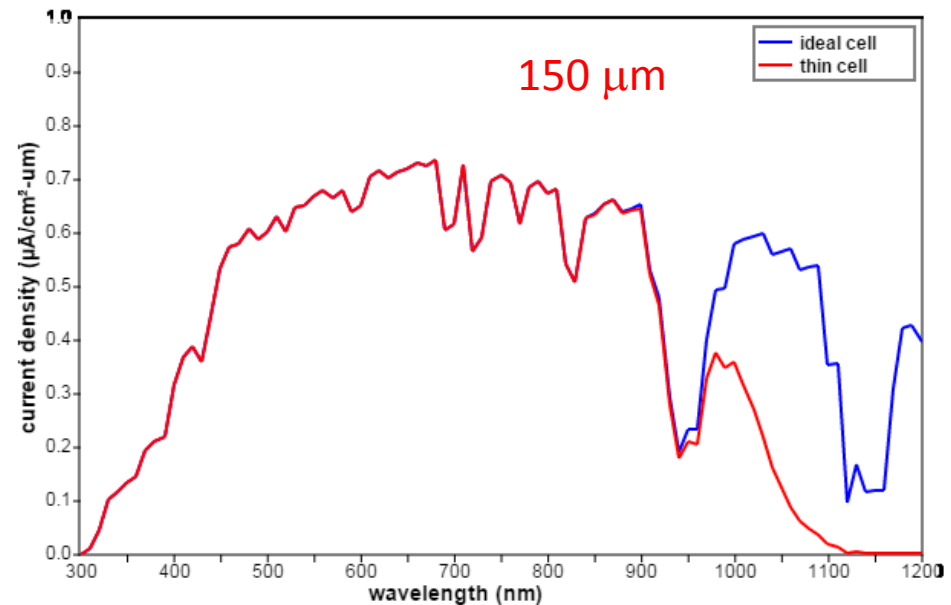
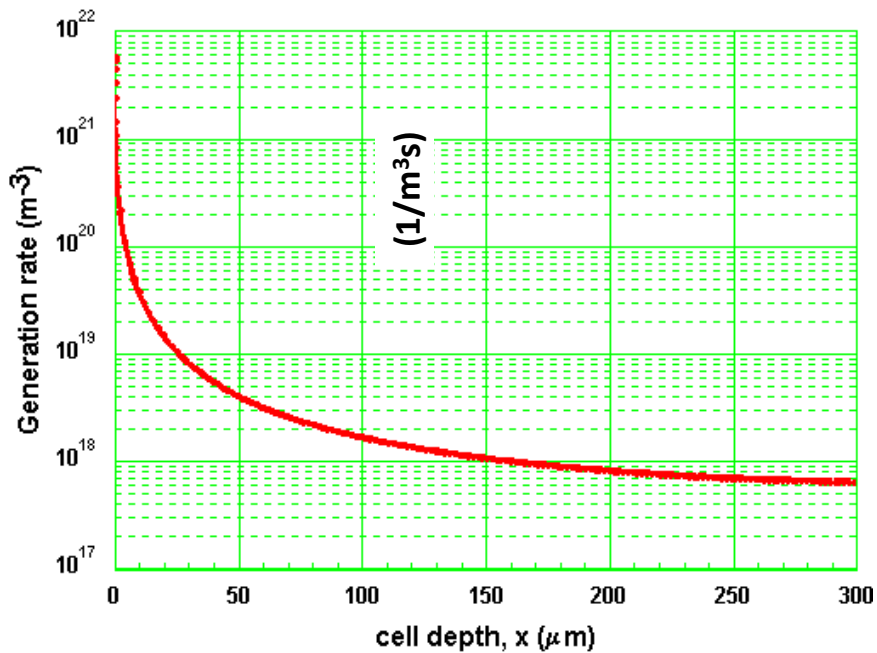


Silicon, 300 K

# Generation rate for solar spectrum

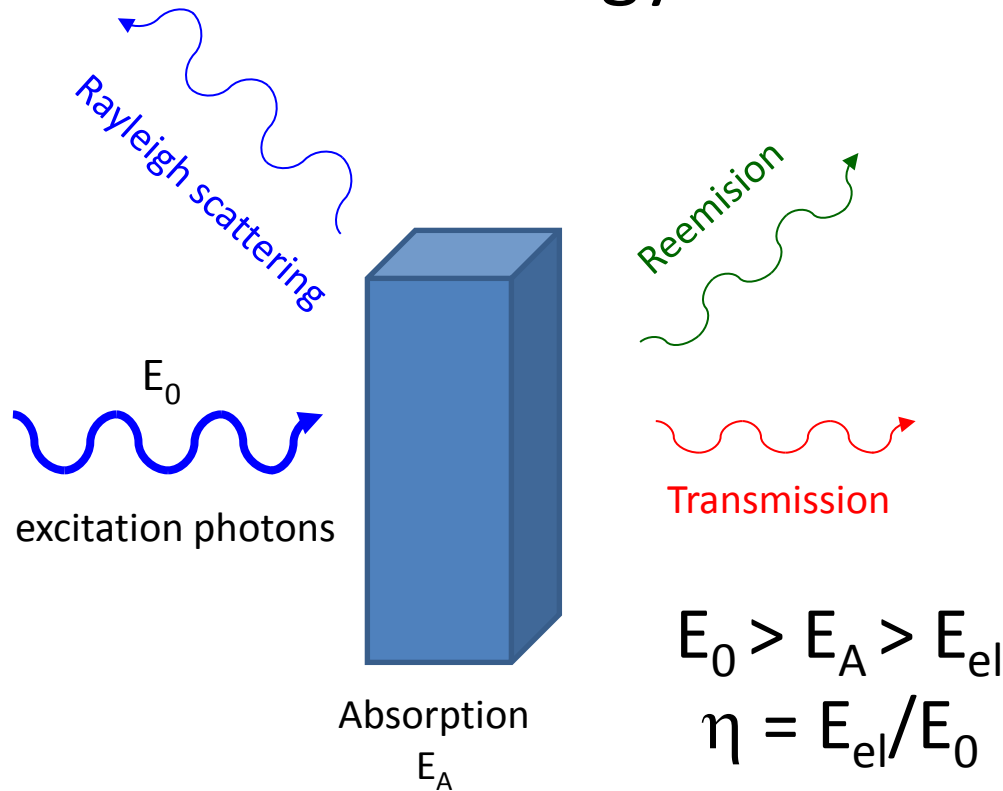
$$G(x) = \int_0^{\lambda_g} G(\lambda, x) d\lambda \quad \text{with} \quad \lambda_g = \frac{hc}{E_g}$$

For a standard solar spectrum (AM 1.5) incident on silicon:



Generation rate of electron-hole pairs in a piece of silicon as a function of distance into the cell. The cell front surface is at 0  $\mu\text{m}$  and most of the high energy photons are absorbed very close to it.

# Energy losses - efficiency



- **Transmission:**  $E_g$  too large
- **Scattering:** Surface and photon – phonon interactions
- **Reemission:** non-separation and defects
- **Thermalisation:**  $E_g$  too small



$$\eta_{TOTAL} = \eta_{ABSORPTION} \times \eta_{EXCITATION} \times \eta_{SEPARATION} \times \eta_{DRIFT} \times \eta_{COLLECTION}$$



# Suppress losses – increase efficiency

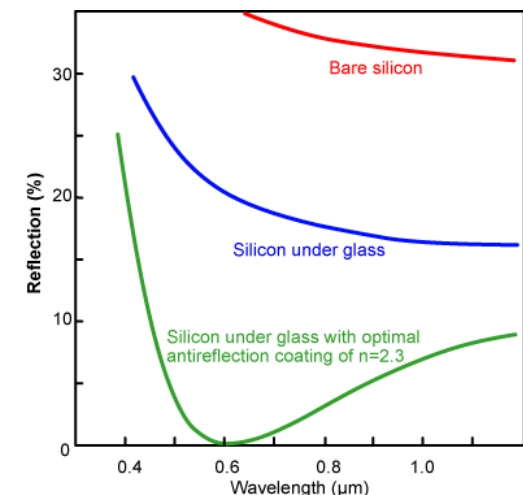
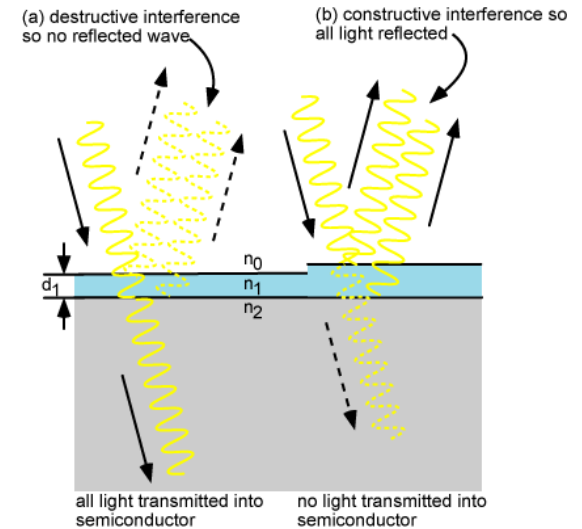
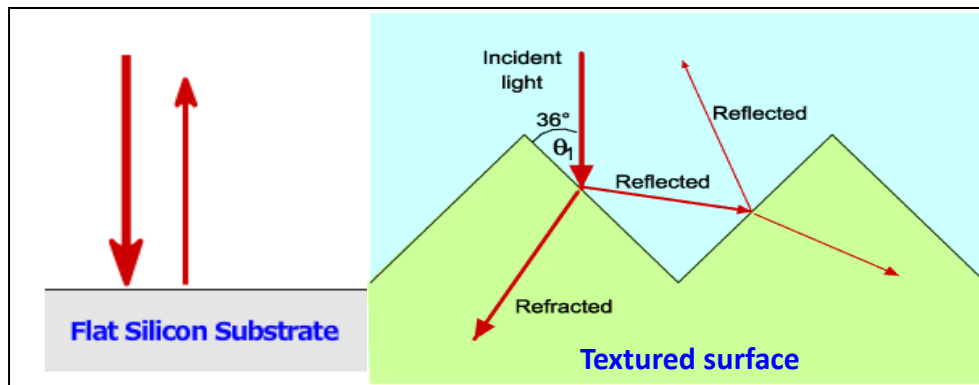
$$\eta_{\text{TOTAL}} = \eta_{\text{ABSORPTION}} \times \eta_{\text{EXCITATION}} \times \eta_{\text{SEPARATION}} \times \eta_{\text{DRIFT}} \times \eta_{\text{COLLECTION}}$$

For minimizing absorption losses: “Light management methods”

- Anti-reflection coating;
- Surface texturization;
- Back surface reflection, “light trapping”;
- Etc.

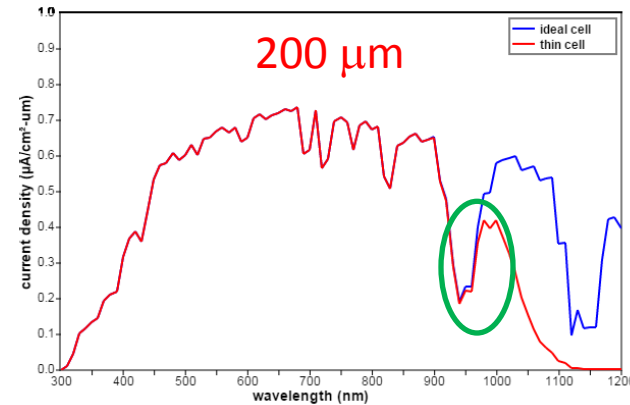
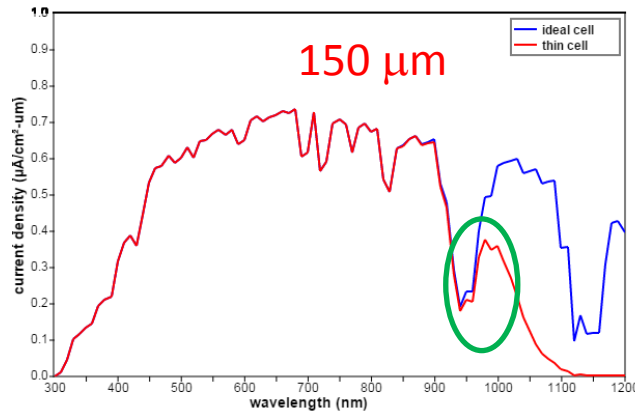
$$d_1 = \lambda_0 / 4n_1 \text{ (e.g. for } n_1=2 \text{ and } \lambda_0=560 \text{ nm, } d_1=70 \text{ nm)}$$

$$n_1 = (n_0 \times n_2)^{1/2} \text{ (} n_2(\text{Si, } 560 \text{ }\mu\text{m}) \approx 4, n_0(\text{air})=1)$$



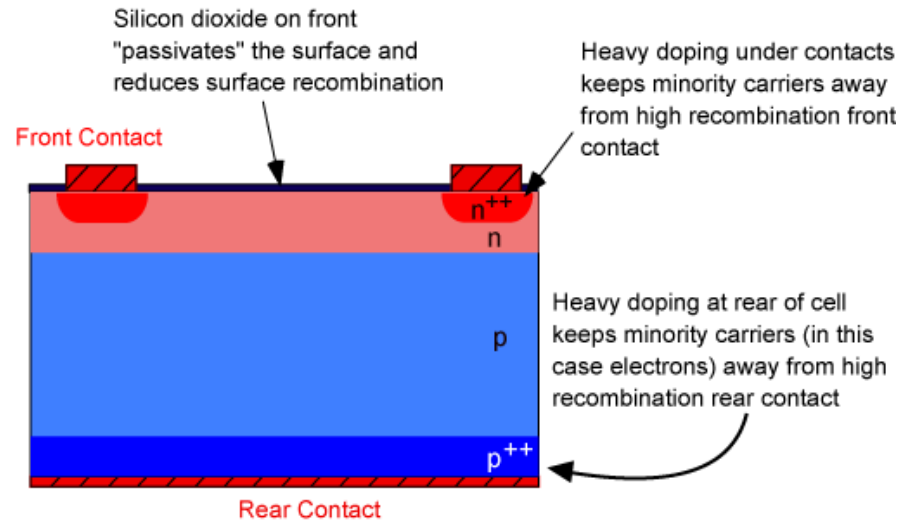
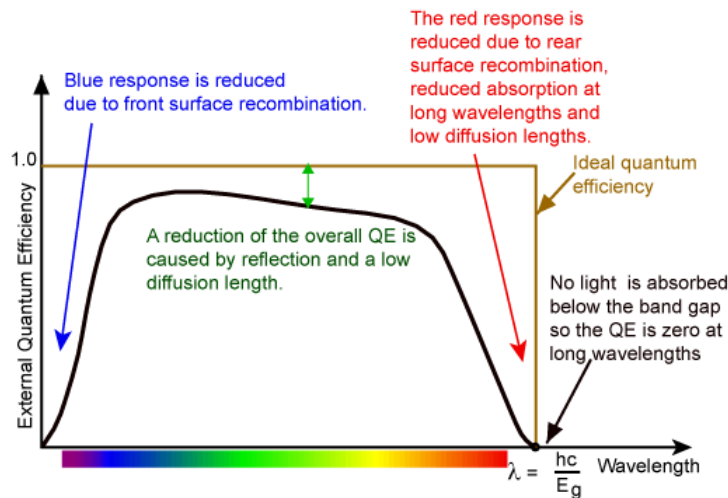
# Suppress losses – increase efficiency

$$\eta_{\text{TOTAL}} = \eta_{\text{ABSORPTION}} \times \eta_{\text{EXCITATION}} \times \eta_{\text{SEPARATION}} \times \eta_{\text{DRIFT}} \times \eta_{\text{COLLECTION}}$$

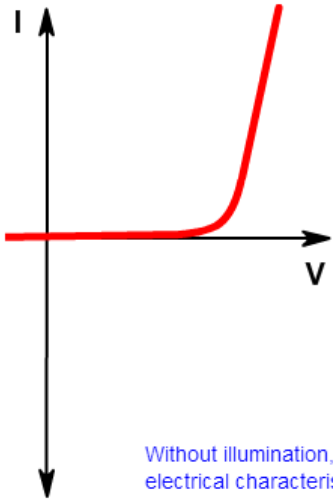


$$\eta_{\text{TOTAL}} = \eta_{\text{ABSORPTION}} \times \eta_{\text{EXCITATION}} \times \eta_{\text{SEPARATION}} \times \eta_{\text{DRIFT}} \times \eta_{\text{COLLECTION}}$$

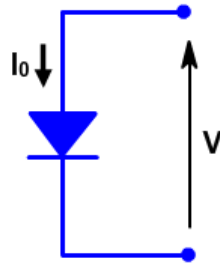
## “Recombination losses”



# IV curve for a solar cell

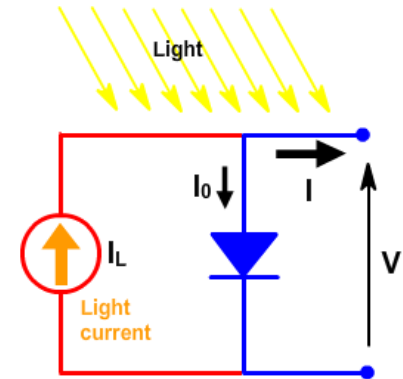
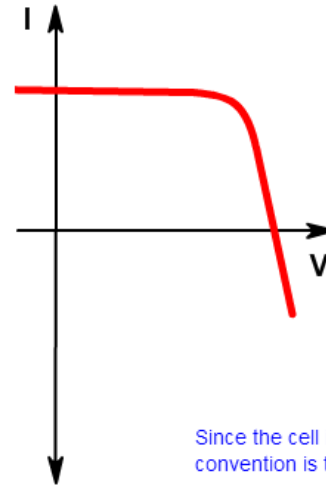


Without illumination, a solar cell has the same electrical characteristics as a large diode.



$$I = I_0 [\exp(qV/nkT) - 1]$$

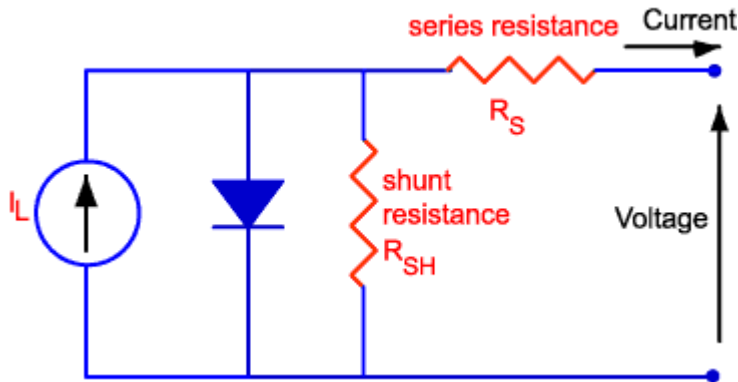
$$I = I_L - I_0 [\exp(qV/nkT) - 1]$$



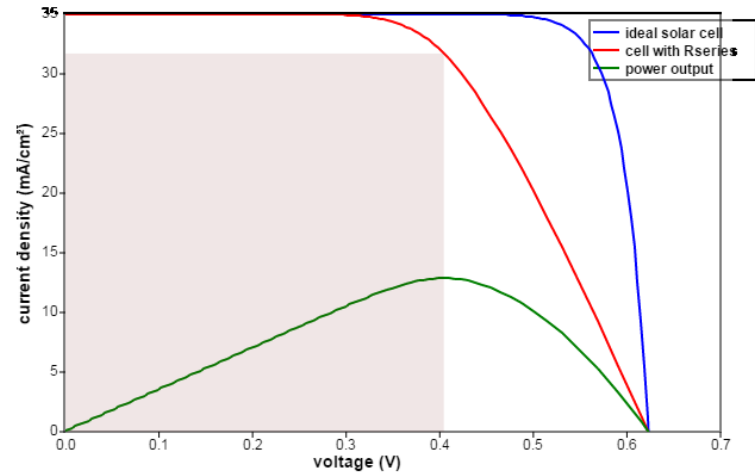
Since the cell is generating power the convention is to invert the current axis.

# Suppress losses – increase efficiency

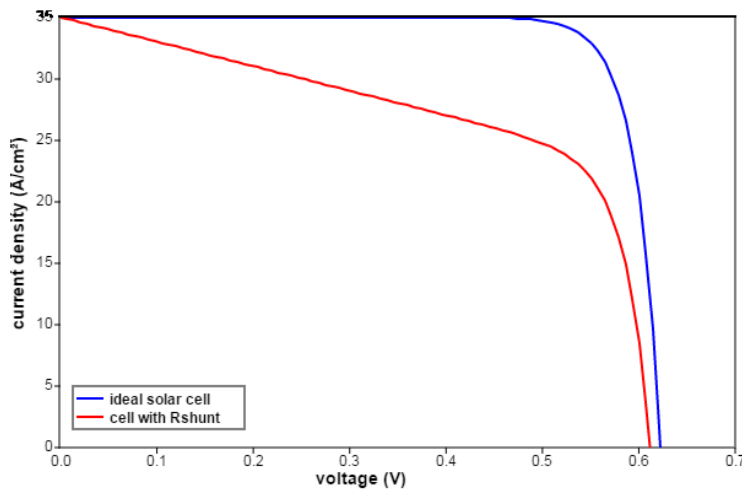
$$\eta_{\text{TOTAL}} = \eta_{\text{ABSORPTION}} \times \eta_{\text{EXCITATION}} \times \eta_{\text{SEPARATION}} \times \eta_{\text{DRIFT}} \times \eta_{\text{COLLECTION}}$$



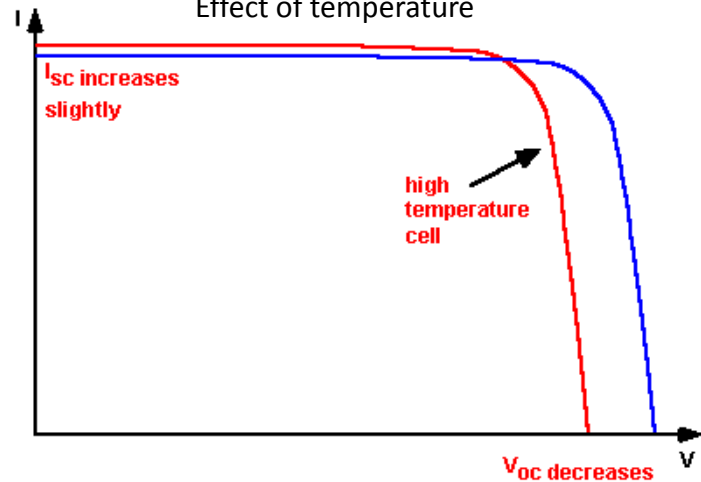
Cell series resistance  $5 \Omega\text{cm}^2$



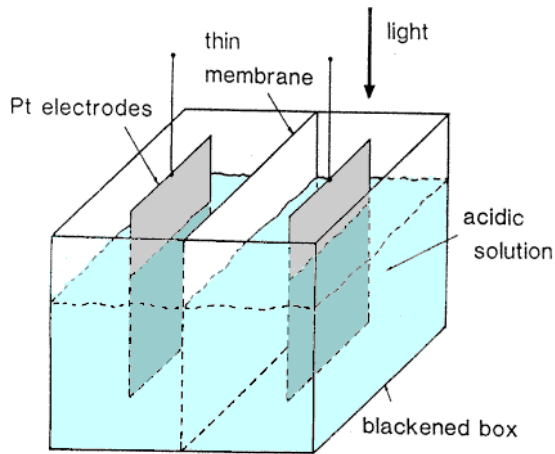
Cell shunt resistance  $50 \Omega\text{cm}^2$



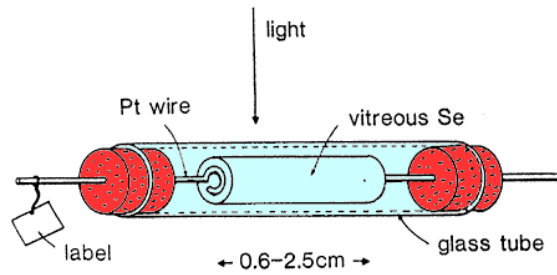
Effect of temperature



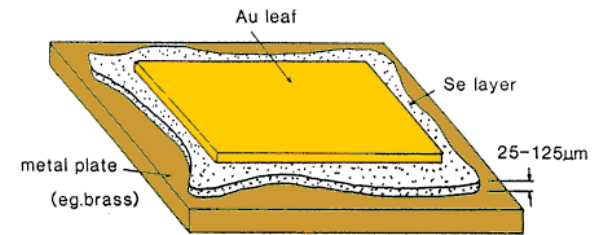
# The history of photovoltaic devices



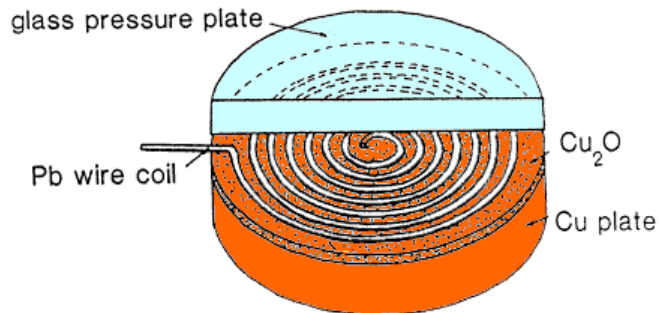
Edmond Becquerel (1839)



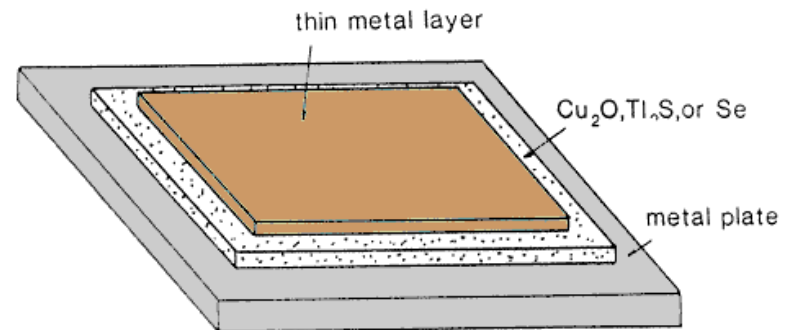
Adams and Day (1876)



Fritts (1883)

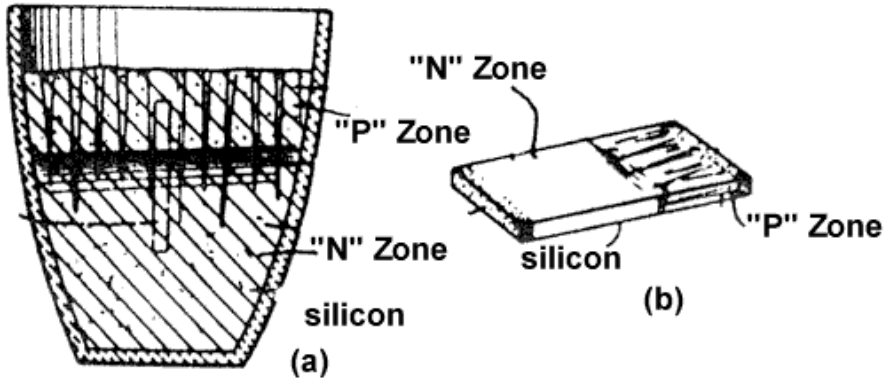


Grondahl, Geiger, Bergmann, Nix... (circa ~1927-40).



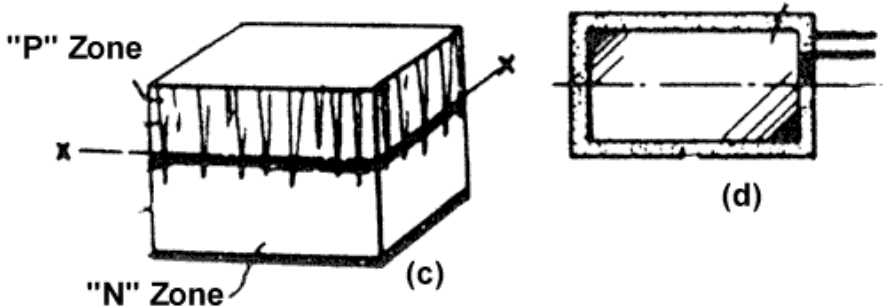
# First silicon cells

Ohl RS. Light-Sensitive Electric Device. U.S. Patent. 1941; 2:402, 602.

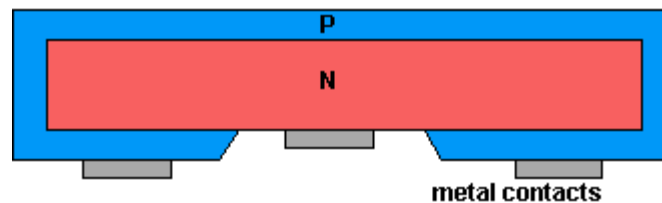


"Natural Si junctions"

$\eta < 0.4\%$



Chapin, Fuller and Pearson (1954)



$\eta = 6\%$

# Si cell efficiency progress

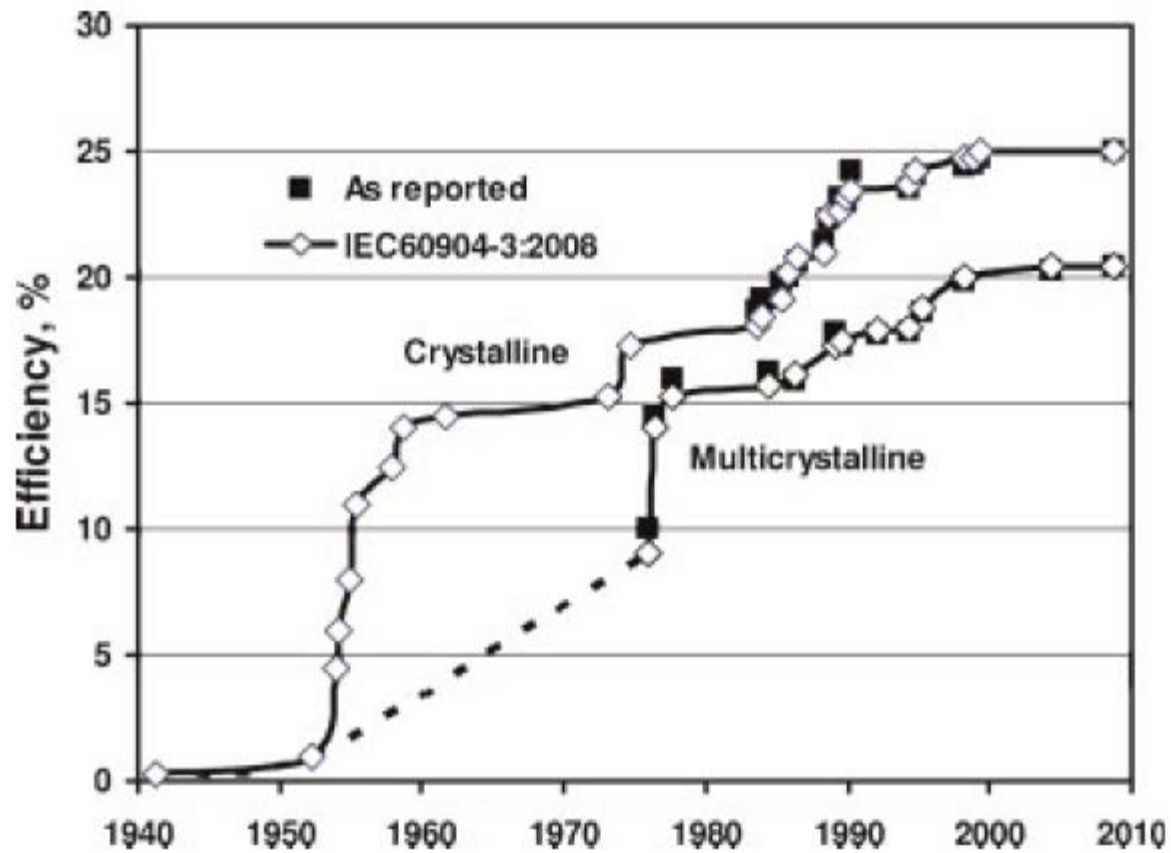
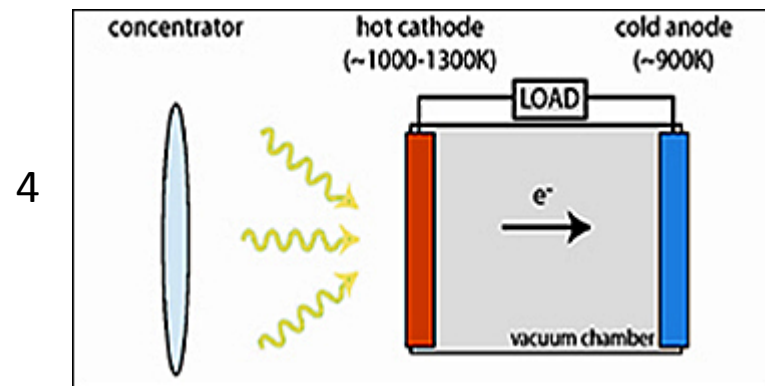
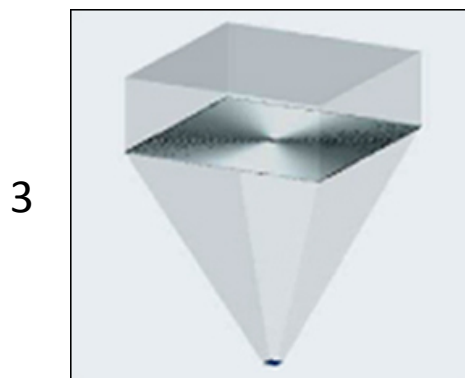
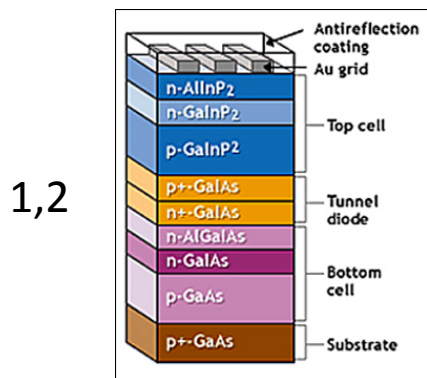


Figure 3. Evolution of crystalline and multicrystalline silicon solar cell efficiency

# Strategies to exceed the SQ limit

	SQ limit assumptions	A strategy to overcome
1	One semiconductor material (excluding doping materials) per solar cell	Use more than one semiconductor material in a cell
2	One P/N junction per solar cell	Use more than one junction in a cell - "tandem cells"
3	The sunlight is not concentrated - a "one sun" source	Sunlight can be concentrated about 500 times using inexpensive lenses
4	All energy is converted to heat from photons greater than the band gap	Combine a PV semiconductor with a heat based technology; Use "quantum dots" to harvest some of the excess photon energy for electricity





# დასკვნები

- ნივთიერებაზე დაცემული სინათლის მხოლოდ ნაწილი შთანთქმება დანარჩენი აირეკლება, გარდაიქმნება სხვა სახის გამოსხივებად ან გატარდება შეუცვლელად.
- შთანთქმული სინათლის ელექტრობად გადასაქცევად საჭიროა ნივთიერების ისეთი სტრუქტურა სადაც ელექტრონები სინათლესთან ურთიერქმედების შედეგად თავისუფლები ხდებიან და შეუძლიათ ნივთიერებაში გადაადგილება ელექტრული ველის ზეგავლენით (ნახევარგამტარები).
- თუ მარტო მზის სპექტრის შთანთქმის შედეგად თავისუფალი ელექტრონების წარმოქმნას მივიღებთ მხედველობაში, სილიციუმი საუკეთესო ნივთიერებაა ფოტოვოლტაიკისათვის.

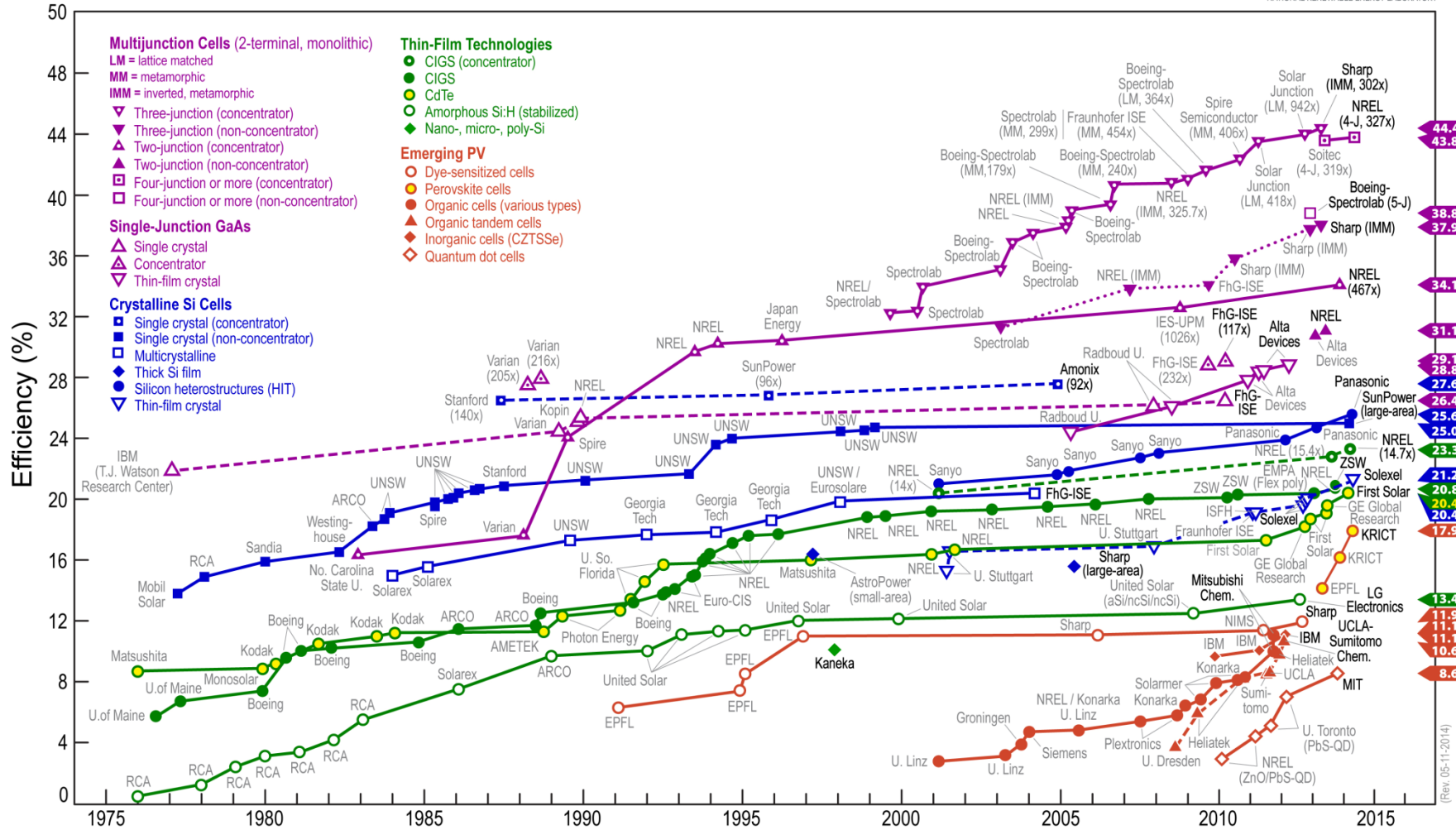
# დასკვნები

- თეორეტიკული ეფექტურობის ლიმიტი (SQ-limit) ერთი ნივთიერების, ერთი -გადასვლის, არაკონცენტრირებული მზის გამოსხივებისა და სითბური დანაკარგების გათვალისწინებით არის 33.7%. SQ-ლიმიტის გაუმჯობესება შესაძლებელია ერთი ან რამდენიმე ზემოაღნიშნული პირობის შეცვლის გზით.
- მაღალი ფოტოვოლტაიკური ეფექტურობის მისაღებად საჭიროა ყველა შესაძლებელი დანაკარგების შემცირება. სინათლის შთანთქმის, დენის მატარებლების გენერაციის, მათი გადაადგილების და შეგროვების დანაკარგების შემცირება წარმოადგენს თანამედროვე კვლევის ერთ-ერთ მთავარ ამოცანას.
- ფოტოვოლტაიკური ელემენტების ეფექტურობა ბოლო 80 წლის განმავლობაში 0.0006%-დან 0.26%-მდე გაიზარდა (600-ჯერ!).

# ლექცია III: ფოტოვოლტაიკური ელემენტები მოდულები, ქსელები.

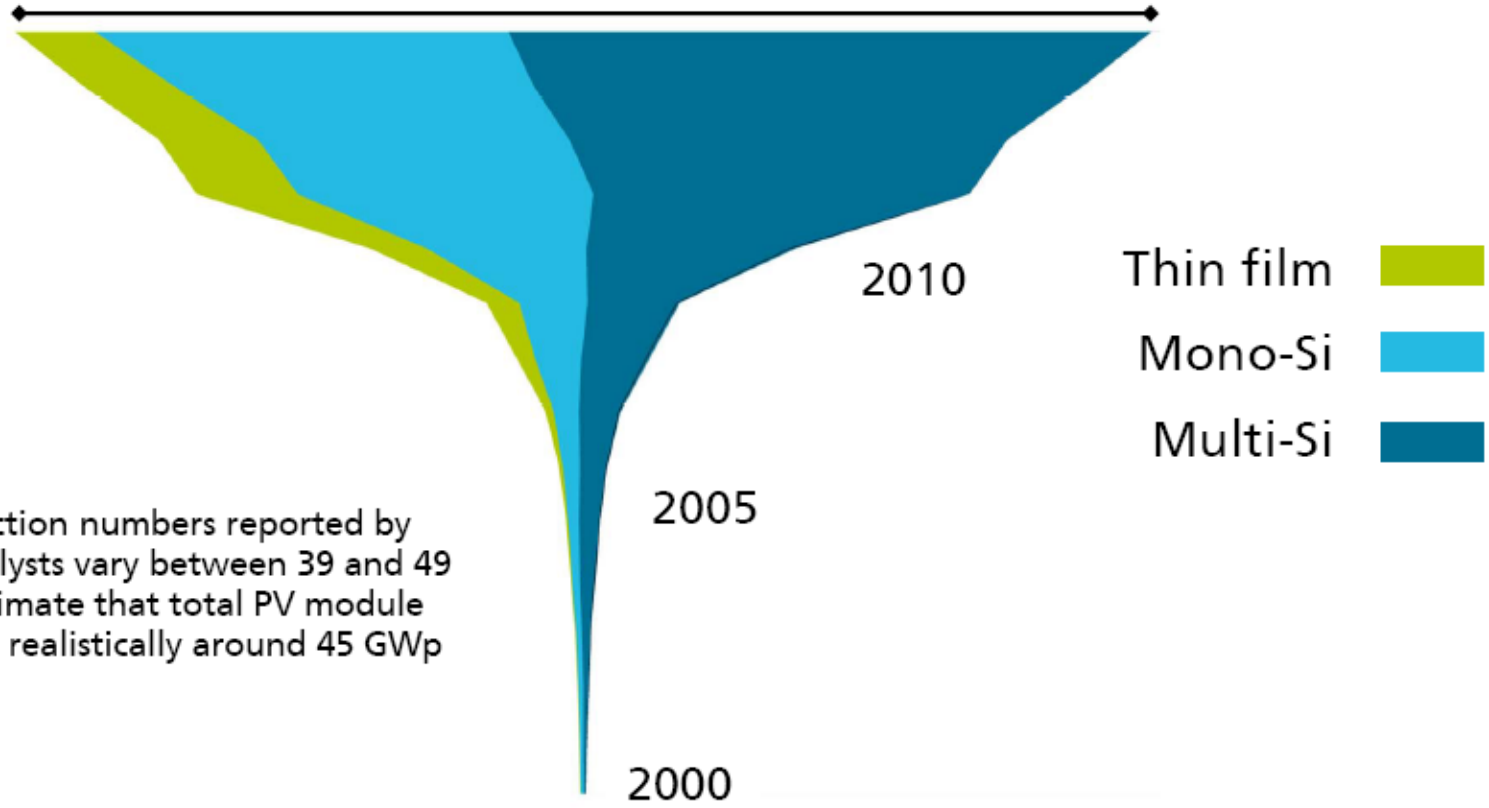
- თანამედროვე ფოტოვოლტაიკური ელემენტები;
- კრისტალური Si ელემენტების წარმოება;
- ფოტოვოლტაიკური მოდულები;
- ქსელების და ელექტრობის აკუმულაციის  
ალტერნატივა;
- განახლებადი ენერჯის წყაროების შედარება;
- ფოტოვოლტაიკის ეკონომიკა და ფოლისოფია;
- დასკვნები და მომავლის პერსპექტივა.

# Progress in research-cell efficiencies



# Annual PV Production by Technology Worldwide (in GWp)

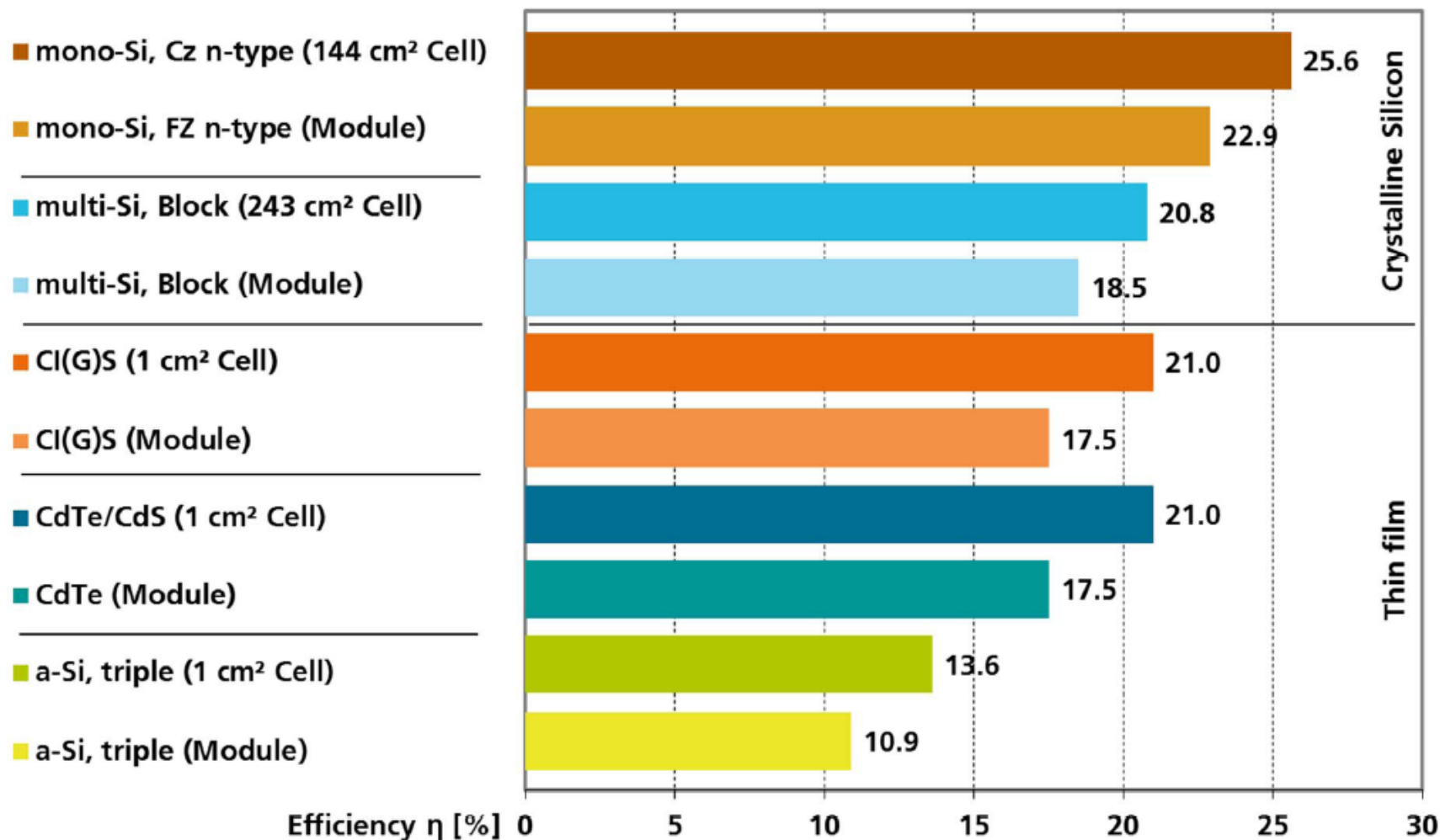
About 47.5\* GWp PV module production in 2014



\*2014 production numbers reported by different analysts vary between 39 and 49 GWp. We estimate that total PV module production is realistically around 45 GWp for 2014.

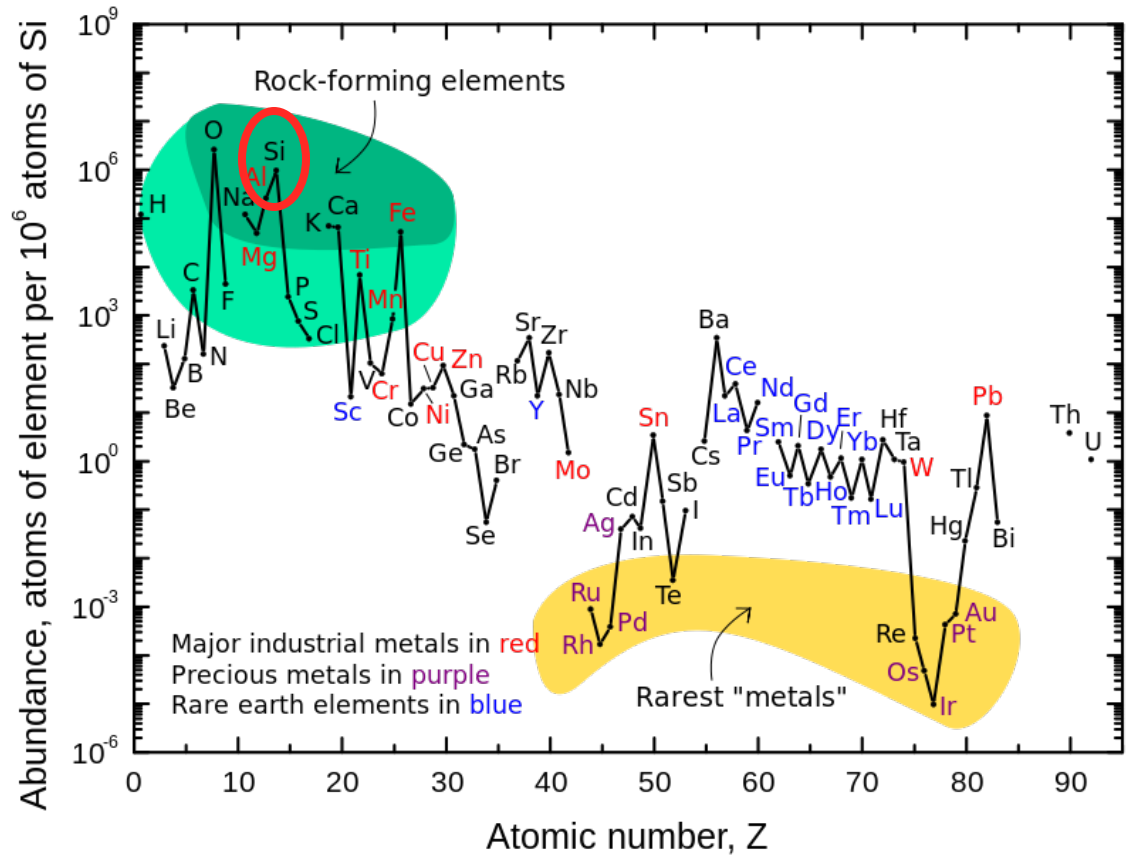
Data: from 2000 to 2010: Navigant; from 2011: IHS (Mono-/Multi- proportion: Paula Mints). Graph: PSE AG 2015

# Efficiency Comparison of Technologies: Best Lab Cells vs. Best Lab Modules

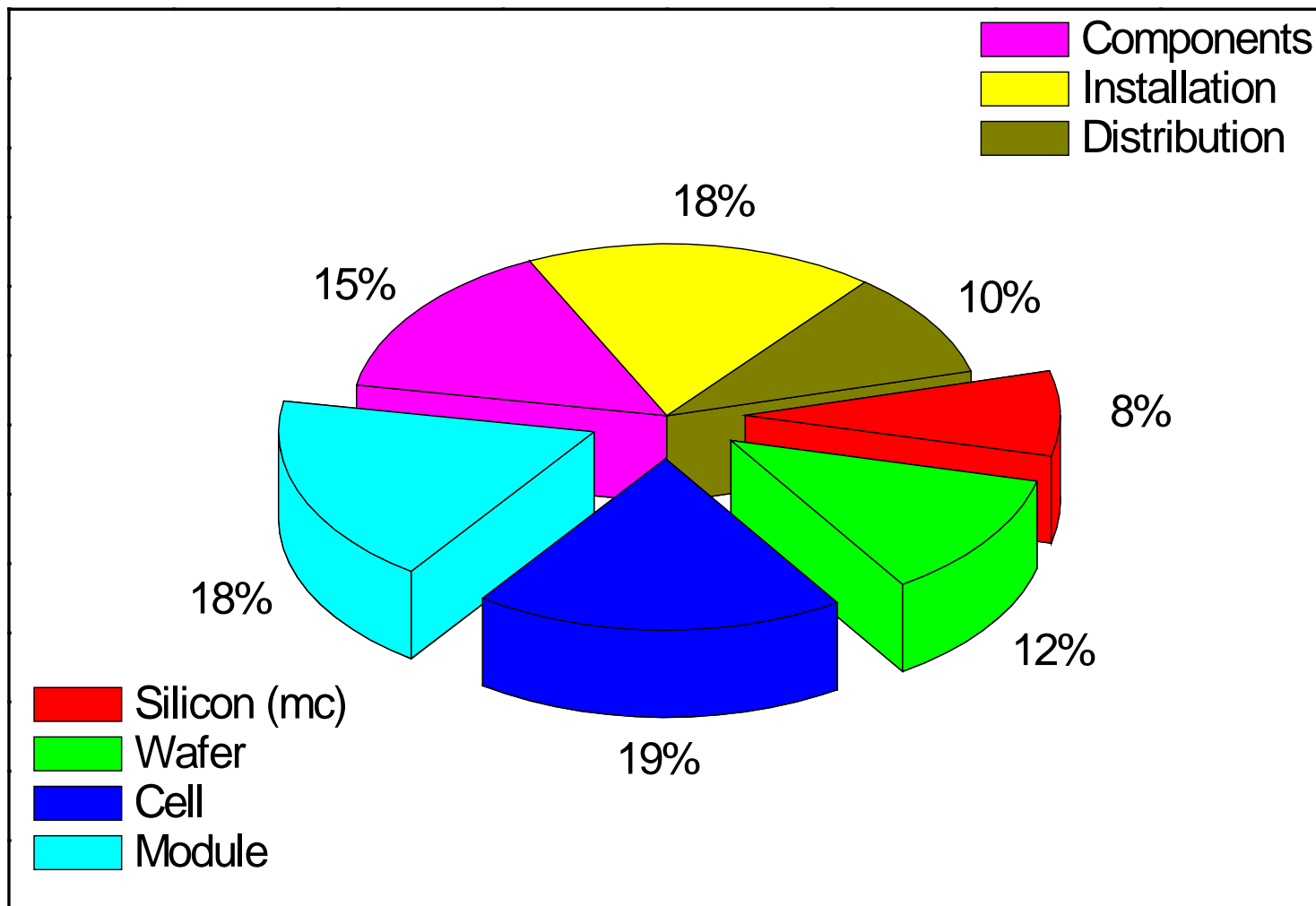


# Why Si

- Second most abundant element on the earth after oxygen;
- Non toxic;
- Well developed Si industry and technology;
- Fast forming  $\text{SiO}_2$  protective layer on the open Si surface and its passivation properties;
- Suitable value for the bandgap;
- High value of real refraction index;
- Low solubility limits for the most of the elements; Candidate for new mass standard!



# Cost distribution for PV systems, an estimate

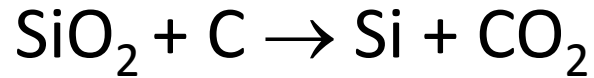




# Refining silicon

1. Beach sand, Quartz rock

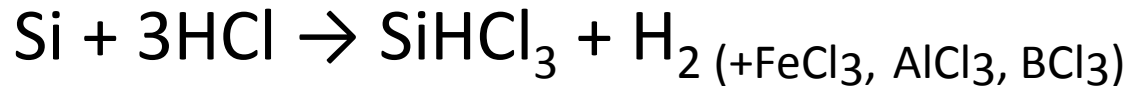
1500-2000°C, electrode arc furnace



MG-Si, 98% pure (B, P, Alkali, earth, transition metals, carbon...)

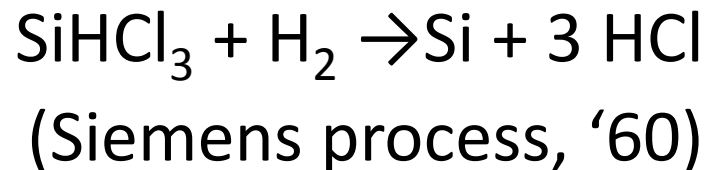
2. Powdered MG-Si

300°C, fluidized bed reactor



The resulting  $\text{SiHCl}_3$  now has impurities of less than 1 ppba.

3. The pure  $\text{SiHCl}_3$  is reacted with H at 1100°C for ~200 – 300 hours

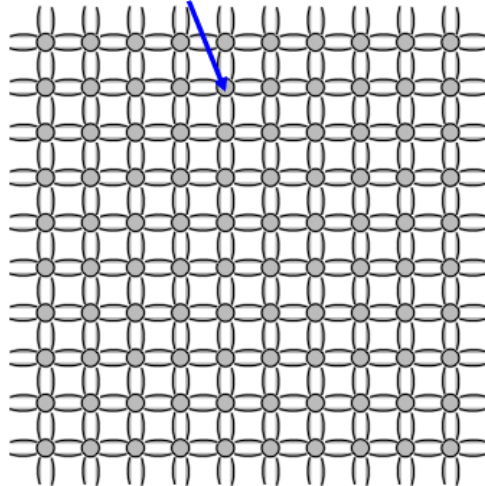


# Types of silicon

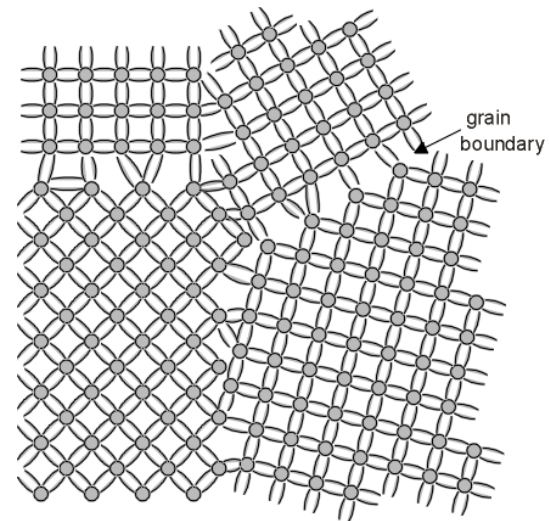
Descriptor	Symbol	Grain Size	Common Growth Techniques
Single crystal	c-Si	> 10cm	Czochralski (Cz) Float zone (FZ)
Multicrystalline	mc-Si	1mm-10cm	Cast, sheet, ribbon
Polycrystalline	pc-Si	1 $\mu$ m-1mm	Chemical-vapour deposition
Microcrystalline	$\mu$ c-Si	< 1 $\mu$ m	Plasma deposition
Amorphous	a-Si	-	Plasma deposition

Each silicon atom is bonded to four neighbouring atoms.

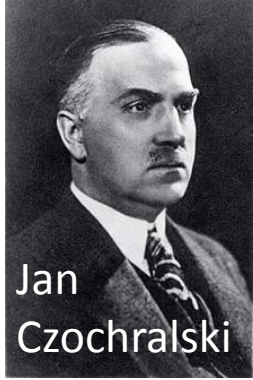
c-Si



mc-Si



# Czochralski growth process

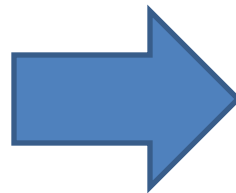


Jan Czochralski

~1916



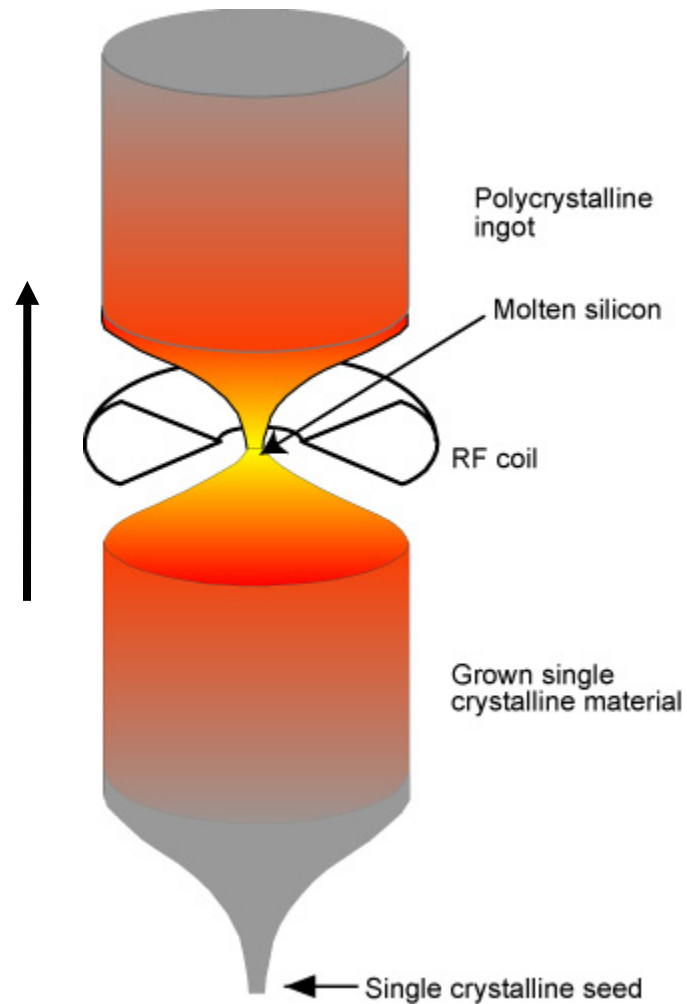
Poly Si



Diameter up to 45 cm

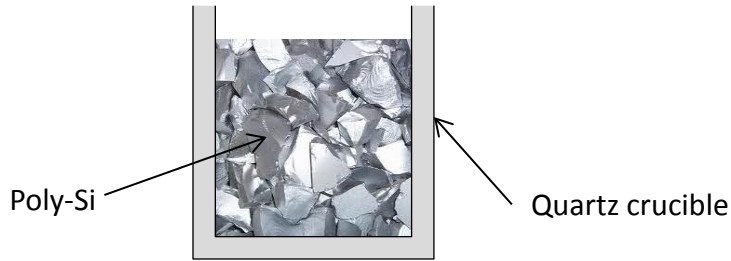
# Floating zone growth process

William Gardner Pfann  
and Henry Theuerer  
Bell Labs, ~1955

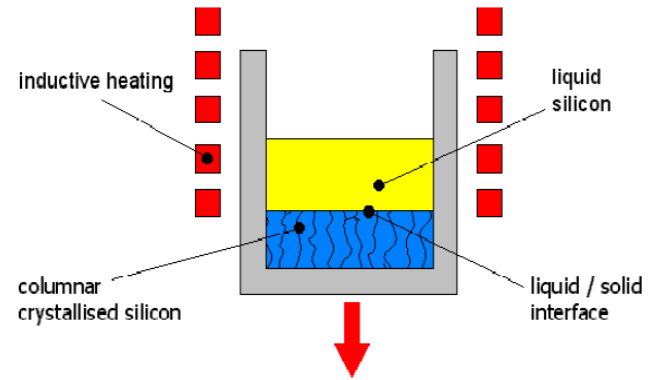


Diameter up to 20 cm

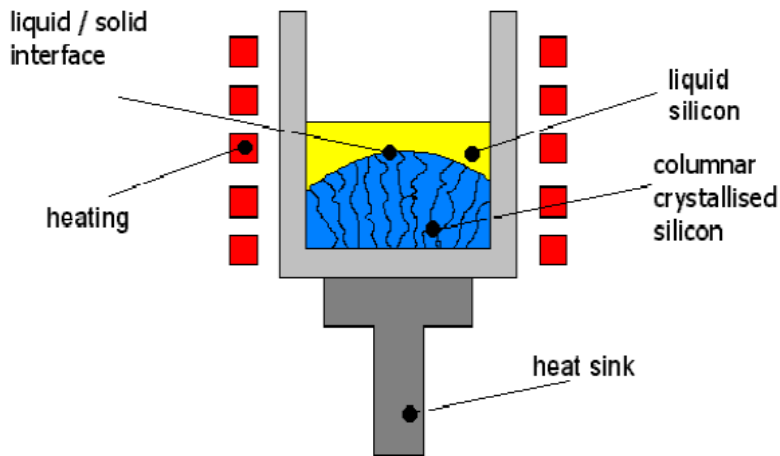
# mc-Si fabrication



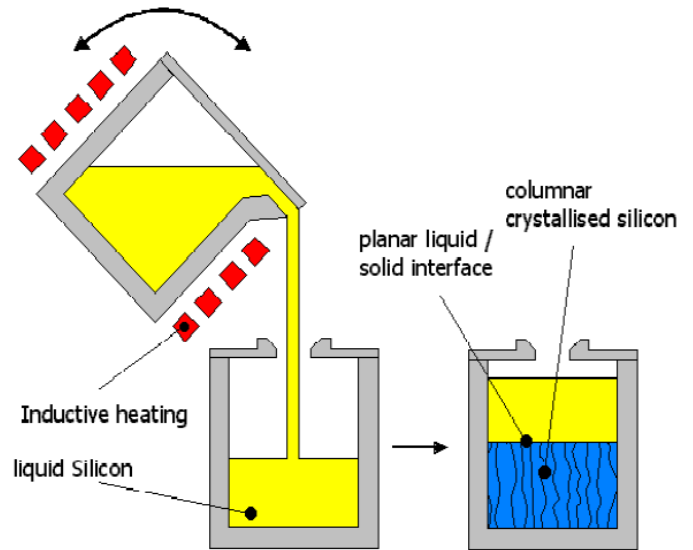
## Bridgman solidification



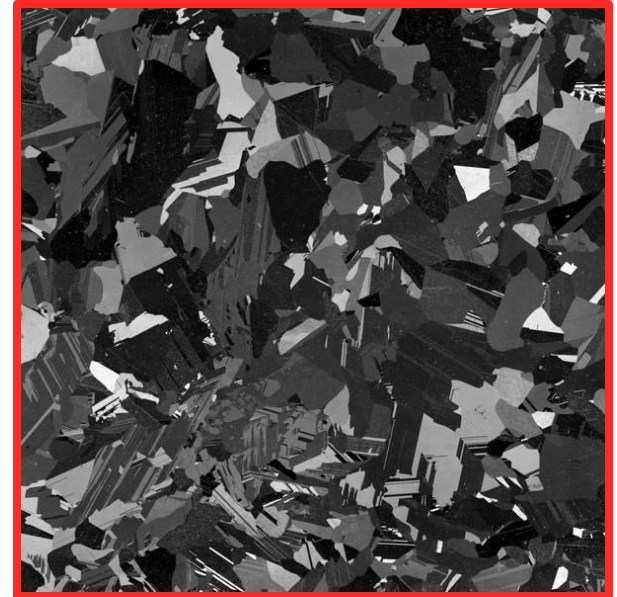
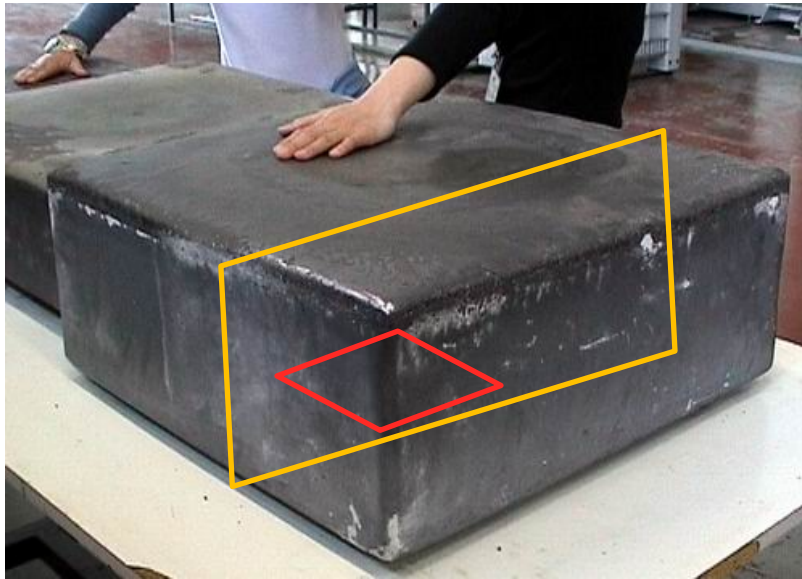
## Heat exchange method (HEM)



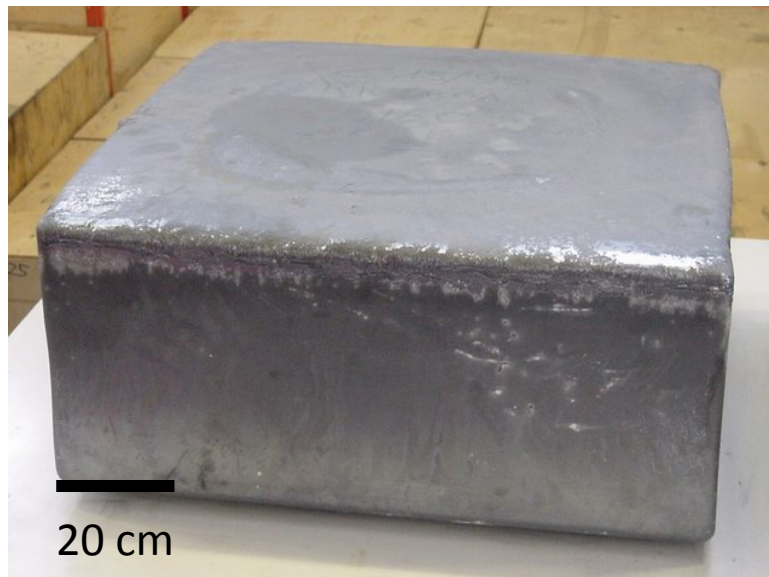
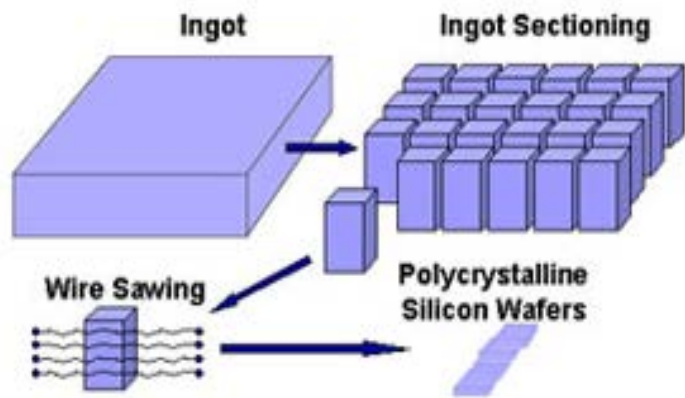
## Casting of silicon blocks



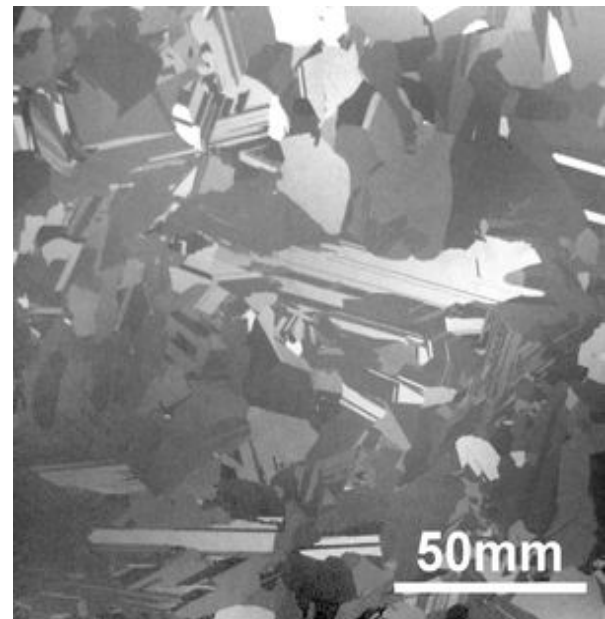
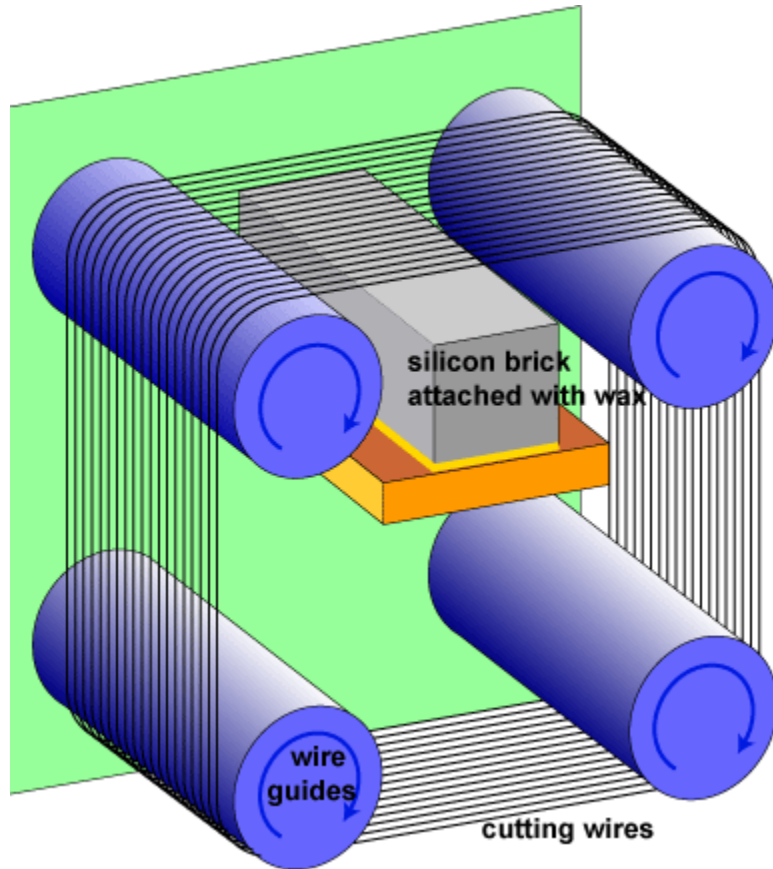
# mc-Si directional solidification



# Wafering



# Wafering





# Screen Printed Solar Cells

1. Texturing and Cleaning



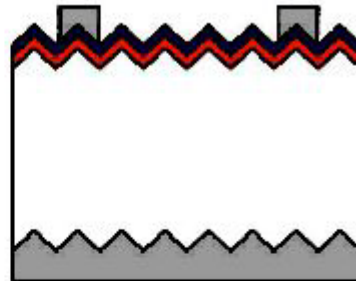
2. Phosphorus Diffusion



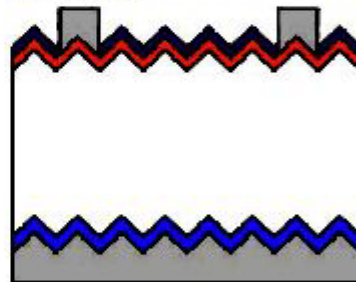
3. SiNx Deposition



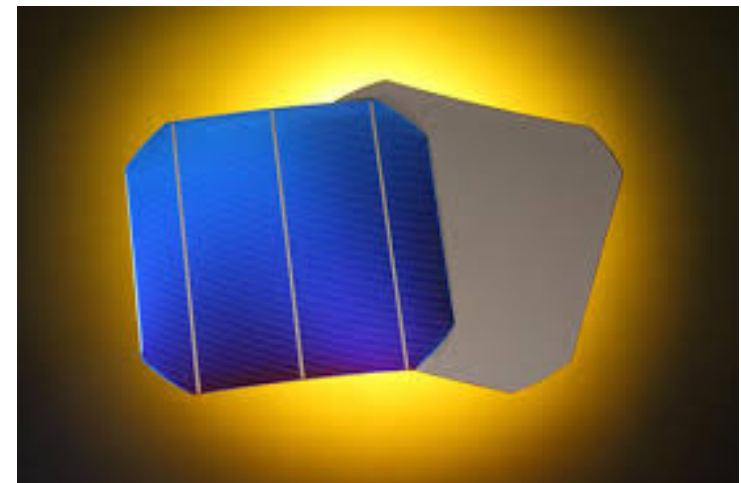
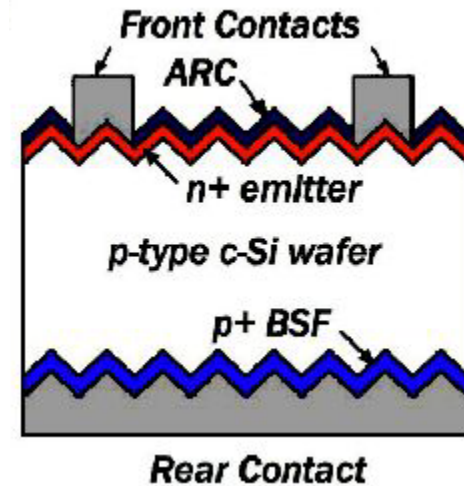
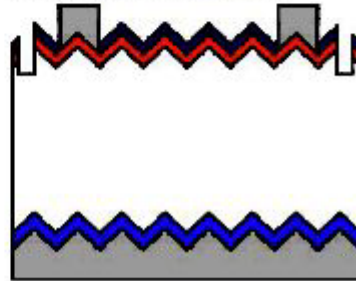
4. Al and Ag Screen Printing



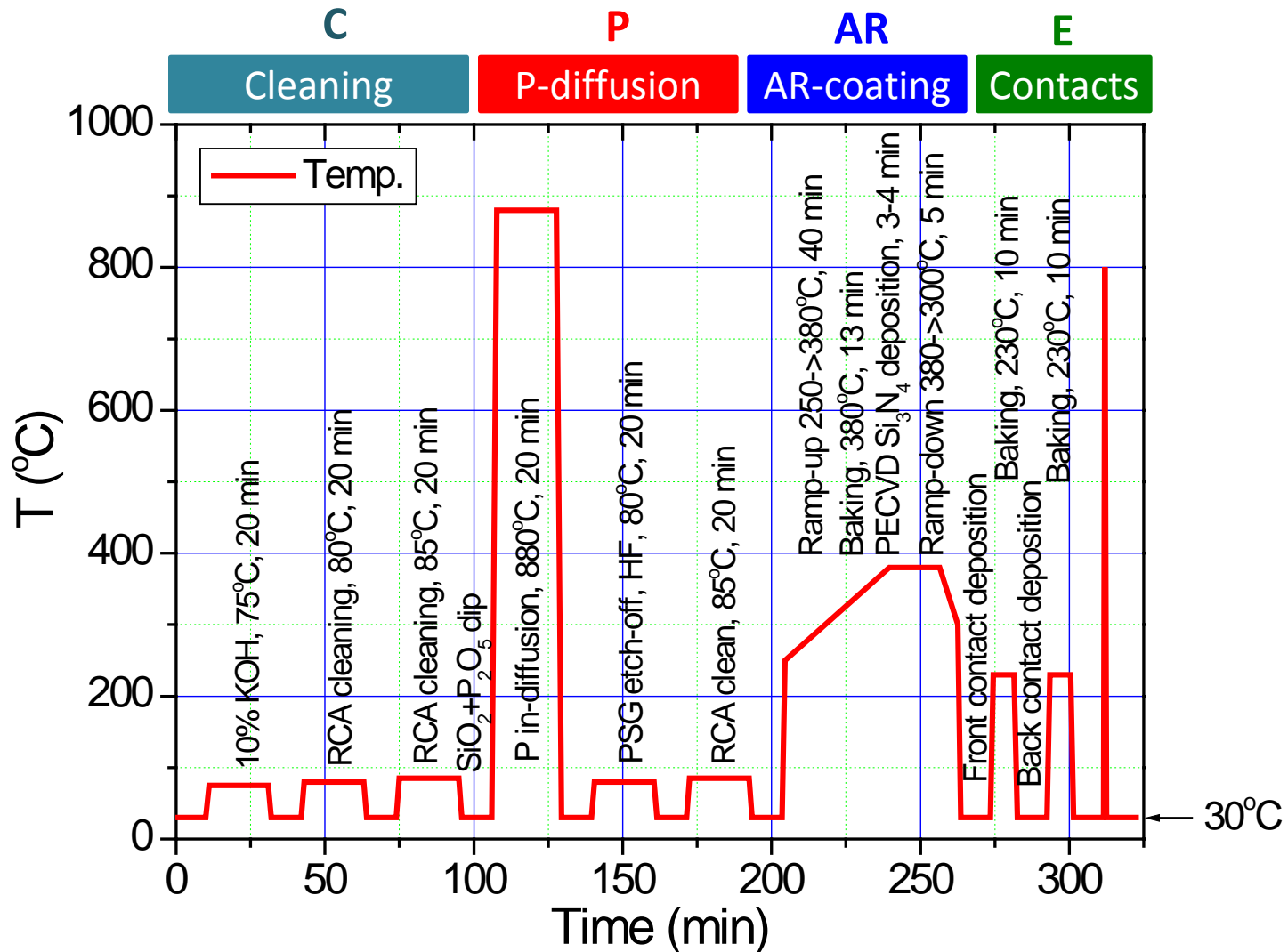
5. Firing



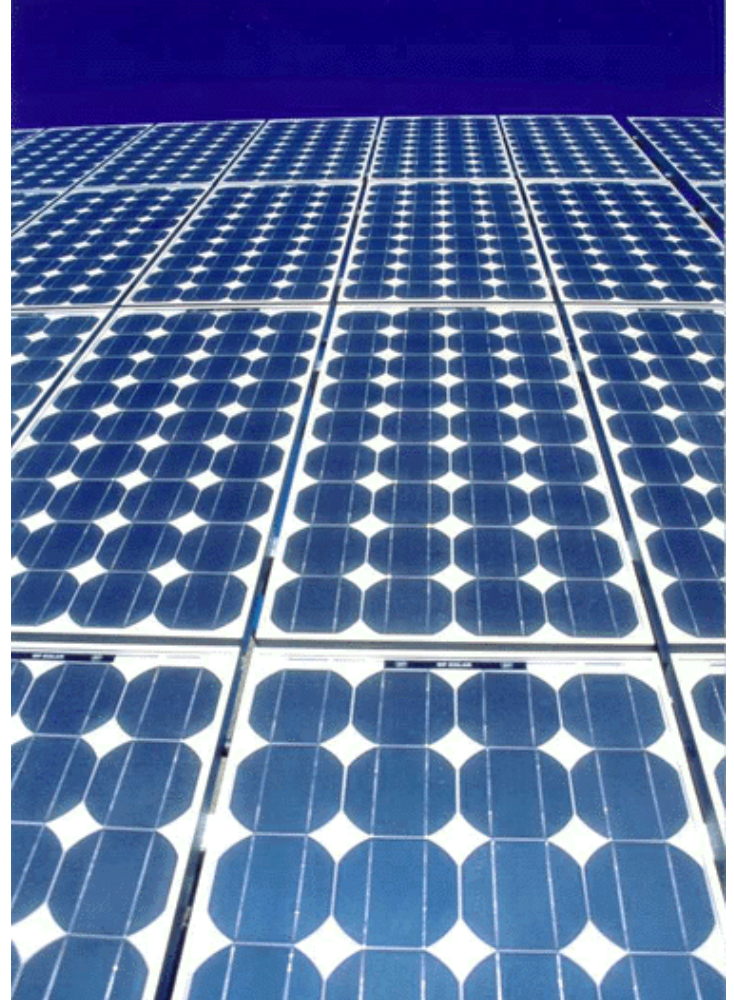
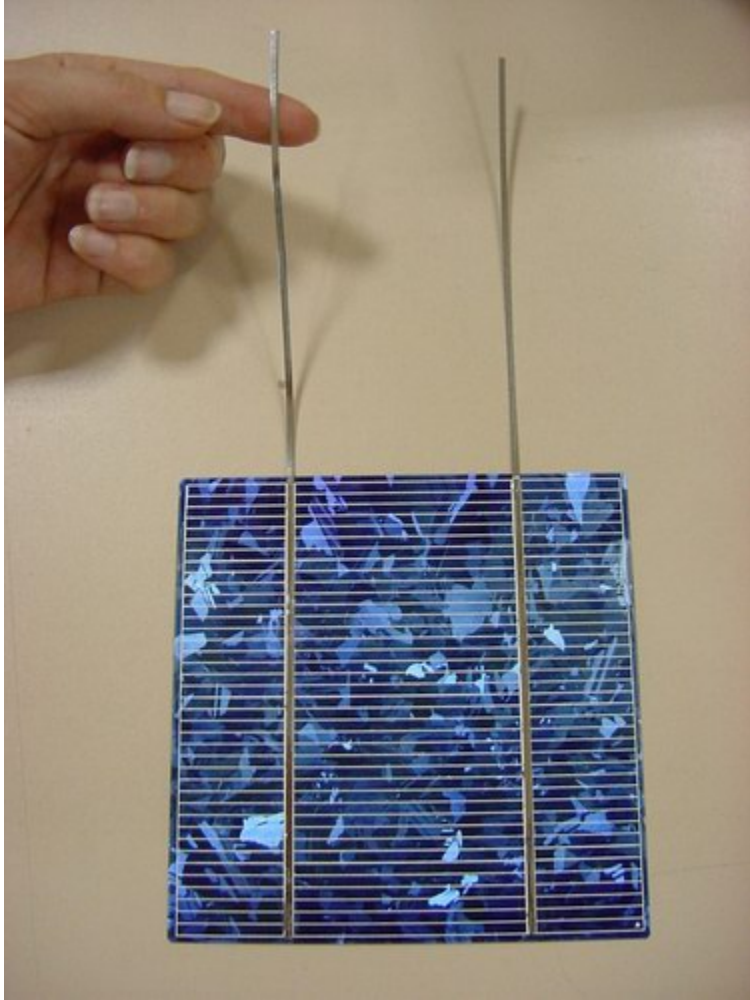
6. Edge Isolation



# Solar cell fabrication process

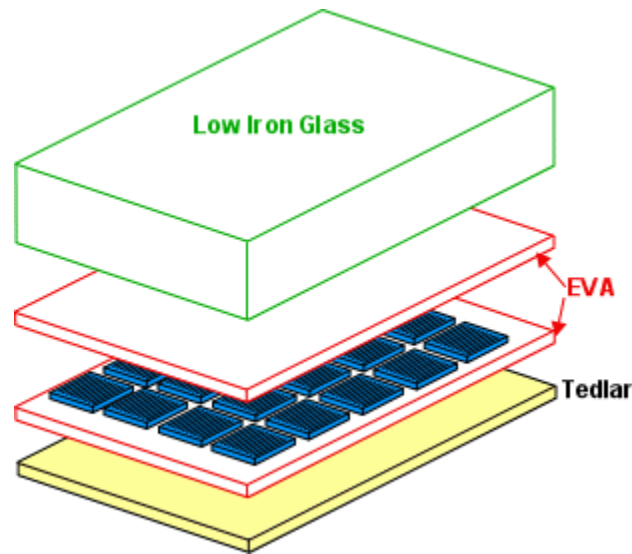
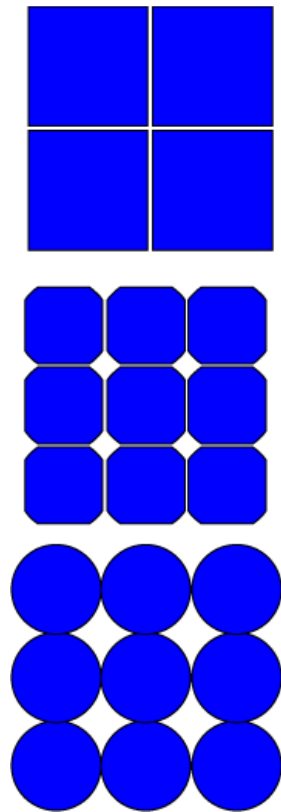


# From cells to modules

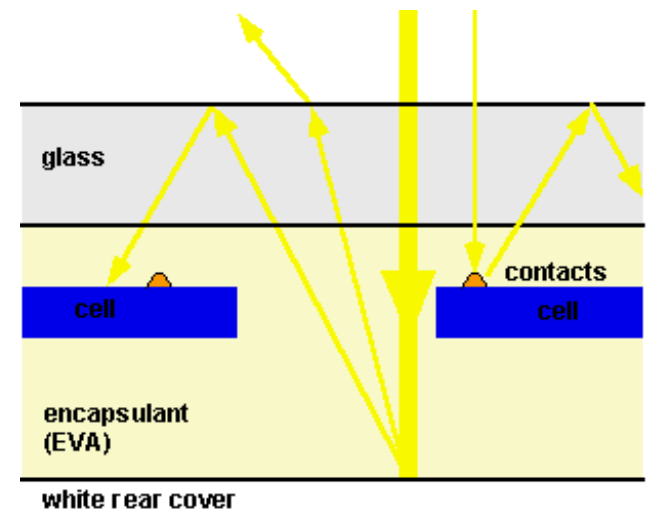


# Module structure

A PV module consists of a number of interconnected closely packed solar cells encapsulated into a single, long-lasting, stable unit. Module lifetimes and warranties on bulk silicon PV modules are over 20 years. A typical warranty will guarantee that the module produces 90% of its rated output for the first 10 years and 80% of its rated output up to 25 years.

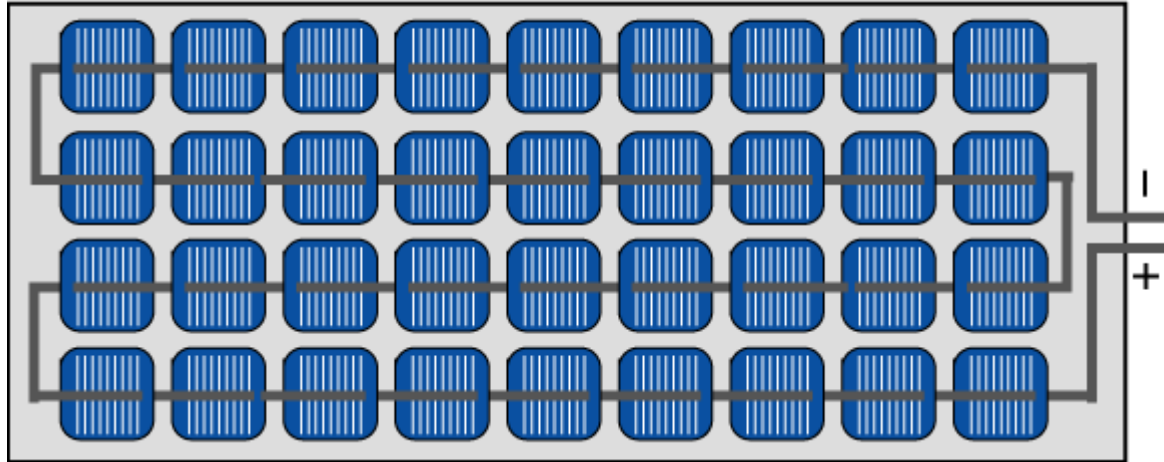


\*)EVA - ethyl vinyl acetate



# Module circuit design

A typical module has 36 cells connected in series

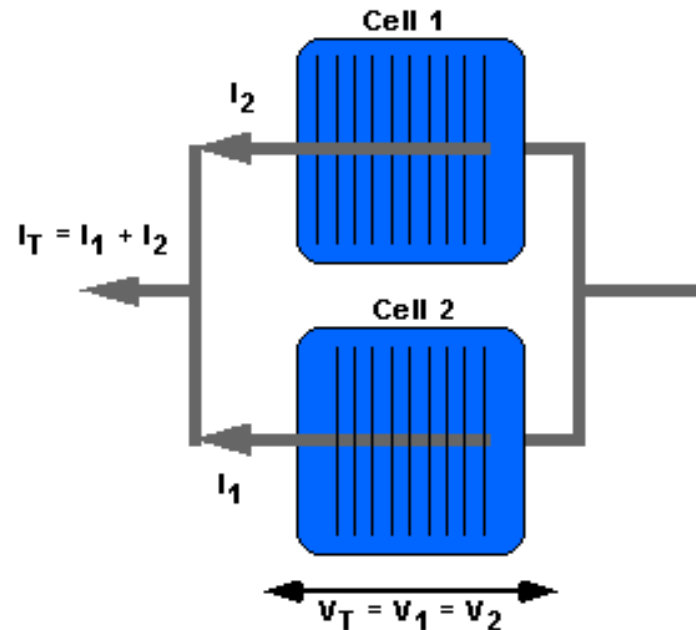
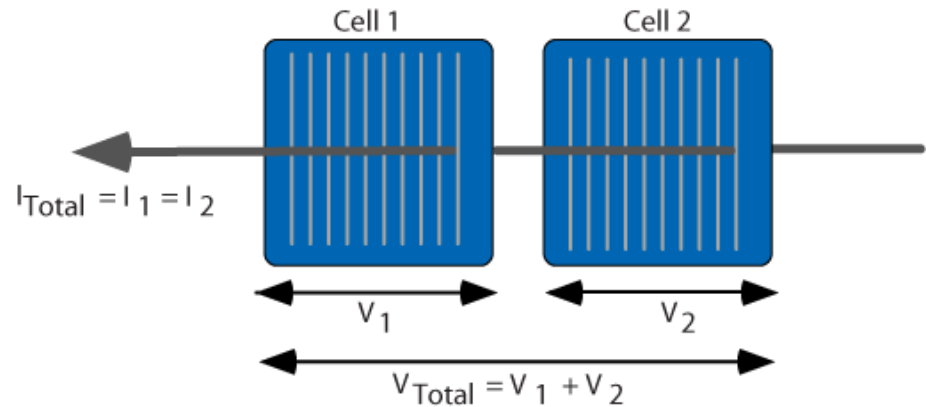
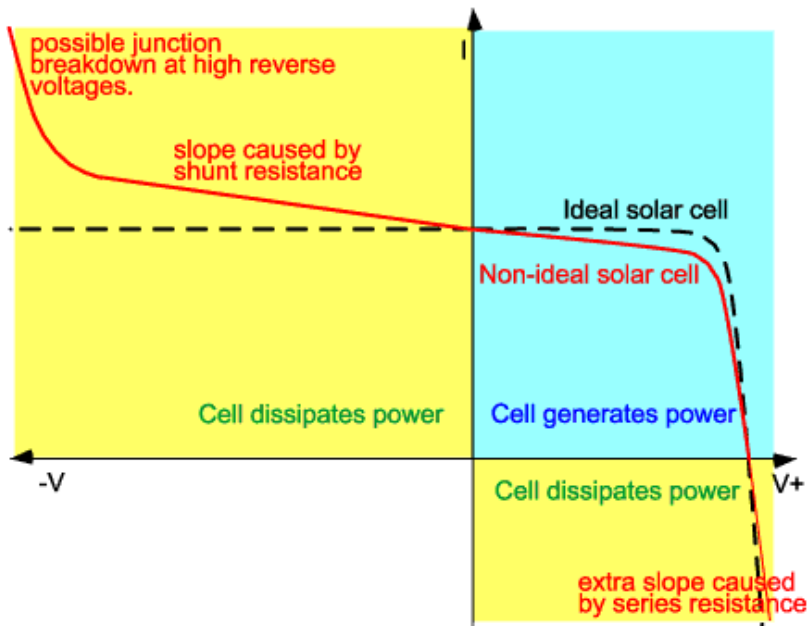


An individual silicon solar cell has a voltage of just under 0.6V under 25 °C and AM1.5 illumination:  $0.6 \times 36 = 21.6$  V.

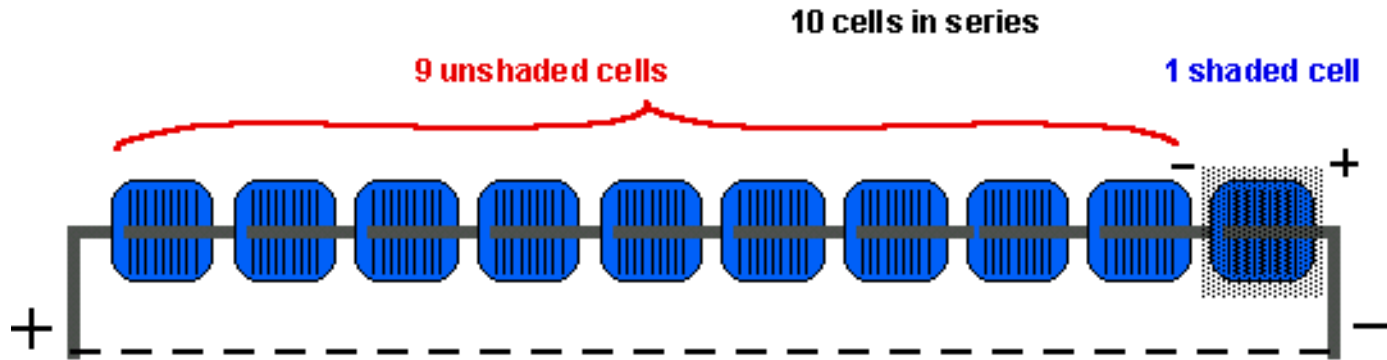
$$I_T = M \cdot I_L - M \cdot I_0 \left[ \exp \left( \frac{q V_T}{n k T} \right) - 1 \right]$$

where: N is the number of cells in series; M is the number of cells in parallel;  $I_T$  is the total current from the circuit;  $V_T$  is the total voltage from the circuit;  $I_0$  is the saturation current from a single solar cell;  $I_L$  is the short-circuit current from a single solar cell; n is the ideality factor of a single solar cell; and q, k, and T are constants.

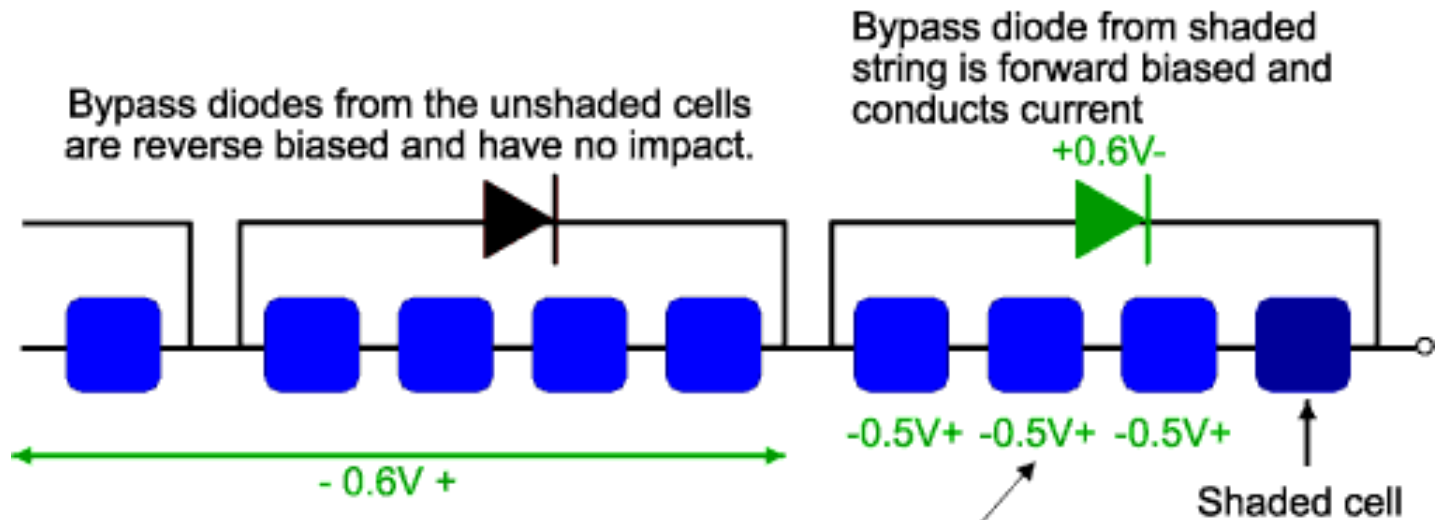
# Mismatch effects



# Shading effects and bypass diodes

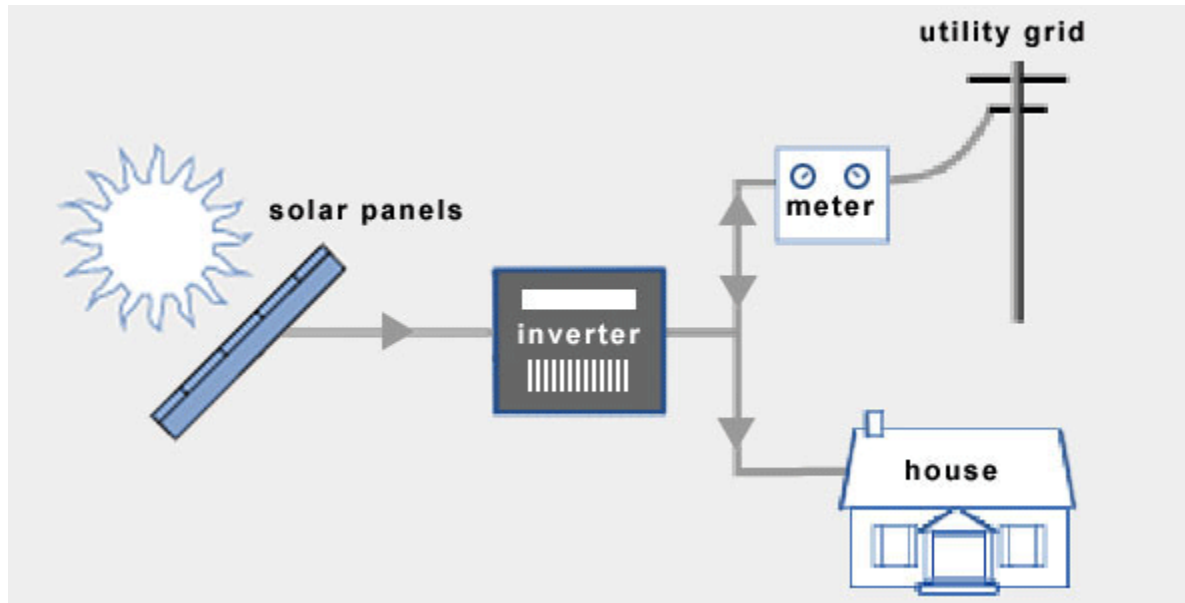


If the terminals of the module are connected in series ( $I_{SC}$ ), the power from the unshaded cells is dissipated across the shaded cell.

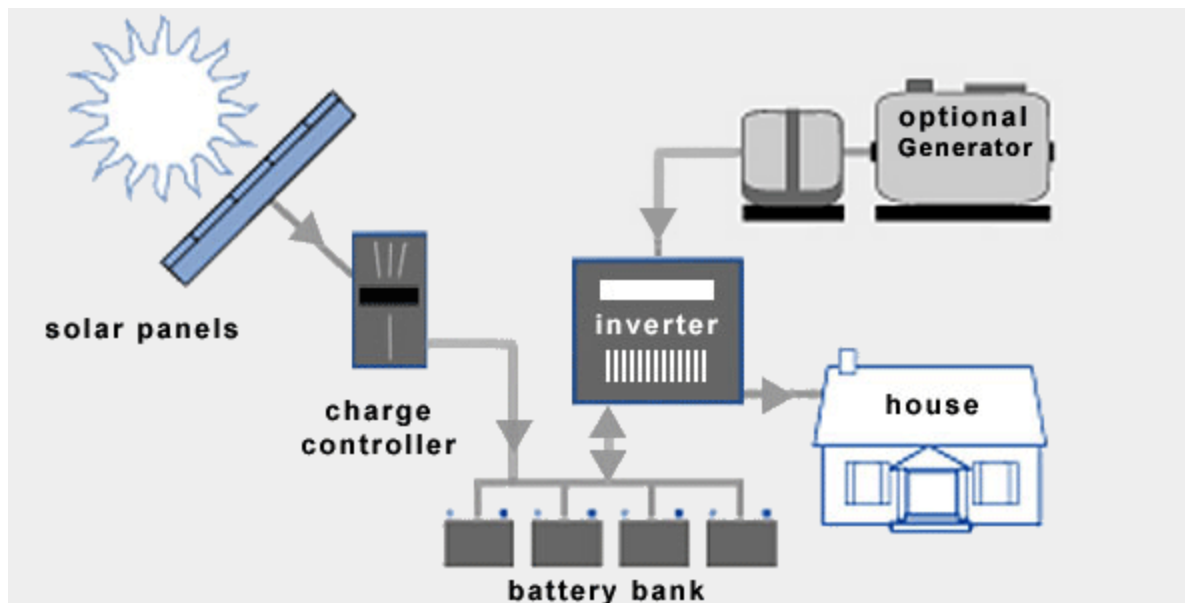


Current from string of cells is limited by lowest current cell. If some cells are shaded, then the extra current from the good cells in the string forward biased these cells.

# On-grid vs. off-grid alternative



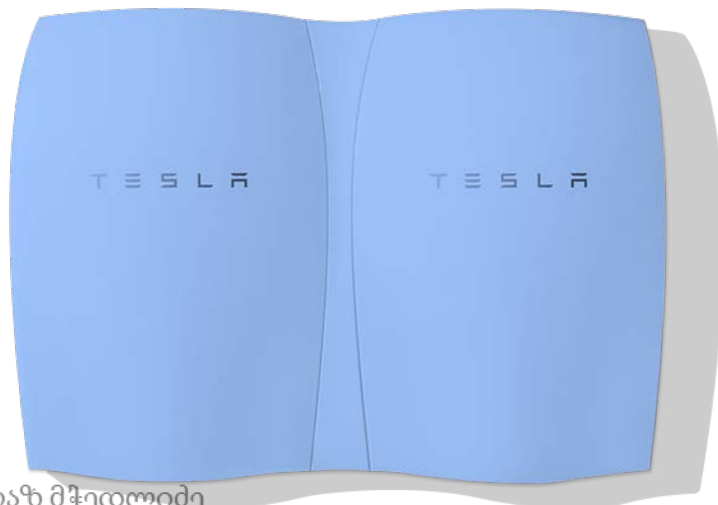
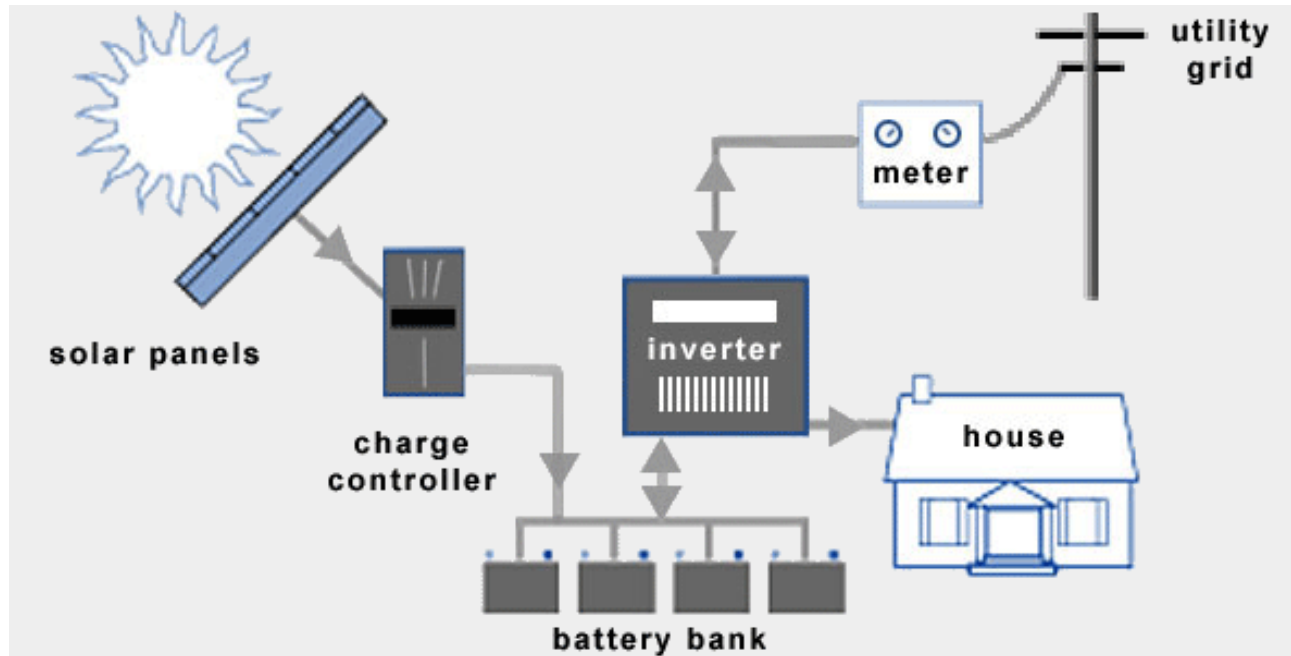
On-grid



Off-grid



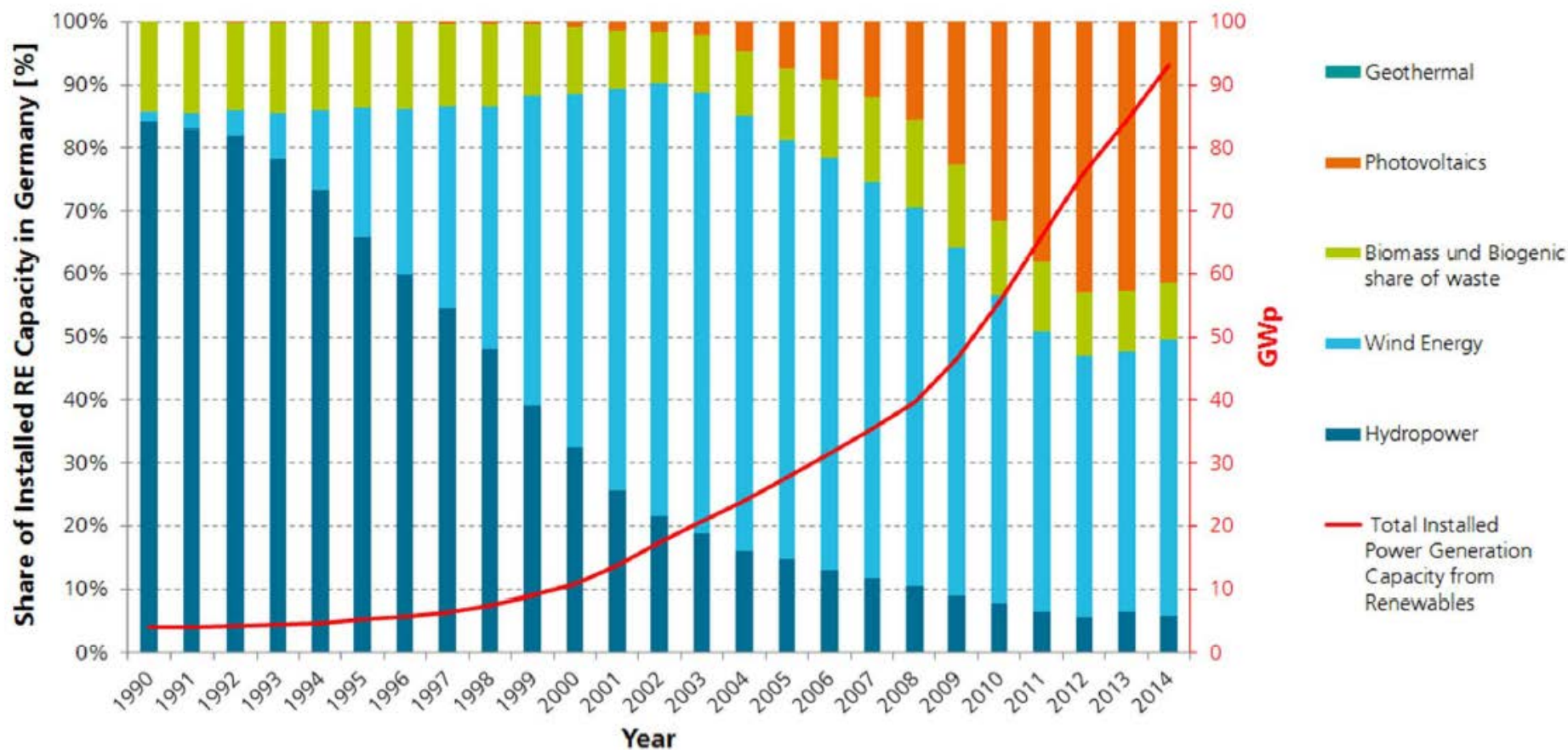
# Hybrid solar system



## TESLA

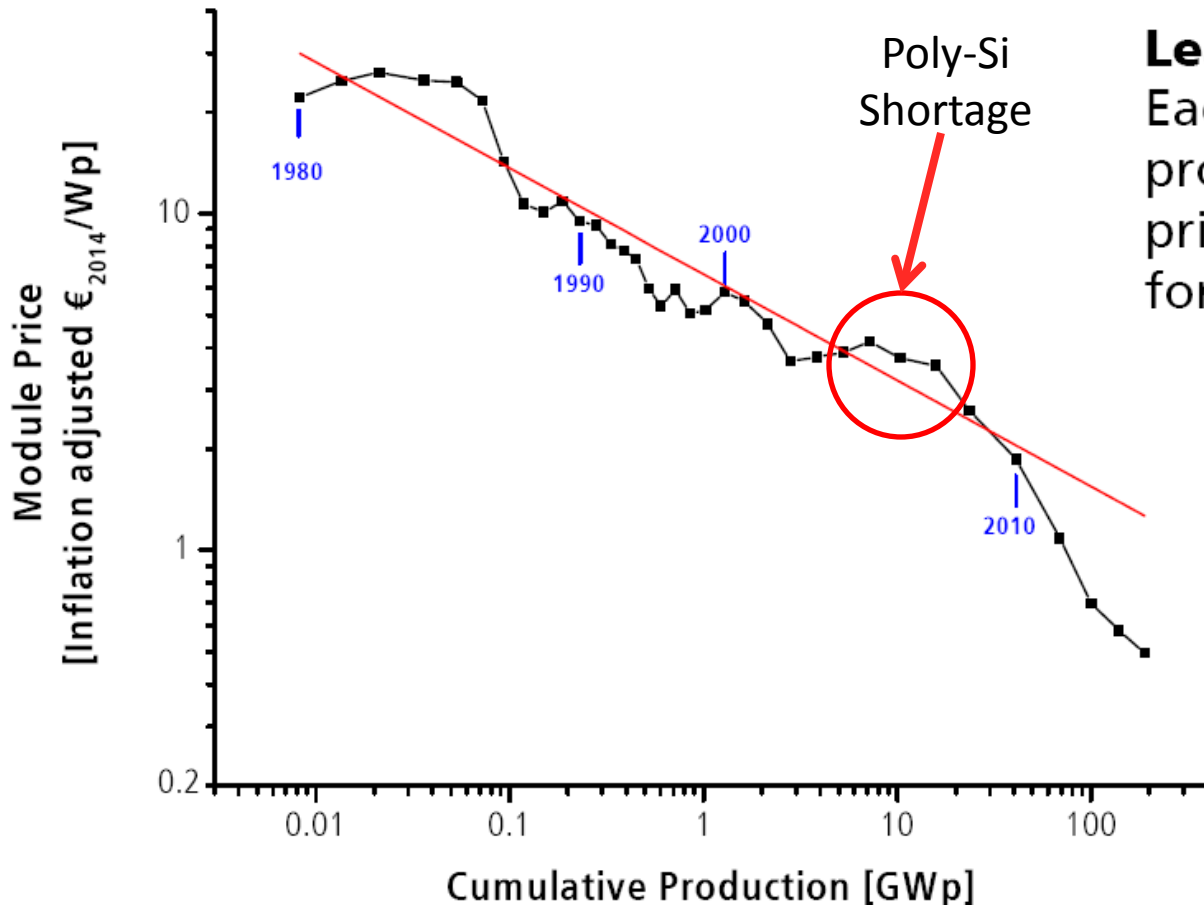
Each Powerwall has a 7 kWh energy storage capacity, sufficient to power most homes during the evening using electricity generated by solar panels during the day.

# Electrical capacity of renewable energy sources for Germany



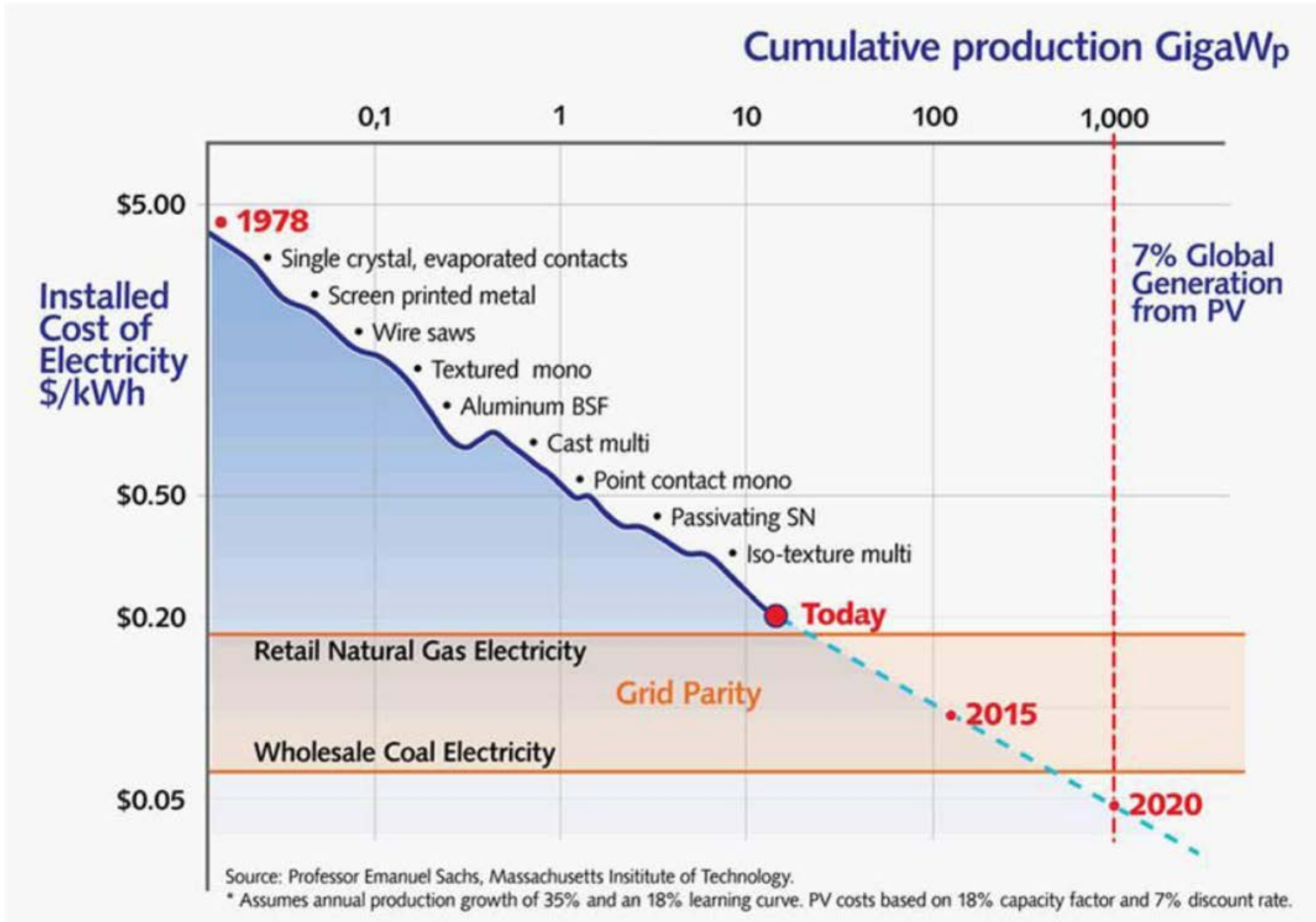
In 2014 about 28% of the electricity in Germany was generated by renewable energy (RE) sources according to BMWi.

# Price Learning Curve



**Learning Rate:**  
Each time the cumulative production doubled, the price went down by 19.6% for the last 34 years.

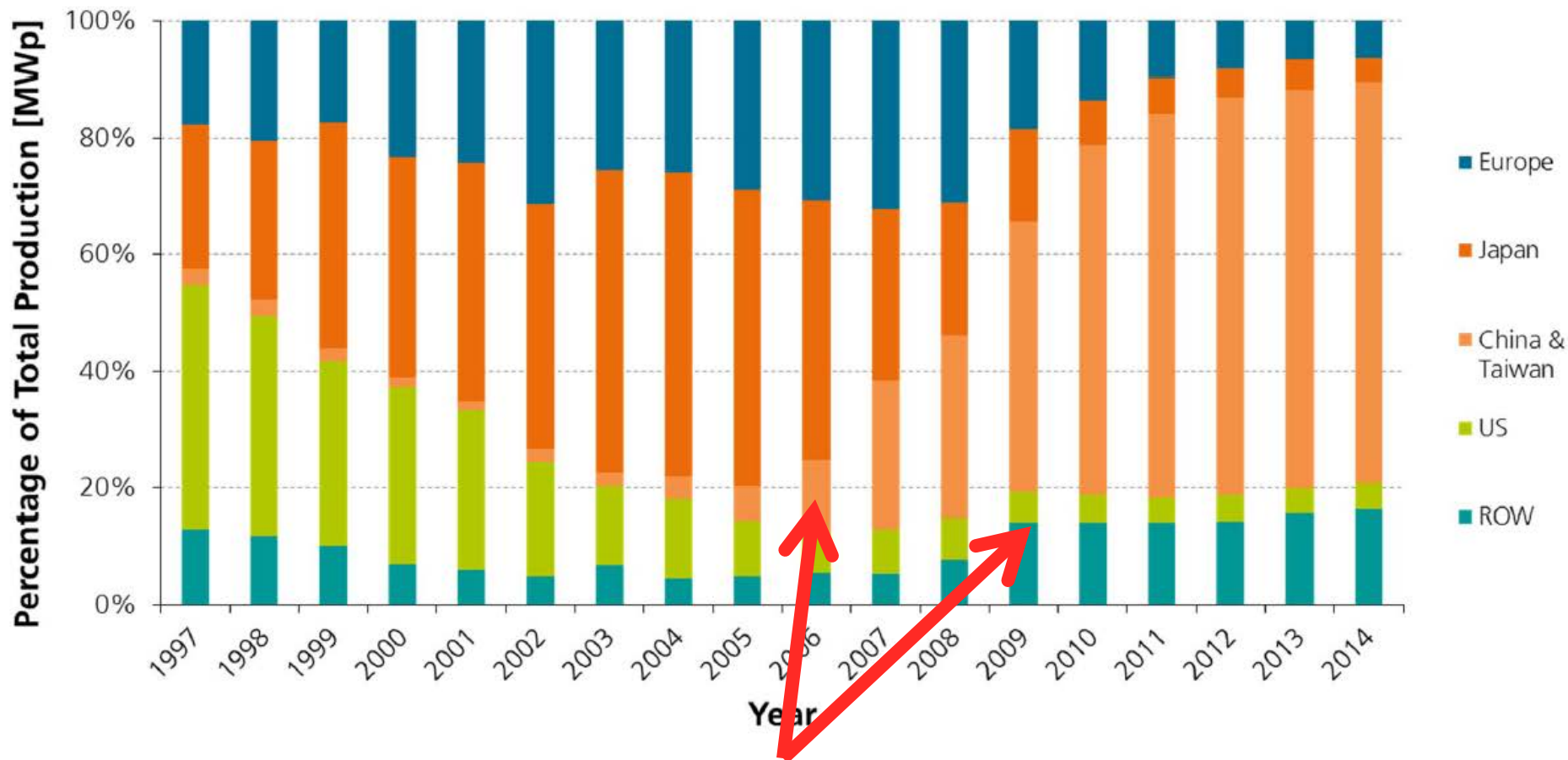
# Innovations pushing the price down



<http://paxonbothouses.blogspot.de/2014/04/has-grid-parity-arrived.html>

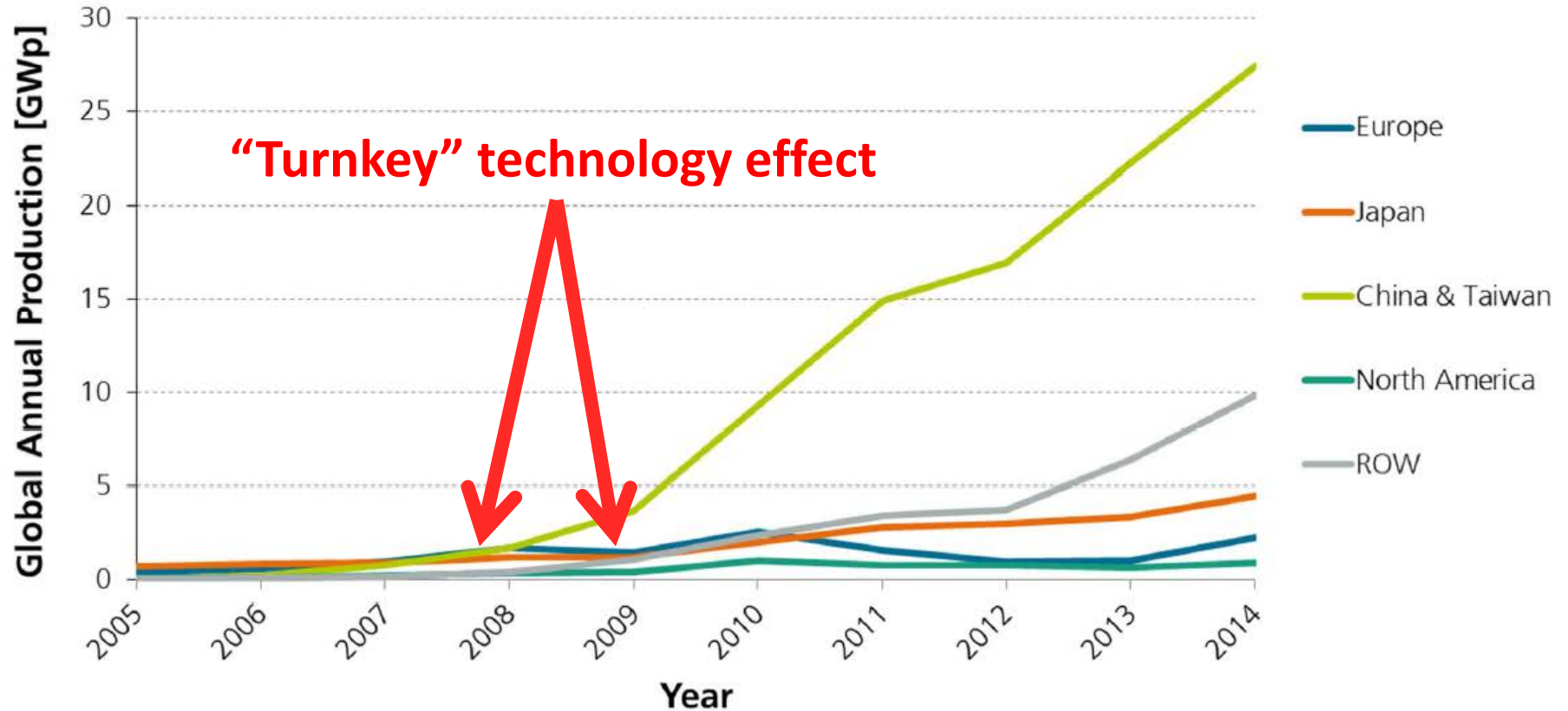
<http://www.treehugger.com/natural-sciences/15-photovoltaics-solar-power-innovations-you-must-see.html>

# PV Module Production by Region 1997-2014

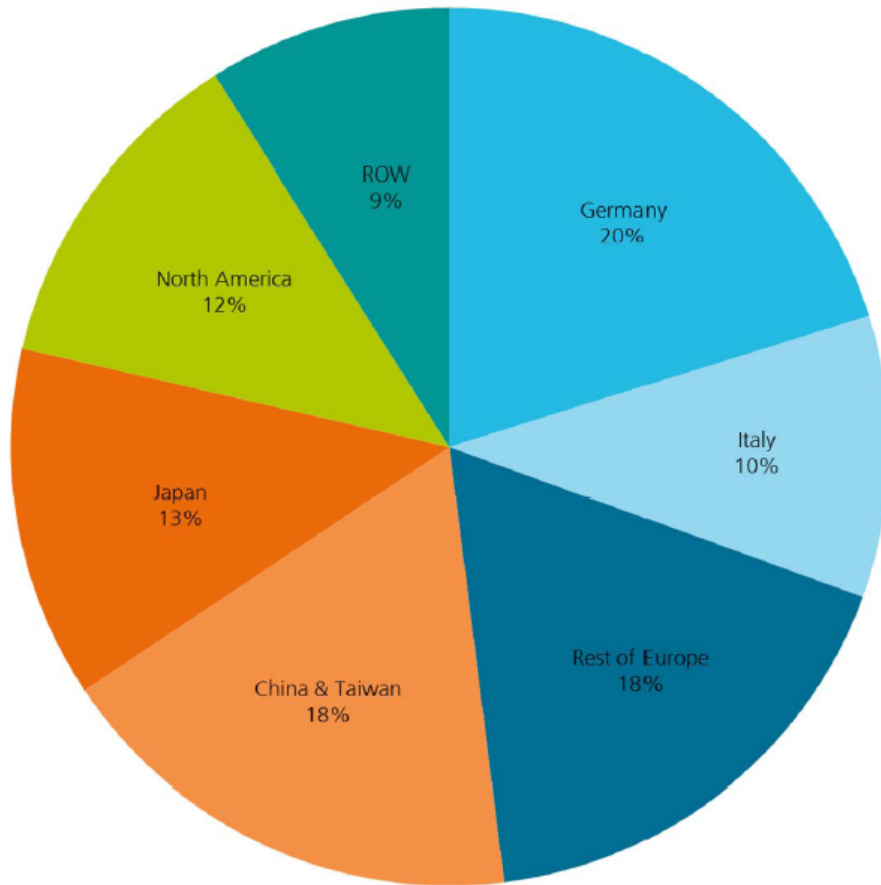


**“Turnkey” technology effect**

# PV Industry Production by Region



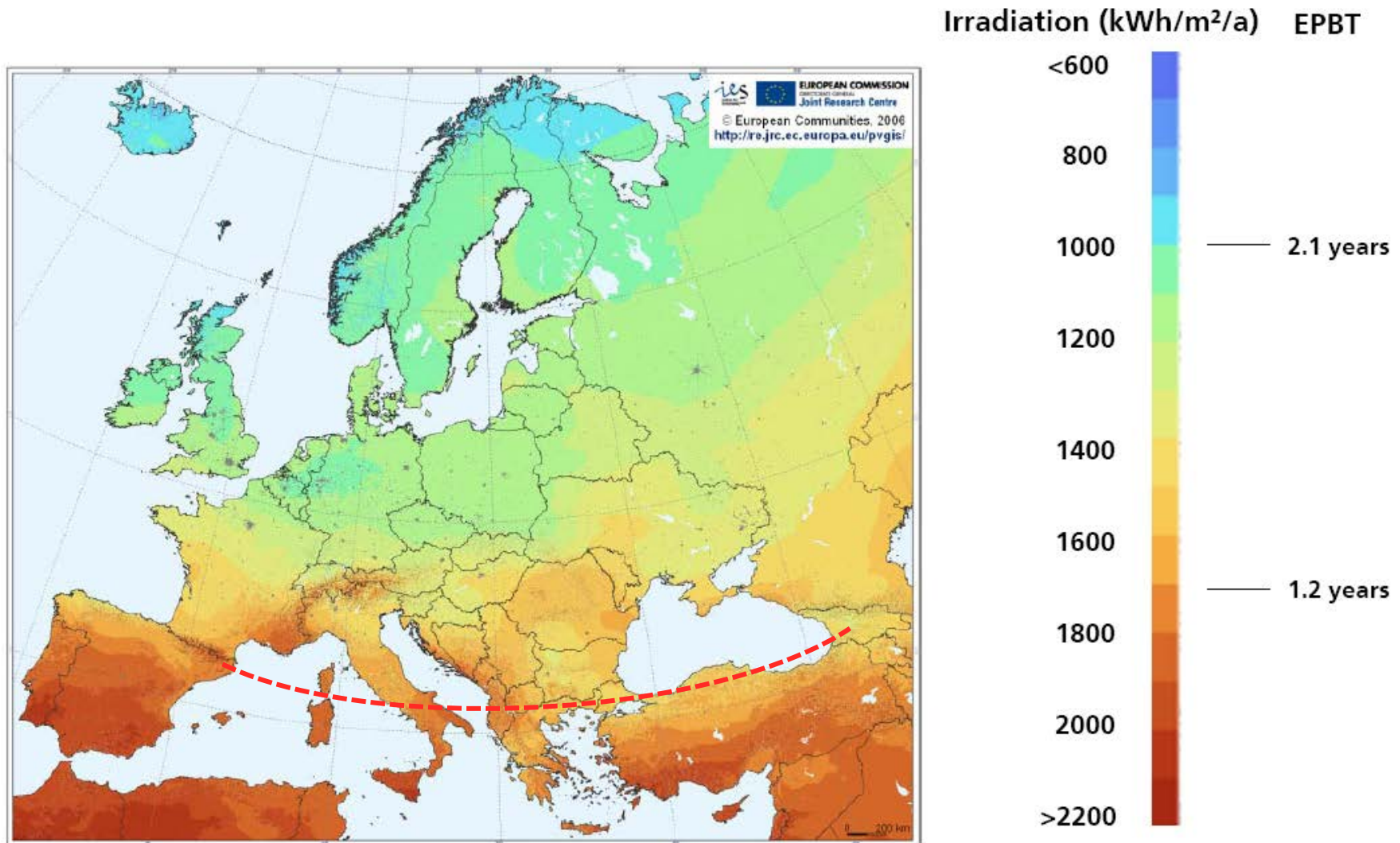
# Global Cumulative PV Installation by Region Status 2014



The total cumulative installations amounted to 183 GWp at the end 2014.

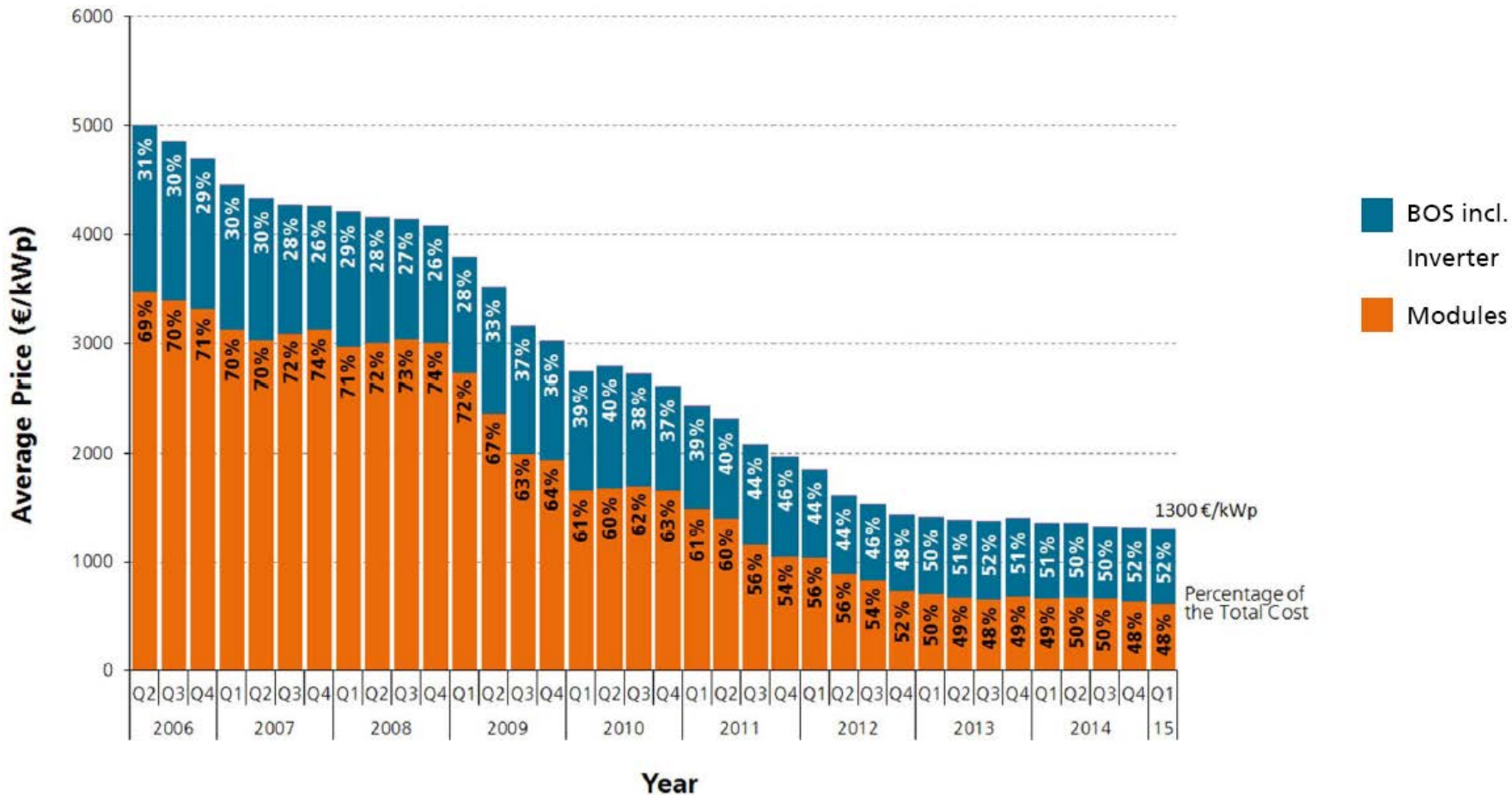
All percentages are related to total global installations, including off-grid systems.

# Energy pay-back time of mc-Si PV rooftop systems - geographical comparison





# Average Price for PV Rooftop Systems in Germany (10kWp - 100kWp)



ფოტოვოლტაიკის ეკონომიკა და ფოლისოფია.  
დასკვნები და მომავლის პერსპექტივა.



The Siemens solar farm (2011),  
Les Mées, France:  $\sim 0.7 \text{ km}^2$ , 31  
MWp, 112000 modules, enough  
for 12000 households.